

# TOWARDS A BETTER UNDERSTANDING OF ADDICTION ON SOCIAL NETWORK: A METRIC COMPARISON

Graph Mining Presentation  
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# INTRODUCTION

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- **Aim:** to study the problem of Internet addiction and its spread through interaction on social network

## Our proposal:

- a Hybrid Automata model of the Dopaminergic System, used to simulate the activity of a user type on a virtual social network
- To test different network topologies



# THE MODEL OF DOPAMINERGIC SYSTEM

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- **Dopamine concentration.** The equation describes the dynamics of variable  $D$  representing the dopamine concentration in the prefrontal cortex:

$$\frac{dD}{dt} = \alpha \left( -D + k + \begin{cases} 1, & \text{if } r - M \geq \theta_p \\ 0, & \text{if } \theta_n \leq r - M \leq \theta_p \\ -\frac{D*M}{2}, & \text{if } r - M \leq \theta_n \end{cases} \right)$$

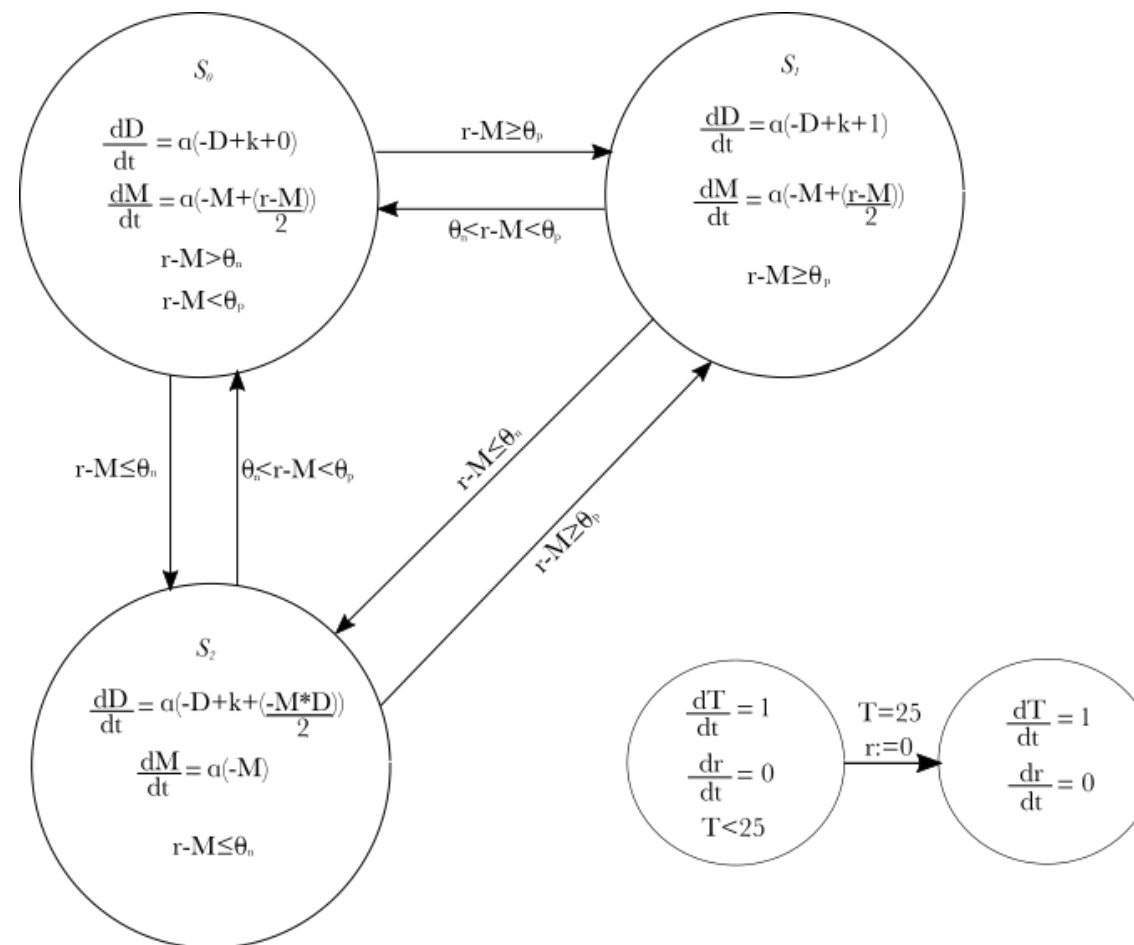
- **Memory.** The equation describes the opponent process (a contrary emotional reaction to a previous stimulus) that is modelled as a memorisation process of previous stimuli.

$$\frac{dM}{dt} = \alpha \left( -M + \begin{cases} \frac{r-M}{2}, & \text{if } r > M \\ 0, & \text{otherwise} \end{cases} \right)$$

# HYBRID AUTOMATA MODEL

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Hybrid Automata are finite state automata in which states are associated to differential equations that describe the dynamics of a set of continuous variables.



- Compositionality of Hybrid Automata
- Better description of transition



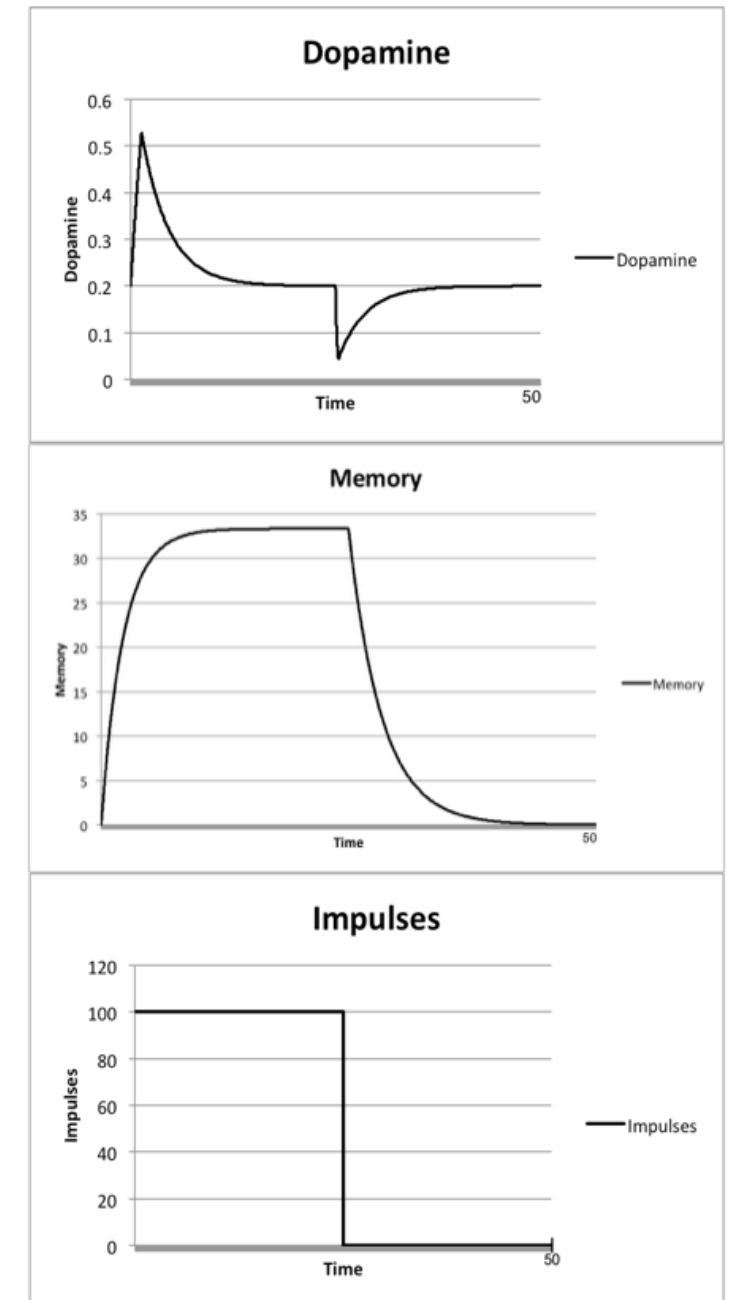
# SIMULATION AT CONSTANT PULSE

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The **trend of dopamine**, similar to the graph obtained by Gutkin, shows an initial peak which results in a withdrawal symptom, previous to the interruption of the stimulus itself.

The performance of the memory, however, corresponds to the **opponent process**.

To establish if a user became addicted, we consider the memory threshold:  $M \geq 15$



# THE INTERNET ADDICTION

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Excessive use of Internet as a mechanism to **escape** from the daily dissatisfaction.

Main expressions:

- Gaming
- Social network
- Surfing



We represent the social network as a **graph**:

- Each node of graph is a **user**
- Each user is characterised by the Dopaminergic System and the **propensity factor**



# THE PROPENSITY FACTOR

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- It is a parameter, which spans the range  $[0,1]$ , to model the user's predisposition to communicate
- It influences the probability to send (or reply) messages through the social network

# THE NETWORK COMMUNICATION MODEL

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- Each user can send at most **one message each day**
- The probability to send a message is proportional to his/her propensity factor. If he/she sends a message, this is received by his/her neighbours
- On the same day, all users that have received one or more messages choose whether to reply or not, again with a probability proportional to their propensity factors.

Stimuli:

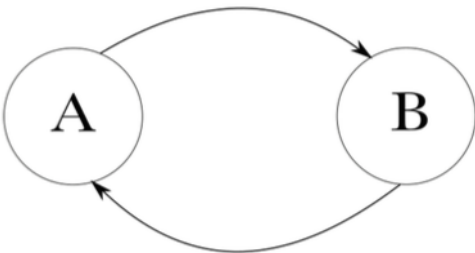
- **medium-high:** when user receives a message
- **high:** when an addicted\* user sends a message (*prediction error phenomenon*)

\*Memory  $\geq 15$



# GRAPH WITH ONLY TWO NODES

This graph is used to **examine the role of the propensity factor**. All the possible combinations of users have been tested to study the behaviour of the Dopaminergic System in different situations



		User B										
User A		0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
	0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0
	0.1	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=66	A=0; B=97	A=0; B=99
	0.2	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=83	A=0; B=100	A=0; B=100	A=0; B=100	A=0; B=100	A=0; B=100	A=0; B=100
	0.3	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=0	A=0; B=95	A=1; B=100	A=2; B=100	A=6; B=100	A=6; B=100	A=5; B=100	A=8; B=100
	0.4	A=0; B=0	A=0; B=0	A=90; B=0	A=96; B=3	A=95; B=96	A=93; B=100	A=91; B=100	A=96; B=100	A=91; B=100	A=94; B=100	A=93; B=100
	0.5	A=0; B=0	A=0; B=0	A=100; B=0	A=100; B=5	A=100; B=94	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
	0.6	A=0; B=0	A=0; B=0	A=100; B=0	A=100; B=6	A=100; B=96	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
	0.7	A=0; B=0	A=0; B=0	A=100; B=0	A=100; B=2	A=100; B=95	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
	0.8	A=0; B=0	A=51; B=0	A=100; B=0	A=100; B=2	A=100; B=99	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
	0.9	A=0; B=0	A=88; B=0	A=100; B=0	A=100; B=5	A=100; B=96	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
	1	A=0; B=0	A=99; B=0	A=100; B=0	A=100; B=2	A=100; B=96	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100	A=100; B=100
		None			One		Both					
		<input type="checkbox"/>			<input type="checkbox"/>		<input type="checkbox"/>					

- We find three values:
- low propensity: 0.2
  - medium propensity: 0.35
  - high propensity: 0.9

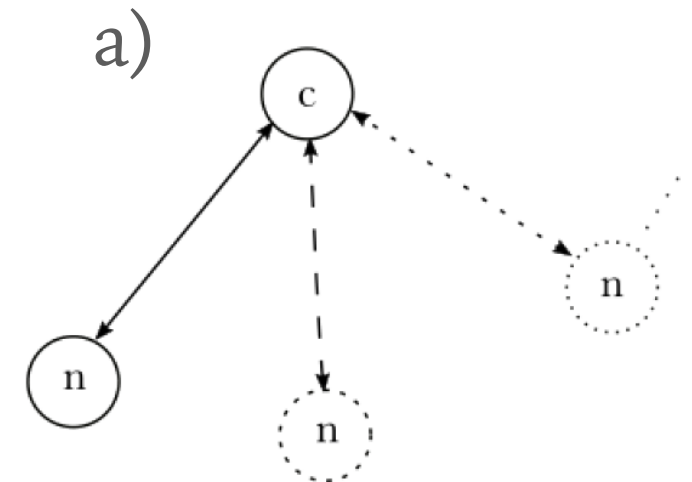
# EXPERIMENTS WITH STAR GRAPH

a) To study the propagation of addiction in a graph, we start by considering how many peripheral nodes  $n$  are necessary to cause addiction of the central node  $c$ , according to different propensity factor.

		Nodes N		
Node C		0.2	0.35	0.9
	0.2	9	7	4
	0.35	3	1	1
	0.9	1	1	1

Few Nodes      More Nodes

■                      ■

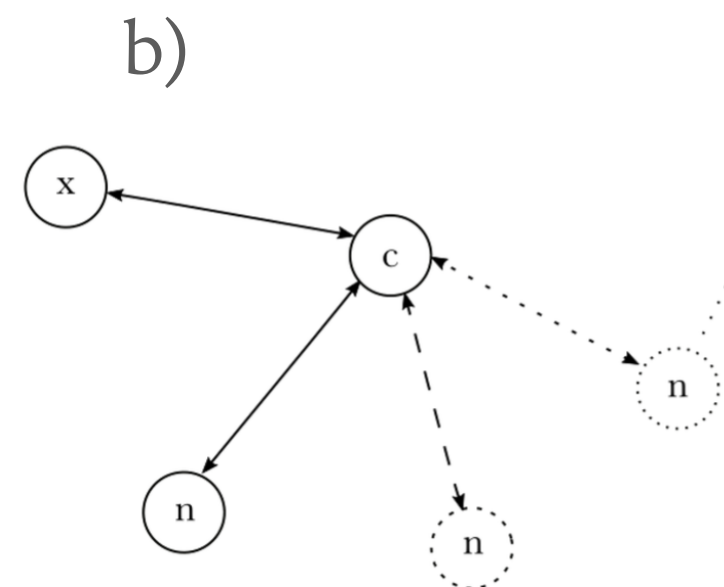


b) After, we study how one of the peripheral nodes  $x$  whose propensity factor is 0.2 (fixed) can be influenced by the others (both  $c$  and  $n$ ).

		Nodes N		
Node C		0.2	0.35	0.9
	0.2	44	36	17
	0.35	17	13	5
	0.9	15	7	4

Few Nodes      More Nodes

■                      ■

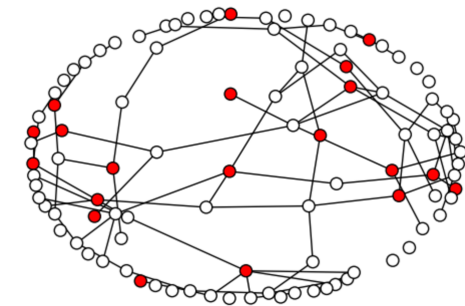
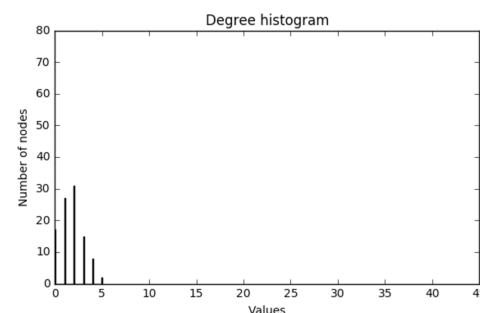




# EXPERIMENTS WITH RANDOM AND SCALE-FREE NETWORKS

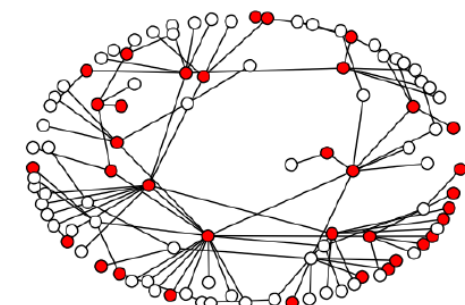
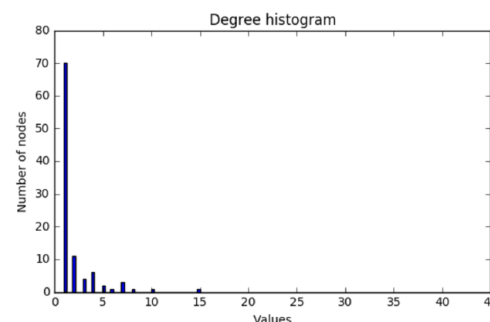
For our experiments, we used three kinds of networks of 100 nodes, generated in different ways:

a) with the Erdős-Rényi graph (ER), approach:



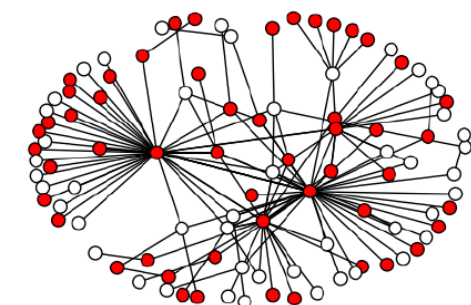
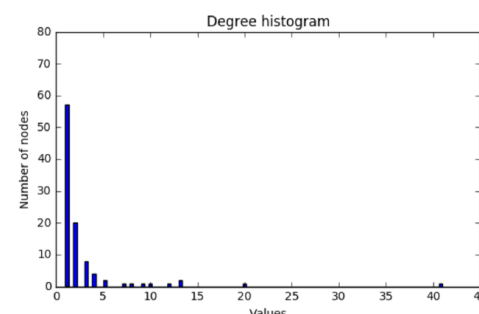
20 nodes addicted in ER

b) with the Barabási-Albert (BA) approach:



35 nodes addicted in BA

c) with the Bollobás-Riordan (BR) approach:



52 nodes addicted in BR

# EXPERIMENTS WITH HUGER GRAPH

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## Real dataset information:

- This dataset consists of 'circles' (or 'friends lists') from Facebook (by SNAP)
- Number of nodes: 4039
- Number of edges: 88234

## A scale free graph (Barabasi):

- Number of nodes: 4039
- Number of edges: 88334

## A random graph (Erdős-Rényi):

- Number of nodes: 4039
- Number of edges: 88234

# CLOSENESS CENTRALITY

Closeness centrality can be regarded as a measure of how long it will take to spread information from  $v$  to all other nodes sequentially.

The more central a node is, the lower its total distance to all other nodes.

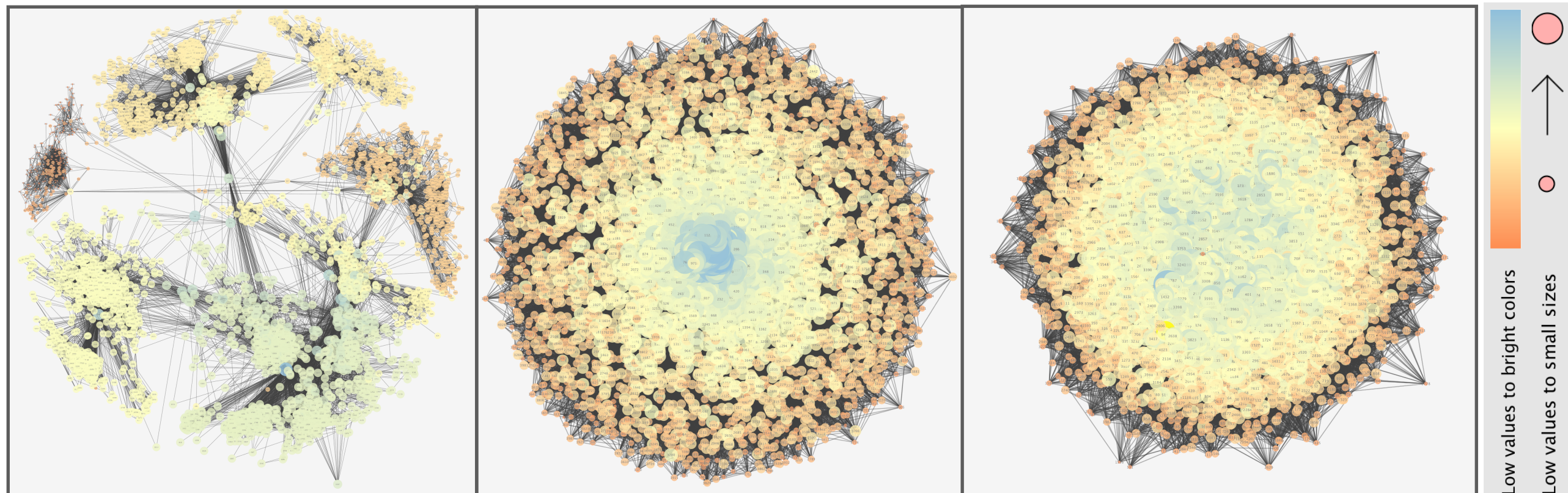
THE MAX VALUE OF CLOSENESS CENTRALITY:

Real Graph	Barabasi Graph	Random Graph
0.45	0.53	0.41

REAL GRAPH

BARABASI GRAPH

RANDOM GRAPH





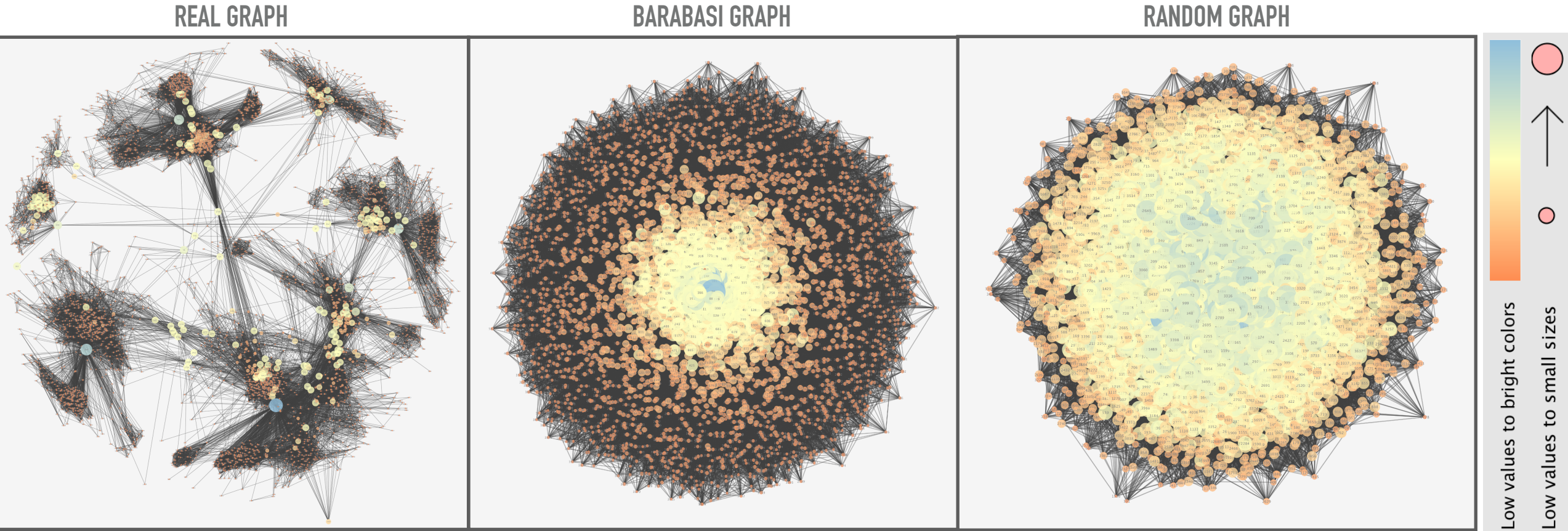
# BETWEENNESS CENTRALITY

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Betweenness centrality quantifies the number of times a node acts as a bridge along the shortest path between two other nodes.

In this conception, vertices that have a high probability to occur on a randomly chosen shortest path between two randomly chosen vertices have a high betweenness.

THE MAX VALUE OF BETWEENNESS CENTRALITY:

Real Graph	Barabasi Graph	Random Graph
0.48	0.021	0.001





# DEGREE CENTRALITY

**Degree centrality:** a highly effective measure of the influence or importance of a node.

In many social network settings people with more connections tend to have more power and more visibility.

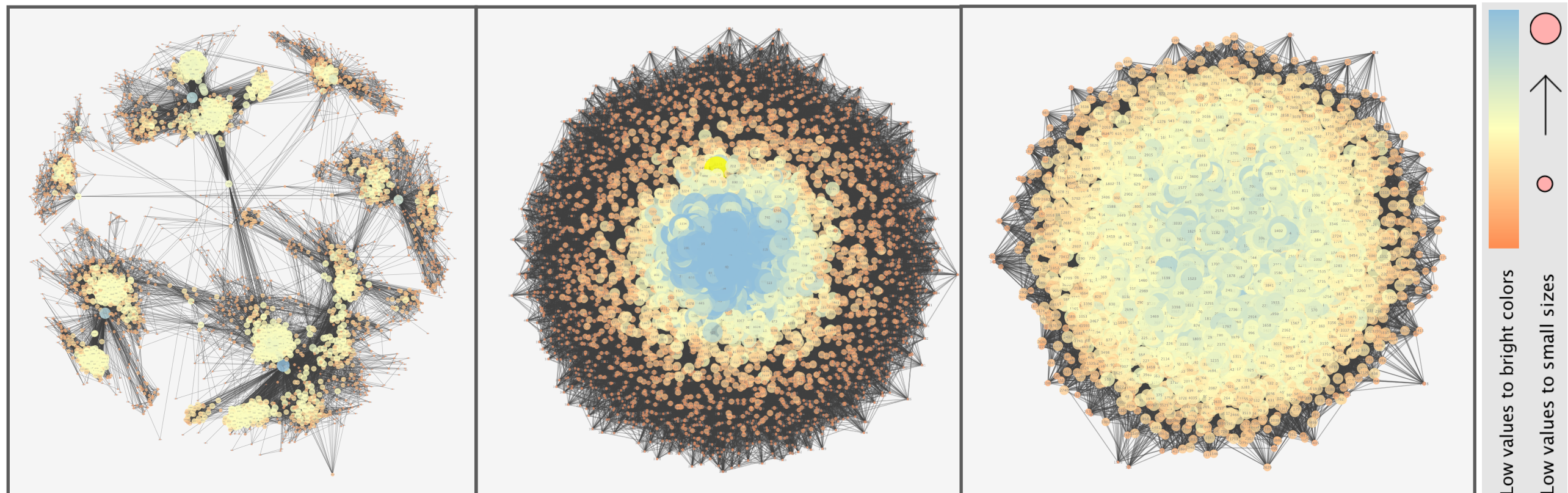
THE MAX VALUE OF DEGREE CENTRALITY:

Real Graph	Barabasi Graph	Random Graph
0.25	0.1	0.017

REAL GRAPH

BARABASI GRAPH

RANDOM GRAPH



# CLUSTERING COEFFICIENT

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**Clustering coefficient:** is a measure of the degree to which nodes in a graph tend to cluster together.

Evidence suggests that in most real-world networks, and in particular social networks, nodes tend to create tightly knit groups characterised by a relatively high density of ties.

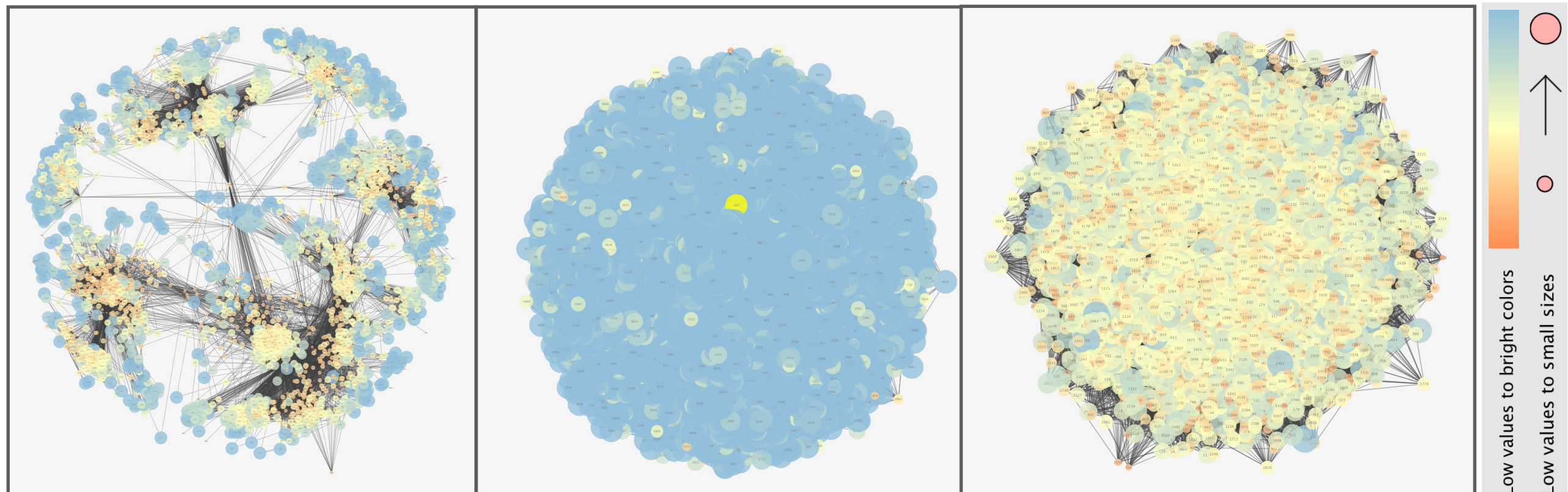
THE MAX VALUE OF CLUSTERING COEFFICIENT:

Real Graph	Barabasi Graph	Random Graph
0.606	0.038	0.011

REAL GRAPH

BARABASI GRAPH

RANDOM GRAPH





# ANALYSIS OF THE SPREAD OF THE ADDICTION

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- To test the model, we count the number of addicted nodes (performing 100 simulations for each kind of graph)
- As expected, the topology and not the size of the network is responsible for the largest impact on Internet addiction
- Considering the model of communication, the most influential metrics are closeness and betweenness

THE AVERAGE NUMBER OF ADDICTED NODES (CALCULATING ON 100 SIMULATIONS):

Real Graph	Barabasi Graph	Random Graph
3541.5	3467.2	2990.4

# ANALYSIS OF THE SPREAD OF THE ADDICTION

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- Considering the model of communication, the most influential metrics are closeness and betweenness
- The nodes characterised with the highest values of closeness and betweenness are the first ones to become addicted

THE NODES WITH THE HIGHEST VALUE OF CLOSENESS AND BETWEENNESS:

	Real Graph	Barabasi Graph	Random Graph
Closeness	User 107	User 25	User 2518
Betweenness	User 107	User 28	User 2518

# CONCLUSIONS

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- To propose a computational framework for the study of addiction
- To use the theory of Hybrid Automata to develop a modular model of the Dopaminergic System
- To study how addiction is correlated to network topologies
- To study different metrics on different networks

## Future work:

- Further validation of our model on a network of the messaging exchange
- To investigate different stimuli



The background is an abstract composition of overlapping, semi-transparent circles in various shades of green, blue, and purple. The circles are layered, creating a sense of depth and movement. The colors are muted and earthy, with some areas appearing darker due to the layering. The overall texture is soft and painterly.

*Thank you!*