# Bottom-up Parsing

# Recap of Top-down Parsing

- Top-down parsers build syntax tree from root to leaves
- Left-recursion causes non-termination in top-down parsers
  - Transformation to eliminate left recursion
  - Transformation to eliminate common prefixes in right recursion
- FIRST, FIRST+, & FOLLOW sets + LL(1) condition
  - LL(1) uses <u>l</u>eft-to-right scan of the input, <u>l</u>eftmost derivation of the sentence, and  $\underline{1}$  word lookahead
  - LL(1) condition means grammar works for predictive parsing
- Given an LL(1) grammar, we can
  - Build a recursive descent parser
  - Build a table-driven LL(1) parser
- LL(1) parser doesn't explicitly build the parse tree
  - Keeps lower fringe of partially complete tree on the stack

# Parsing Techniques

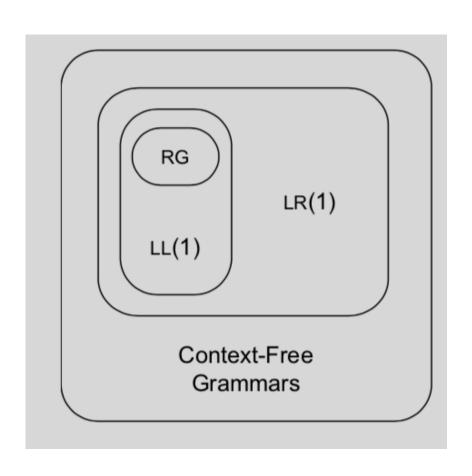
Top-down parsers (LL(1), recursive descent)

- Start at the root of the parse tree and grow toward leaves
- Pick a production & try to match the input
- Bad "pick" ⇒ may need to backtrack
- Some grammars are backtrack-free (predictive parsing)

Bottom-up parsers (LR(1), operator precedence)

- Start at the leaves and grow toward root
- As input is consumed, encode possibilities in an internal state
- Bottom-up parsers handle a large class of grammars

# Bottom-up parser handle a larger class of grammars



The point of parsing is to construct a <u>derivation</u>

A derivation consists of a series of rewrite steps

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow sentence$$

- Each  $\gamma_i$  is a sentential form
  - If  $\gamma$  contains only terminal symbols,  $\gamma$  is a sentence in L(G)
  - If  $\gamma$  contains 1 or more non-terminals,  $\gamma$  is a sentential form
- To get  $\gamma_i$  from  $\gamma_{i-1}$ , expand some NT  $A \in \gamma_{i-1}$  by using  $A \rightarrow \beta$ 
  - Replace the occurrence of  $A \in \gamma_{i-1}$  with  $\beta$  to get  $\gamma_i$
  - In a leftmost derivation, it would be the first NT  $A \in \gamma_{i-1}$

A left-sentential form occurs in a <u>leftmost</u> derivation

A right-sentential form occurs in a rightmost derivation

Bottom-up parsers build a rightmost derivation in reverse

## Bottom-up Parsing

A bottom-up parser builds a derivation by working from the input sentence back toward the start symbol S

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow \text{sentence}$$

To reduce  $\gamma_i$  to  $\gamma_{i-1}$  match some rhs  $\beta$  against  $\gamma_i$  then replace  $\beta$  with its corresponding lhs, A. (assuming the production  $A \rightarrow \beta$ )

# Bottom-up Parsing

In terms of the parse tree, it works from leaves to root

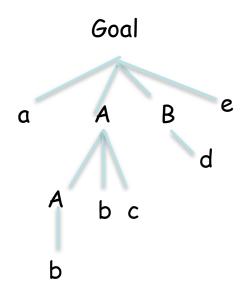
Nodes with no parent in a partial tree form its upper fringe (border)

#### Consider the grammar

0	Goal	$\rightarrow$	<u>a</u> A B <u>e</u>
1	Α	$\rightarrow$	А <u>b</u> <u>c</u>
2		1	<u>b</u>
3	В	$\rightarrow$	<u>d</u>

• Since each replacement of  $\beta$  with A shrinks the upper fringe, we call it a reduction. (remember we are constructing a rightmost derivation)

#### The input string abbcde



While the process of finding the next reduction appears to be almost oracular, it can be automated in an efficient way for a large class of grammars

0	Goal	$\rightarrow$	<u>a</u> A B <u>e</u>
1	Α	$\rightarrow$	А <u>ь</u> с
2		1	<u>b</u>
3	В	$\rightarrow$	<u>d</u>

The input string abbcde

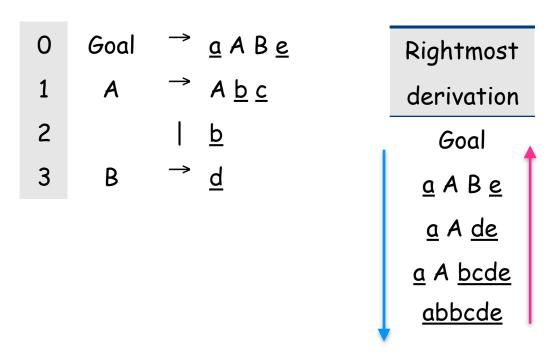
Sentential	Reduction		
Form	Prod'n	Pos'n	
<u>ab</u> bcde	2	2	
<u>a</u> A <u>bcde</u>	1	4	
<u>a</u> A <u>de</u>	3	3	
<u>a</u> A B <u>e</u>	0	4	
Goal	_	_	

The trick is scanning the input and finding the next reduction.

The mechanism for doing this must be efficient

"Position" specifies where the right end of  $\beta$  occurs in the current sentential form.

# Leftmost reductions for rightmost derivations



To reconstruct a Rightmost derivation bottom up we have to look for the leftmost substring that matches a right handside of a derivation!

# Finding Reductions

## (Handles)

The parser must find a substring  $\beta$  of the tree's frontier that matches some production  $A \to \beta$  that occurs as one step in the rightmost derivation. We call this substring  $\beta$  an handle

An handle of a right-sentential form  $\gamma$  is a pair  $\langle A \rightarrow \beta, k \rangle$  where  $A \rightarrow \beta \in P$  and k is the position in  $\gamma$  of  $\beta$ 's rightmost symbol.

If  $\langle A \rightarrow \beta, k \rangle$  is a handle, then replacing  $\beta$  at k with A produces the right sentential form from which  $\gamma$  is derived in the rightmost derivation.

For this string is b not d!!

handles	<b>A-&gt;</b> β	k
→ <u>abbcde</u>	2	2
<u>a</u> A <u>bc</u> de	1	4
<u>a</u> A <u>de</u>	3	3
<u>a</u> A B <u>e</u>	0	4
Goal	_	_

# A property of handles

Because  $\gamma$  is a right-sentential form, the substring to the right of a handle contains only terminal symbols

handles	<b>Α-&gt;</b> β	k
<u>abbcde</u>	2	2
<u>a</u> A <u>bcde</u>	1	4
<u>a</u> A <u>de</u>	3	3
<u>a</u> A B <u>e</u>	0	4
Goal	_	_

# Example

0	Goal	$\rightarrow$	Expr
1	Expr	$\rightarrow$	Expr + Term
2			Expr - Term
3			Term
4	Term	$\rightarrow$	Term * Factor
5			Term / Factor
6			Factor
7	Factor	$\rightarrow$	number
8		1	<u>id</u>
9			(Expr)

Bottom up parsers handle either left-recursive or right-recursive grammars.

A simple left-recursive form of the classic expression grammar

# Example

#### derivation

0	Goal	$\rightarrow$	Expr
1	Expr	$\rightarrow$	Expr + Term
2			Expr - Term
3			Term
4	Term	$\rightarrow$	Term * Factor
5			Term / Factor
6			Factor
7	Factor	$\rightarrow$	<u>number</u>
8			<u>id</u>
9			(Expr)

Prod'n	Sentential Form
_	Goal
0	Expr
2	Expr - Term
4	Expr - Term * Factor
8	Expr - Term * <id,y></id,y>
6	Expr - Factor * <id,y></id,y>
7	Expr - <num,2> * <id,y></id,y></num,2>
3	Term- <num,2>*<id,y></id,y></num,2>
6	Factor - <num,2> * <id,y></id,y></num,2>
8	<id,<u>x&gt; - <num,<u>2&gt; * <id,<u>y&gt;</id,<u></num,<u></id,<u>

Rightmost derivation of  $\times -2 \times y$ 

# Example

0	Goal	$\rightarrow$	Expr
1	Expr	$\rightarrow$	Expr + Term
2			Expr - Term
3			Term
4	Term	$\rightarrow$	Term * Factor
5			Term / Factor
6			Factor
7	Factor	$\rightarrow$	number
8			<u>id</u>
9			(Expr)

			_
Prod'n	Sentential Form	Handle	1
_	Goal	_	
0	Expr	0,1	
2	Expr - Term	2,3	
4	Expr - Term * Factor	4,5	
8	Expr - Term * <id,y></id,y>	8,5	
6	Expr - Factor * <id,y></id,y>	6,3	
7	Expr - <num,2> * <id,y></id,y></num,2>	7,3	
3	Term- <num,2>*<id,y></id,y></num,2>	3,1	
6	Factor - <num,2> * <id,y></id,y></num,2>	6,1	
8	<id,<u>x&gt; - <num,<u>2&gt; * <id,<u>y&gt;</id,<u></num,<u></id,<u>	8,1	pars

Handles for rightmost derivation of  $\times -2 \times y$ 

A bottom-up parser repeatedly finds a handle  $A \rightarrow \beta$  in the current right-sentential form and replaces  $\beta$  with A.

To construct a rightmost derivation

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow w$$

Apply the following conceptual algorithm

for i 
$$\leftarrow$$
 n to 1 by -1 of course, n is unknown Find the handle  $\langle A_i \rightarrow \beta_i$ ,  $k_i >$  in  $\gamma_i$  until the derivation is built Replace  $\beta_i$  with  $A_i$  to generate  $\gamma_{i-1}$ 

This takes 2n steps

#### More on Handles

Bottom-up reduce parsers find a rightmost derivation in reverse order

- Rightmost derivation ⇒ rightmost NT expanded at each step in the derivation
- Processed in reverse ⇒ parser proceeds left to right

These statements are somewhat counter-intuitive

# Handles Are Unique

#### Theorem:

If G is unambiguous, then every right-sentential form has a unique handle.

#### Sketch of Proof:

- 1 G is unambiguous  $\Rightarrow$  rightmost derivation is unique
- 2  $\Rightarrow$  a unique production  $A \rightarrow \beta$  applied to derive  $\gamma_i$  from  $\gamma_{i-1}$
- $\Rightarrow$  a unique position k at which  $A \rightarrow \beta$  is applied
- 4  $\Rightarrow$  a unique handle  $\langle A \rightarrow \beta, k \rangle$

This all follows from the definitions

If we can find the handles, we can build a derivation!

# Shift-reduce Parsing

To implement a bottom-up parser, we adopt the shift-reduce paradigm

A shift-reduce parser is a stack automaton with four actions

- Shift next word is shifted onto the stack (push)
- Reduce right end of handle is at top of stack
   Locate left end of handle within the stack
   Pop handle off stack & push appropriate lhs
- Accept stop parsing & report success
- Error call an error reporting/recovery routine

Reduce consists in |rhs| pops & 1 push

But how does the parser know when to shift and when to reduce? It shifts until it has a handle at the top of the stack.

#### A simple shift-reduce parser:

```
push $
token \leftarrow next\_token()
repeat until (top of stack = Goal and token = EOF)
   if the top of the stack is a handle A \rightarrow \beta
                // reduce \beta to A
       then
          pop |\beta| symbols off the stack
          push A onto the stack
       else if (token \neq EOF)
          then // shift
               push token
               token \leftarrow next_token()
       else // need to shift, but out of input
     report an error
```

- It fails to find a handle
- Thus, it keeps shifting
- Eventually, it consumes all input

This parser reads all input before reporting an error, not a desirable property.

Error localization is an issue in the handle-finding process that affects the practicality of shift-reduce parsers...

We will fix this issue later.

# Back to <u>x = 2 \* y</u>

Stack	Input	Handle	Action
\$	<u>id</u> - <u>num</u> * <u>id</u>	none	shift
\$ <u>id</u>	- <u>num</u> * <u>id</u>	8,1	reduce 8
\$ Factor	- <u>num</u> * <u>id</u>	6,1	reduce 6
\$ Term	- <u>num</u> * <u>id</u>	3,1	reduce 3
\$ Expr	- <u>num</u> * <u>id</u>		

Expr is not a handle at this point because it does not occur in this point in a rightmost derivation of id - num \* id

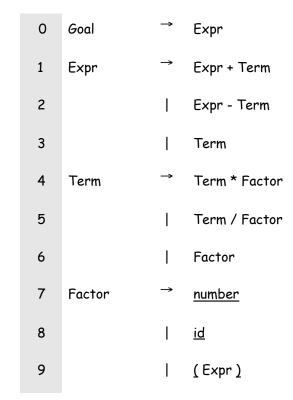
While that statement sounds like oracular mysticism, we will see that the decision can be automated efficiently.

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle and reduce

0	Goal	$\rightarrow$	Expr
1	Expr	$\rightarrow$	Expr + Term
2		I	Expr - Term
3		I	Term
4	Term	$\rightarrow$	Term * Factor
5		I	Term / Factor
6		1	Factor
7	Factor	$\rightarrow$	<u>number</u>
8		I	<u>id</u>
9		l	(Expr)

Stack	Input	Handle	Action
\$	<u>id - num * id</u>	none	shift
\$ <u>id</u>	- <u>num</u> * <u>id</u>	8,1	reduce 8
\$ Factor	- <u>num</u> * <u>id</u>	6,1	reduce 6
\$ Term	- <u>num</u> * <u>id</u>	3,1	reduce 3
\$ Expr	- <u>num</u> * <u>id</u>	none	shift
\$ Expr -	num * id	none	shift
\$ Expr - <u>num</u>	* <u>id</u>	7,3	reduce 7
\$ Expr - Factor	* <u>id</u>	6,3	reduce 6
\$ Expr - Term	* <u>id</u>	none	shift
\$ Expr - Term *	<u>id</u>	none	shift
\$ Expr - Term * <u>id</u>		8,5	reduce 8
\$ Expr - Term * Factor		4,5	reduce 4
\$ Expr - Term		2,3	reduce 2
\$ Expr		0,1	reduce 0
\$ Goal		none	accept

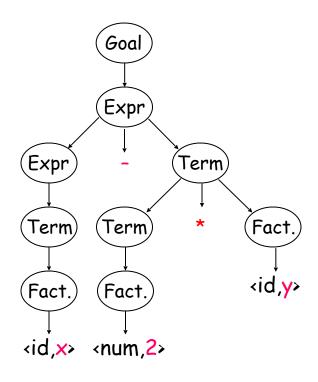
- 1. Shift until the top of the stack the right end of a handle
- 2. Find the left end of the handle and reduce



5 shifts + 9 reduces + 1 accept

# Parse tree for x = 2 \* y

Stack	Input	Action
\$	<u>id</u> - <u>num</u> * <u>id</u>	shift
\$ <u>id</u>	- <u>num</u> * <u>id</u>	reduce 8
\$ Factor	- <u>num</u> * <u>id</u>	reduce 6
\$ Term	- <u>num</u> * <u>id</u>	reduce 3
\$ Expr	- <u>num</u> * <u>id</u>	shift
\$ Expr -	<u>num</u> * <u>id</u>	shift
\$ Expr - <u>num</u>	* <u>id</u>	reduce 7
\$ Expr - Factor	* <u>id</u>	reduce 6
\$ Expr - Term	* <u>id</u>	shift
\$ Expr - Term *	<u>id</u>	shift
\$ Expr - Term * <u>id</u>		reduce 8
\$ Expr - Term * Factor		reduce 4
\$ Expr - Term		reduce 2
\$ Expr		reduce O
\$ Goal		accept



Corresponding Parse Tree

# An Important Lesson about Handles

An handle must be a substring of a sentential form  $\gamma$  such that :

- It must match the right hand side  $\beta$  of some rule  $A \rightarrow \beta$ ; and
- There must be some rightmost derivation from the goal symbol that produces the sentential form  $\gamma$  with A  $\to \beta$  as the last production applied
- Simply looking for right hand sides that match strings is not good enough

Critical Question: How can we know when we have found an handle without generating lots of different derivations?

Answer: We use left context encoded in a "parser state" and a lookahead at the next word in the input. (Formally, 1 word beyond the handle.)

• LR(1) parsers use states to encode information on the left context and also use 1 word beyond the handle.

The additional left context is precisely the reason that LR(1) grammars express a superset of the languages that can be expressed as LL(1) grammars

Such information is encoded in a GOTO and ACTION tables

The actions are driven by the state and the lookhaed

- LR(1) parsers are table-driven, shift-reduce parsers that use a limited right context (1 token) for handle recognition
- The class of grammars that these parsers recognize is called the set of LR(1) grammars

A grammar is LR(1) if, given a rightmost derivation

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow \text{sentence}$$

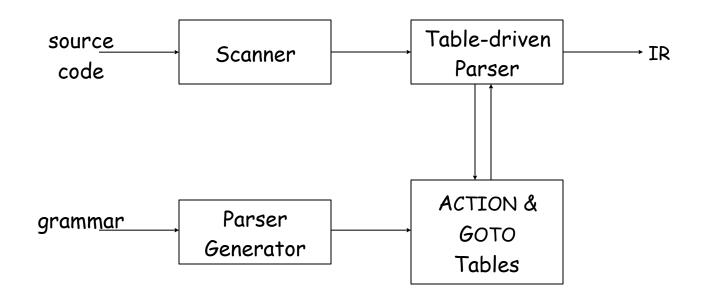
We can

- 1. isolate the handle of each right-sentential form  $\gamma_i$ , and
- 2. determine the production by which to reduce,

going at most 1 symbol beyond the right end of the handle of  $\gamma_{\rm i}$ 

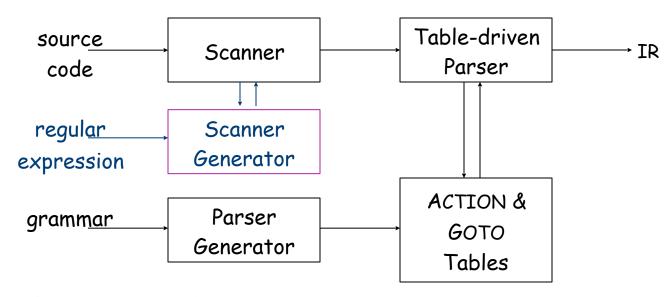
LR(1) means left-to-right scan of the input, rightmost derivation (in reverse), and 1 word of lookahead.

#### A table-driven LR(1) parser looks like



Tables <u>can</u> be built by hand However, this is a perfect task to automate

A table-driven LR(1) parser looks like



Tables <u>can</u> be built by hand However, this is a perfect task to automate Just like automating construction of scanners ...

## LR(1) Skeleton Parser

```
stack.push($);
stack.push(s_0);
                                  // initial state
token = scanner.next token();
loop forever {
     s = stack.top();
     if (ACTION[s,token] == "reduce A \rightarrow \beta") then {
        stack.popnum(2*|\beta|); // pop 2*|\beta| symbols
        s = stack.top();
        stack.push(A); // push A
        stack.push(GOTO[s,A]); // push next state
     else if (ACTION[s,token] == "shift s;") then {
           stack.push(token); stack.push(s;);
           token \leftarrow scanner.next token();
     else if ( ACTION[s,token] == "accept"
                      & token == EOF)
           then break:
     else throw a syntax error;
report success;
```

#### The skeleton parser

- relies on a stack & a scanner
- uses two tables, called ACTION & GOTO

ACTION: state x word → action

GOTO: state  $\times$  NT  $\rightarrow$  state

 detects errors by failure of the other three cases

### To make a parser for L(G), need a set of tables

#### The grammar

```
    1 Goal → SheepNoise
    2 SheepNoise → SheepNoise baa
    3 | baa
```

#### For now assume we have the tables

ACTION Table			
State EOF <u>baa</u>			
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State SheepNoise		
0	1	
1	0	
2	0	
3	0	

# The string baa

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> EOF	

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3		-	<u>baa</u>

ACTION Table			
State EOF		<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State SheepNoise		
0	1	
1	0	
2 0		
3 0		

# The string <u>baa</u>

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> EOF	shift 2
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	EOF	

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3			<u>baa</u>

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State	SheepNoise	
0	1	
1	0	
2	0	
3	0	

# The string baa

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> EOF	shift 2
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	EOF	reduce 3
$s_0 SN s_1$	EOF	

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3		1	<u>baa</u>

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State	SheepNoise	
0	1	
1	0	
2	0	
3	0	

# The string <u>baa</u>

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> EOF	shift 2
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	EOF	reduce 3
$s_0 SN s_1$	EOF	accept

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3		1	<u>baa</u>

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State	SheepNoise	
0	1	
1	0	
2	0	
3	0	

Stack	Input	Action	1	Goal	$\rightarrow$	SheepNoise
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF		2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
¥ 30	<u> </u>		3		1	<u>baa</u>

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table		
State SheepNoise		
0	1	
1	0	
2	0	
3	0	

Stack	Input	Action	1	Goal	$\rightarrow$	SheepNoise
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF	shift 2		SheepNoise	<b>→</b>	SheepNoise <u>baa</u>
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	<u>baa</u> EOF		3		ı	<u>baa</u>

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GC	GOTO Table		
State	State SheepNoise		
0	1		
1	0		
2	0		
3	0		

## The string <u>baa</u> <u>baa</u>

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF	shift 2
\$ s <sub>0</sub> baa s <sub>2</sub>	<u>baa</u> EOF	reduce 3
$$s_0 SNs_1$	<u>baa</u> EOF	

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3			<u>baa</u>

Last example, we faced EOF and we accepted. With <u>baa</u>, we shift ...

	ACTION Table			
State	EOF	<u>baa</u>		
0	_	shift 2		
1	accept	shift 3		
2	reduce 3	reduce 3		
3	reduce 2	reduce 2		

GOTO Table			
State	State SheepNoise		
0	1		
1	0		
2	0		
3	0		

Stack	Input	Action	1 Goal → SheepNoi	se
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF	shift 2	2 SheepNoise → SheepNoi	se <u>baa</u>
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	<u>baa</u> EOF	reduce 3	3   <u>baa</u>	
$s_0 SN s_1$	<u>baa</u> EOF	shift 3		
\$ s <sub>0</sub> SN s <sub>1</sub> <u>baa</u> s <sub>3</sub>	EOF			

	ACTION Table			
State	EOF	<u>baa</u>		
0	_	shift 2		
1	accept	shift 3		
2	reduce 3	reduce 3		
3	reduce 2	reduce 2		

GOTO Table			
State	State SheepNoise		
0	1		
1	0		
2	0		
3	0		

Stack	Input	Action	1 Goal → SheepNoise
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF	shift 2	2 SheepNoise → SheepNoise <u>baa</u>
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	<u>baa</u> EOF	reduce 3	3 <u>baa</u>
$s_0 SN s_1$	<u>baa</u> EOF	shift 3	
\$ s <sub>0</sub> SN s <sub>1</sub> baa s <sub>3</sub>	EOF	reduce 2	Now, we accept
$s_0 SNs_1$	EOF		

ACTION Table			
State	EOF	<u>baa</u>	
0	_	shift 2	
1	accept	shift 3	
2	reduce 3	reduce 3	
3	reduce 2	reduce 2	

GOTO Table			
State	SheepNoise		
0	1		
1	0		
2	0		
3	0		

Stack	Input	Action
\$ s <sub>0</sub>	<u>baa</u> <u>baa</u> EOF	shift 2
\$ s <sub>0</sub> <u>baa</u> s <sub>2</sub>	<u>baa</u> EOF	reduce 3
$s_0 SN s_1$	<u>baa</u> EOF	shift 3
$s_0 SN s_1 baa s_3$	EOF	reduce 2
$s_0 SN s_1$	EOF	accept

ACTION Table				
State	EOF	<u>baa</u>		
0	_	shift 2		
1	accept	shift 3		
2	reduce 3	reduce 3		
3	reduce 2	reduce 2		

1	Goal	$\rightarrow$	SheepNoise
2	SheepNoise	$\rightarrow$	SheepNoise <u>baa</u>
3		1	baa

GOTO Table			
State	SheepNoise		
0	1		
1	0		
2	0		
3	0		