

flatten: 'a list list  $\rightarrow$  'a list

$$\text{flatten } [[1;2]; []; [3;4]] = [1;2;3;4]$$

- recursive
- foldr

$[ [1;2] ; [ ] ; [3;4] ]$   
X :: XS

$[1;2] @ [3;4] \rightarrow [1;2;3;4]$

let rec flatten l = match l with

[ ] → [ ]

| x :: xs → x @ flatten xs ;

flatten : 'a list list → 'a list = <fun>

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let flatten l =

let f x y = x @ y

in foldr f [ ] l ;

flatten : 'a list list → 'a list



let rec split l x = match l with

[ ] → ([ ], [ ])

| y :: ys → let (l1, l2) = split ys x  
in if y ≤ x then (y :: l1, l2)  
else (l1, y :: l2);;

let rec split l el =

let rec f cmp ls el = match ls with

[] -> []

| x::xs when cmp x el ->  
- x::f cmp xs el

| x::xs when not cmp x el ->  
f cmp xs el

in (f (pred x >=) l el, f (pred x <) l el) ;

let split l x =

let f el (l1, l2) = if el <= x then  
(el :: l1, l2)  
else (l1, el :: l2)

in foldr f ([], []) l []





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$$f \times y = \frac{\text{let } (l_1, l_2) = y}{m}$$

$$f \times y = \frac{\text{match } y \text{ with}}{(l_1, l_2) \rightarrow}$$

automap : ('a → 'b) \* 'a list → 'b list

ogni elemento delle liste risultate è  
ottenuto applicando il primo elemento della  
coppia al secondo.

ma1 ma2 let ma2 x = x + 2;

automap [(ma1, 5); (ma2, 5); (ma1, 6)]

= [6; 7; 7]

nic foldr

let rec automap l = match l with

[ ] → [ ]

| (f, x) :: xs ⇒ f x :: automap xS ij

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let automap l =

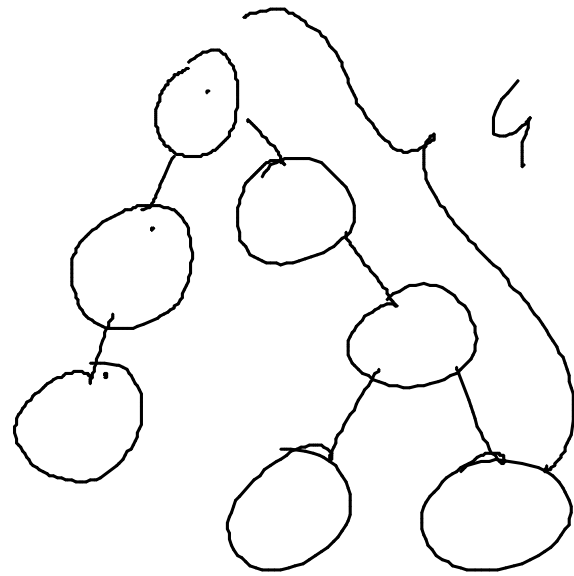
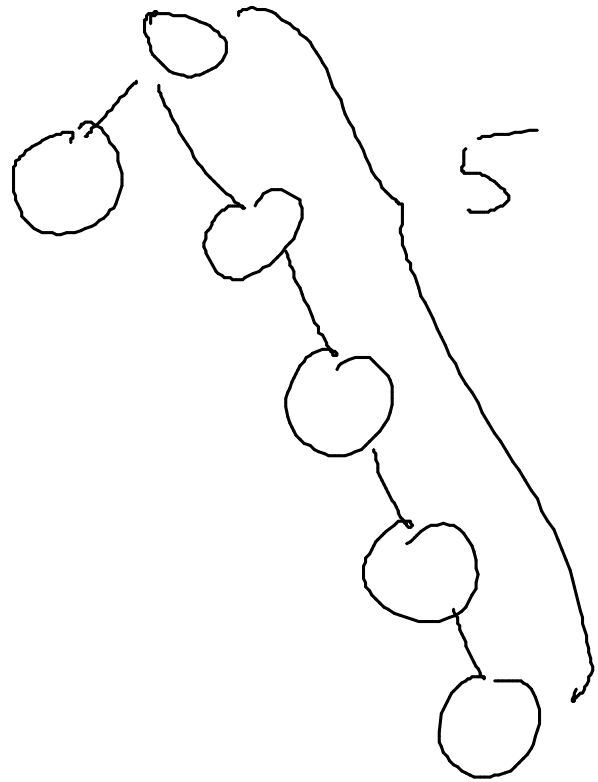
let f (g, x) y = g x :: y

in foldr f [] l ij

x :: ys → let (f, w) = x in (f w) :: automap yS

type 'a btree = Void | Node of 'a \* 'a btree \* 'a btree;;

let rec depth bt =



let rec depth bt = match bt with

Void  $\rightarrow$  0

| Node(x, lbt, rbt)  $\rightarrow$  let p1 = depth lbt

and p2 = depth rbt

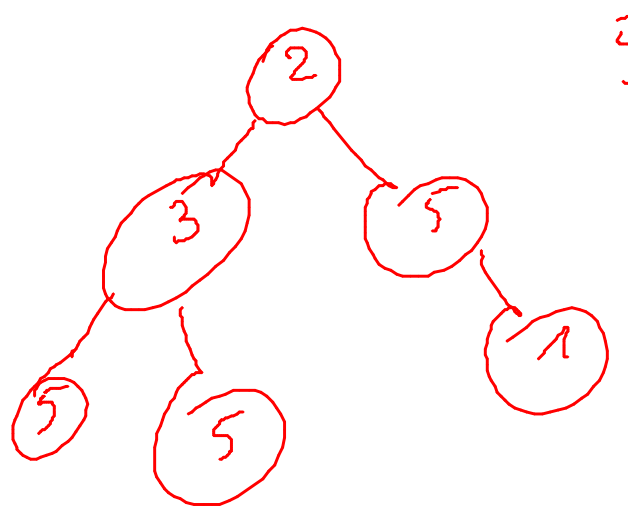
in if  $p1 < p2$  then p2 + 1

else p1 + 1 ;;

Node  $(x, lbt, rbt) \rightarrow$  if  $(\text{depth } lbt) < (\text{depth } rbt)$   
then  $(\text{depth } rbt) + 1$   
else  $(\text{depth } lbt) + 1$

let  $acc$  conta bt  $x =$  numero di occorrenze di  $x$  in bt

Conta



$$5 = 3$$

$$20 = \emptyset$$

$$1 = 1$$

let rec count\_bt x = match bt with

Void  $\rightarrow$  0

| Node (y, lbt, rbt) when x=y  $\rightarrow$  1 + (count\_bt x) +  
(count\_bt x)

| Node (y, lbt, rbt) when x <> y  $\rightarrow$  (count\_bt x) +  
(count\_bt x) ;

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lbt rec . . . .

$$\begin{aligned} |Node(y, lbt, rbt) \rightarrow & (count\ lbt\ x) + \\ & (count\ rbt\ x) + \\ & (if\ x=y\ then\ 1\ else\ 0) \end{aligned}$$