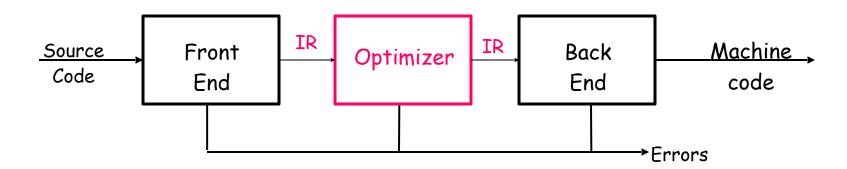
This lecture begins the material from Chapter 8 of EaC

# Introduction to Code Optimization

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## Traditional Three-Phase Compiler



### Optimization (or Code Improvement)

- Analyzes IR and rewrites (or transforms) IR
- Primary goal is to reduce running time of the compiled code
  - May also improve space, power consumption, ...

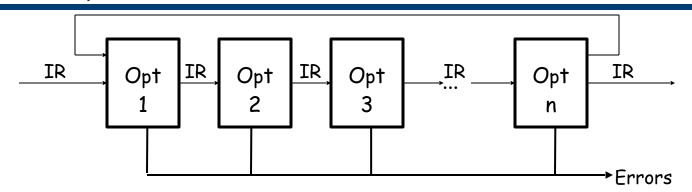
#### Transformations have to be:

- Safely applied and (it does not change the result of the running program)
- Applied when profit has expected

# Background

- Until the early 1980s optimisation was a feature should be added to the compiler only after its other parts were working well
- Debugging compilers vs. optimising compilers
- After the development of RISC processors the demand for support from the compiler

## The Optimizer



Modern optimizers are structured as a series of passes

### Typical Transformations

- Discover & propagate some constant value
- Move a computation to a less frequently executed place
- Specialize some computation based on context
- Discover a redundant computation & remove it
- Remove useless or unreachable code

## The Role of the Optimizer

- The compiler can implement a procedure in many ways
- The optimizer tries to find an implementation that is "better"
  - Speed, code size, data space, ...

## To accomplish this, it

- Analyzes the code to derive knowledge about run-time behavior
  - Data-flow analysis, pointer disambiguation, ...
  - General term is "static analysis"
- Uses that knowledge in an attempt to improve the code
  - Literally hundreds of transformations have been proposed
  - Large amount of overlap between them

## Nothing "optimal" about optimization

Proofs of optimality assume restrictive & unrealistic conditions

## Scope of Optimization

In scanning and parsing, "scope" refers to a region of the code that corresponds to a distinct name space.

In optimization "scope" refers to a region of the code that is subject to analysis and transformation.

- Notions are somewhat related
- Connection is not necessarily intuitive

Different scopes introduces different challenges & different opportunities

Historically, optimization has been performed at several distinct scopes.

# Scope of Optimization

CFG of basic blocks: BB is a maximal length sequence of straightline code.

### Local optimization

- Operates entirely within a single basic block
- Properties of block lead to strong optimizations

### Regional optimization

- Operate on a region in the CFG that contains multiple blocks
- Loops, trees, paths, extended basic blocks

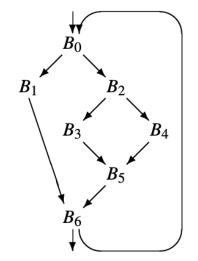
new opportunities

### Whole procedure optimization (intraprocedural)

- Operate on entire CFG for a procedure
- Presence of cyclic paths forces analysis then transformation

### Whole program optimization (interprocedural)

- Operate on some or all of the call graph (multiple procedures)
- Must contend with call/return & parameter binding



## Redundancy Elimination as an Example

An expression x+y is redundant if and only if, along every path from the procedure's entry, it has been evaluated, and its constituent subexpressions (x & y) have not been re-defined.

If the compiler can prove that an expression is redundant

- It can preserve the results of earlier evaluations
- It can replace the current evaluation with a reference

Two pieces to the problem

- Proving that x+y is redundant, or <u>available</u>
- Rewriting the code to eliminate the redundant evaluation

One technique for accomplishing both is called value numbering

## Rewriting to avoid Redundancy

$$a \leftarrow b + c$$

$$b \leftarrow a - d$$

$$c \leftarrow b + c$$

$$d \leftarrow a - d$$

$$a \leftarrow b + c$$

$$b \leftarrow a - d$$

$$c \leftarrow b + c$$

$$d \leftarrow b$$

Rewritten Block

The resulting code runs more quickly but extend the lifetime of b This could cause the allocator to spill the value of b

Since the optimiser cannot predict the behaviour of the register allocator, it assumes that rewriting to avoid redundancy is profitable!

# Redundancy without textual identity

The problem is more complex that it may seem!

$$a \leftarrow b \times c$$

$$d \leftarrow b$$

$$e \leftarrow d \times c$$

## The key notion

- Assign an identifying number, V(e), to each expression
  - V(x+y) = V(j) iff x+y and j always have the same value  $\leftarrow$
  - Use hashing over the value numbers to make it efficient
- Use these numbers to improve the code

## Improving the code

- Replace redundant expressions
  - Same  $V(e) \Rightarrow$  refer rather than recompute

Within a basic block; definition becomes more complex across blocks

## The Algorithm

For each operation  $o = \langle operator, o_1, o_2 \rangle$  in the block, in order

- 1. Get value numbers for operands from hash lookup
- 2. Hash  $\langle operator, VN(o_1), VN(o_2) \rangle$  to get a value number for o
- 3. If o already had a value number, replace o with a reference operator,  $VN(o_1)$ ,  $VN(o_2)$ .

If hashing behaves, the algorithm runs in linear time

## An example

### Original Code

$$a \leftarrow b + c$$

$$b \leftarrow a - d$$

$$c \leftarrow b + c$$

\* 
$$d \leftarrow a - d$$

#### With VNs

$$a^3 \leftarrow b^1 + c^2$$

$$b^5 \leftarrow a^3 - d^4$$

$$c^6 \leftarrow b^5 + c^2$$

\* 
$$d^5 \leftarrow a^3 - d^4$$

#### **Rewritten**

$$a \leftarrow b + c$$

$$b \leftarrow a - d$$

$$c \leftarrow b + c$$

## One redundancy

Eliminate stmt with

# Local Value Numbering: the role of naming

## An example

#### Original Code

$$a \leftarrow x + y$$

\* 
$$b \leftarrow x + y$$

$$* c \leftarrow x + y$$

#### With VNs

$$a^3 \leftarrow x^1 + y^2$$

\* 
$$b^3 \leftarrow x^1 + y^2$$

$$a^4 \leftarrow 17$$

\* 
$$c^3 \leftarrow x^1 + y^2$$

#### **Rewritten**

$$a^3 \leftarrow x^1 + y^2$$

\* 
$$b^3 \leftarrow a^3$$

$$a^4 \leftarrow 17$$

\* 
$$c^3 \leftarrow a^3$$
 (oops!)

#### Two redundancies

Eliminate stmtswith a \*

### **Options**

• Use  $c^3 \leftarrow b^3$ 

with a mapping from values

to names

- Save a<sup>3</sup> in t<sup>3</sup>
- Rename around it

# Local Value Numbering: renaming

## Example (continued):

## Remember the SSA form?

#### **Original Code**

$$a_0 \leftarrow x_0 + y_0$$
  
\*  $b_0 \leftarrow x_0 + y_0$ 

\* 
$$c_0 \leftarrow x_0 + y_0$$

## Renaming:

- Give each value a unique name
- Makes it clear

#### With VNs

$$a_0^3 \leftarrow x_0^1 + y_0^2$$

\* 
$$b_0^3 \leftarrow x_0^1 + y_0^2$$

$$a_1^4 \leftarrow 17$$

$$* c_0^3 \leftarrow x_0^1 + y_0^2$$

#### **Rewritten**

$$a_0^3 \leftarrow x_0^1 + y_0^2$$

\* 
$$b_0^3 \leftarrow a_0^3$$

$$a_1^4 \leftarrow 17$$

\* 
$$c_0^3 \leftarrow a_0^3$$

#### Notation:

 While complex, the meaning is clear

#### Result:

- a<sub>0</sub><sup>3</sup> is available
- Rewriting now works

How to reconcile this new subscripted names with the original ones? A clever implementation would map  $a_1 - a_2 + b_0 - b_1 + c_0 - c_2 + c_0 - c_1 + c_0 - c_0 - c_1 + c_0 - c_0 - c_1 + c_0 - c_0$ 

# The impact of indirect assignments

- To manage the subscripted naming the compiler maintain a map from names to the current subscript.
- With a direct assignment a <- b + c, the changes are clear</li>
- With an indirect assignment \*p <- 0?</li>
- The compiler can perform static analysis to disambiguate pointer references (to restrict the set of variables to whom p can refer to).

Ambiguous reference the compiler cannot isolate a single memory location

# Simple Extensions to Value Numbering

#### Constant folding

- Add a bit that records when a value is constant
- Evaluate constant values at compile-time
- Replace with load immediate or immediate operand
- No stronger local algorithm

#### Commutative operations

• commutative operations that differs only for the order of their operands should receive the same value numbers a x b and b x a

#### Algebraic identities

- Must check (many) special cases
- Replace result with input VN
- Build a decision tree on operation

## (Recap)

## The LVN Algorithm, with bells & whistles

for i ← 0 to n-1

- 1. get the value numbers  $V_1$  and  $V_2$  for  $L_i$  and  $R_i$
- Block is a sequence of n operations of the form  $T_i \leftarrow L_i Op_i R_i$
- 2. if  $L_i$  and  $R_i$  are both constant then Constant folding evaluate Li  $Op_i$   $R_i$ , assign it to  $T_i$  and mark  $T_i$  as a constant
- 3. if Li  $Op_i R_i$  matches an identity then Algebraic identities replace it with a copy operation or an assignment
- 4. if  $Op_i$  commutes and  $V_1 > V_2$  then swap  $V_1$  and  $V_2$
- 5. construct a hash key  $\langle V_1, Op_i, V_2 \rangle$
- if the hash key is already present in the table then replace operation I with a copy into T<sub>i</sub> and mark T<sub>i</sub> with the VN else

insert a new VN into table for hash key & mark T<sub>i</sub> with the VN

## The Algorithm

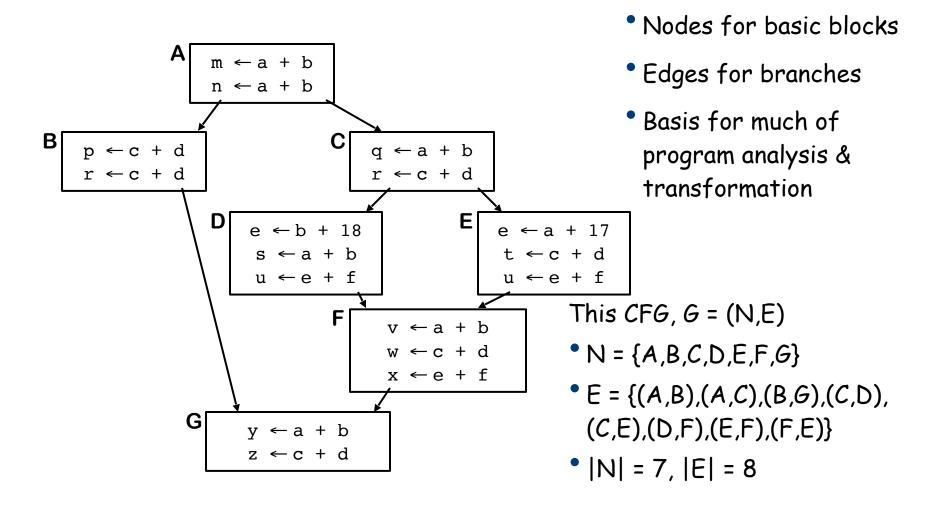
For each operation  $o = \langle operator, o_1, o_2 \rangle$  in the block, in order

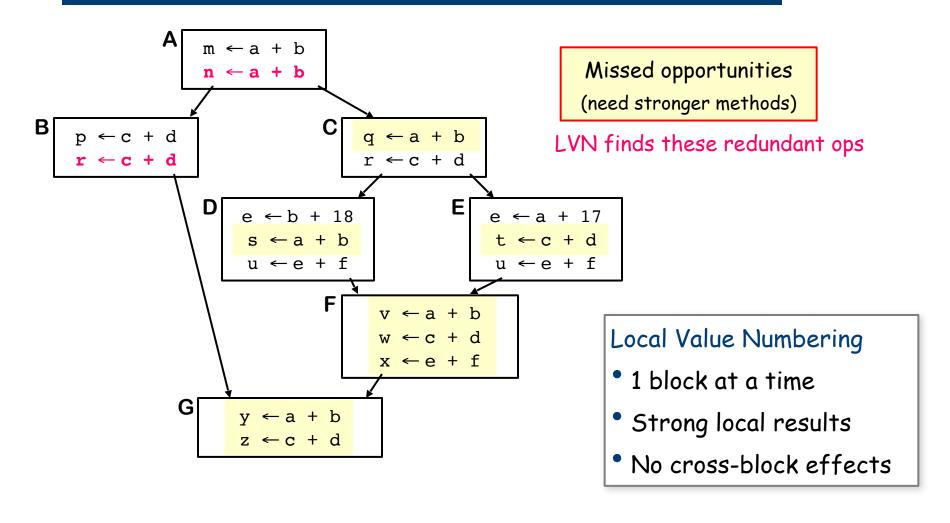
- 1 Get value numbers for operands from hash lookup
- 2 Hash  $\langle operator, VN(o_1), VN(o_2) \rangle$  to get a value number for o
- 3 If a already had a value number, replace a with a reference

## Complexity & Speed Issues

- "Get value numbers" linear search versus hash
- "Hash  $\langle op, VN(o_1), VN(o_2) \rangle$ " linear search versus hash
- Copy folding set value number of result
- Commutative ops double hash versus sorting the operands

# Terminology Control-flow graph (CGF)

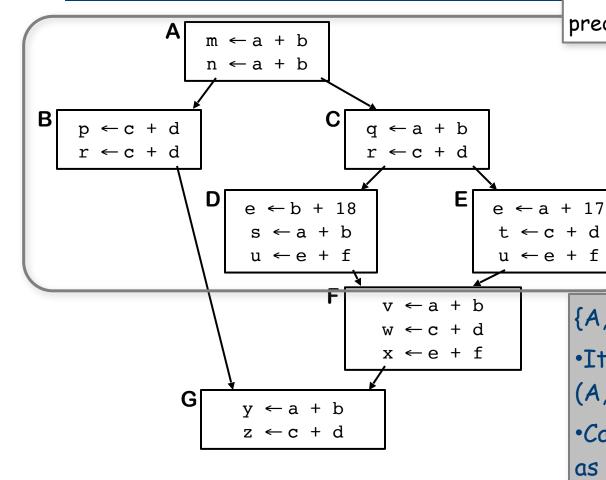




### A Regional Technique

## Superlocal Value Numbering

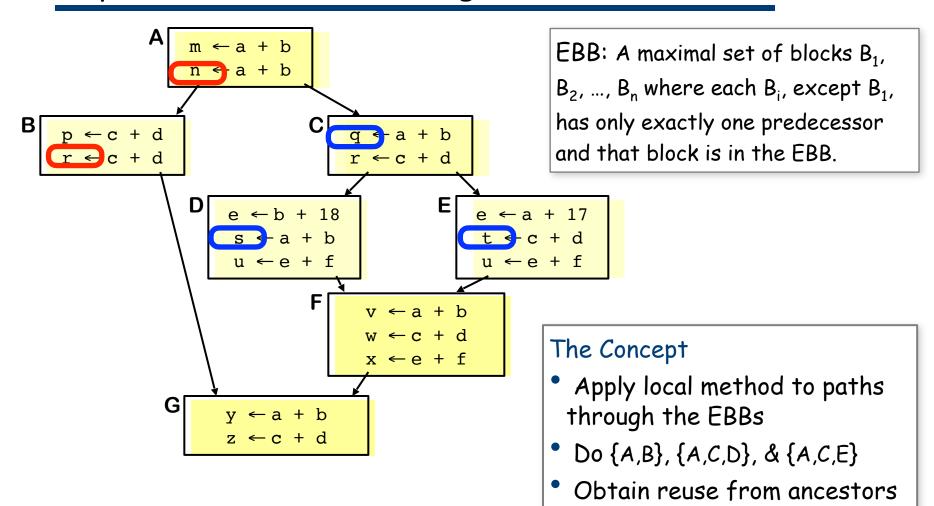
Extended Basic Block: maximal set of blocks  $B_1$ ,  $B_2$ , ...,  $B_n$  where each  $B_i$ , except  $B_1$ , has exactly one predecessor in the EBB itself.



 $\{A,B,C,D,E\}$  is an EBB

- •It has 3 paths: (A,B), (A,C,D), & (A,C,E)
- •Can sometimes treat each path as if it were a block

 $\{F\}$  &  $\{G\}$  are degenerate EBBs



Avoid re-analyzing A & C

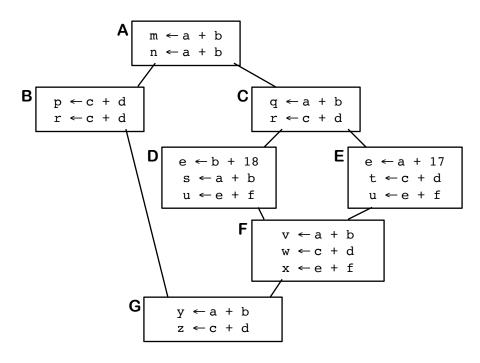
Does not help with F or G

## Efficiency

- Use A's table to initialize tables for B & C
- To avoid duplication, use a scoped hash table
  - A, AB, A, AC, ACD, AC, ACE, F, G

"kill" is a re-definition of some name

- Need a VN→name mapping to handle kills
  - Must restore map with scope
  - Adds complication, not cost

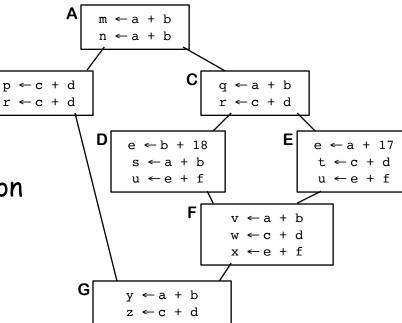


## Efficiency

- Use A's table to initialize tables for B & C
- To avoid duplication, use a scoped hash table
  - A, AB, A, AC, ACD, AC, ACE, F, G
- Need a VN→name mapping to handle kills
  - Must restore map with scope
  - Adds complication, not cost

## To simplify THE PROBLEM

- Need unique name for each definition
- Makes name ⇔ VN
- Use the SSA name space



"kill" is a re-definition

of some name

(locally)

## Example (from earlier):

#### **Original Code**

$$a_0 \leftarrow x_0 + y_0$$

\* 
$$b_0 \leftarrow x_0 + y_0$$
  
 $a_1 \leftarrow 17$ 

\* 
$$c_0 \leftarrow x_0 + y_0$$

#### With VNs

$$a_0^3 \leftarrow x_0^1 + y_0^2$$

\* 
$$b_0^3 \leftarrow x_0^1 + y_0^2$$
  
 $a_1^4 \leftarrow 17$ 

\* 
$$c_0^3 \leftarrow x_0^1 + y_0^2$$

#### Rewritten

$$a_0^3 \leftarrow x_0^1 + y_0^2$$

\* 
$$b_0^3 \leftarrow a_0^3$$

$$a_1^4 \leftarrow 17$$

\* 
$$c_0^3 \leftarrow a_0^3$$

### Renaming:

- Give each value a unique name
- Makes it clear

#### Notation:

 While complex, the meaning is clear

#### Result:

- $a_0^3$  is available
- Rewriting just works

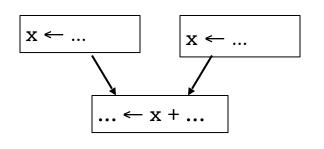
(in general)

## Two principles

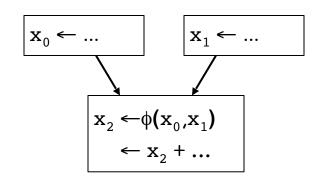
- Each name is defined by exactly one operation
- Each operand refers to exactly one definition

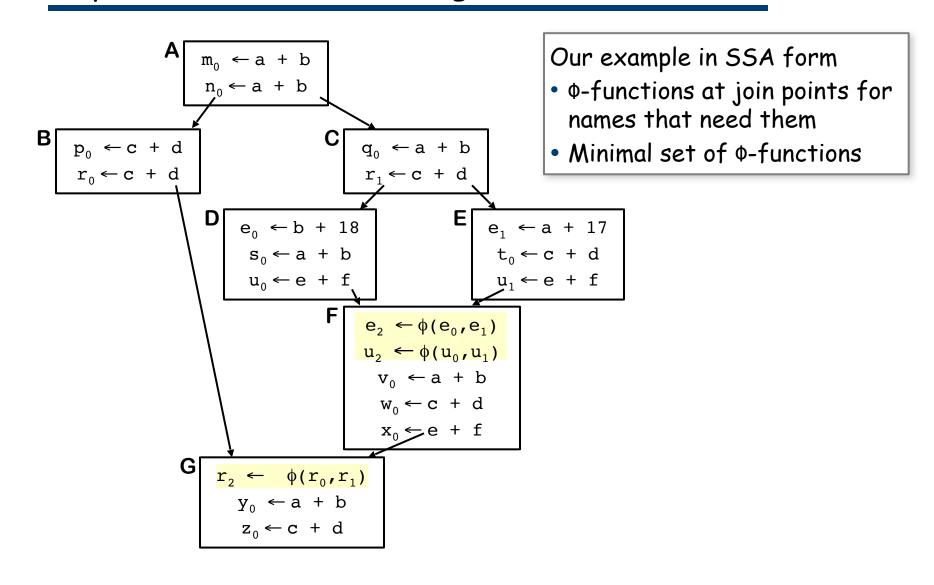
To reconcile these principles with real code

- Insert φ-functions at merge points to reconcile name space
- Add subscripts to variable names for uniqueness



becomes



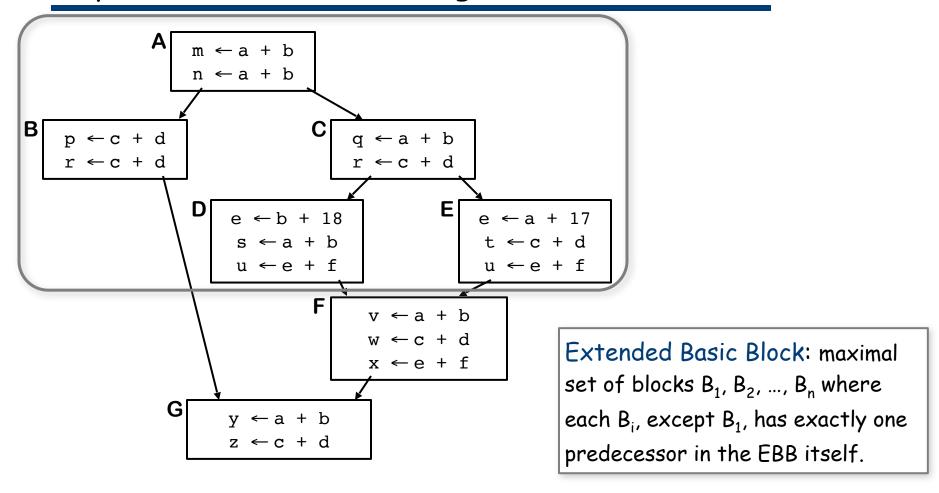


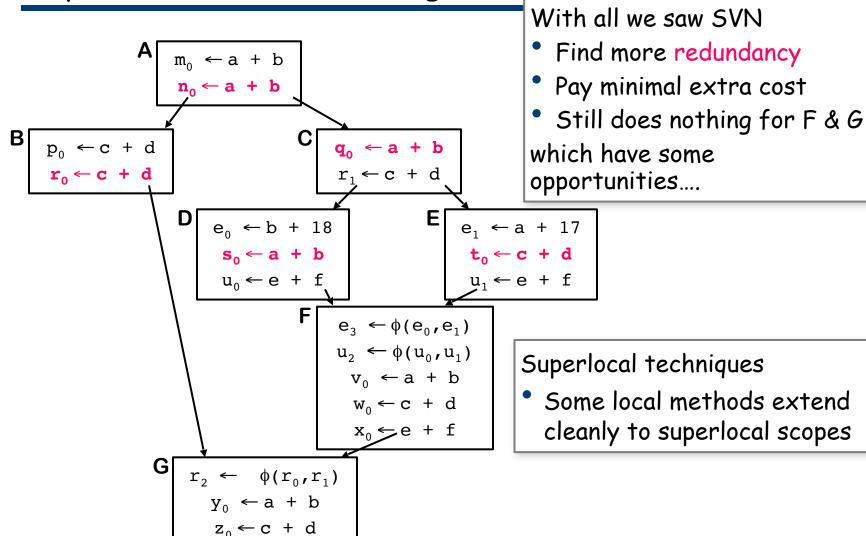
## The SVN Algorithm

```
WorkList ← { entry block }
                                                               Blocks to process
Empty ← new table
                                                             Table for base case
while (WorkList is not empty)
    remove a block b from WorkList
    SVN(b, Empty)
                                        Assumes LVN has been parameterized
                                        around block and table
SVN(Block, Table)
    t ← new table for Block, with Table linked as surrounding scope
                                                            Use LVN for the work
    LVN(Block, t)
    for each successor s of Block
                                                                In the same FBB
      if s has just 1 predecessor
         then SVN(s, t)
                                                               Starts a new EBB
       else if s has not been processed
         then add s to WorkList
    deallocate t
```

### A Regional Technique

# Superlocal Value Numbering





## Loop Unrolling

### Applications spend a lot of time in loops

We can reduce loop overhead by unrolling the loop

```
do i = 1 to 100 by 1

a(i) \leftarrow b(i) * c(i)

end
a(1) \leftarrow b(1) * c(1)
a(2) \leftarrow b(2) * c(2)
a(3) \leftarrow b(3) * c(3)
...
a(100) \leftarrow b(100) * c(100)
```

- Eliminated additions, tests and branches: reduce the number of operations Can subject resulting code to strong local optimization!
- Only works with fixed loop bounds & few iterations
- The principle, however, is sound
- Unrolling is always safe, as long as we get the bounds right

# Loop Unrolling

### Unrolling by smaller factors can achieve much of the benefit

Example: unroll by 4 (8, 16, 32? depends on # of registers)

do i = 1 to 100 by 1  

$$a(i) \leftarrow b(i) * c(i)$$
  
end  
Unroll by 4  
do i = 1 to 100 by 4  
 $a(i) \leftarrow b(i) * c(i)$   
 $a(i+1) \leftarrow b(i+1) * c(i+1)$   
 $a(i+2) \leftarrow b(i+2) * c(i+2)$   
 $a(i+3) \leftarrow b(i+3) * c(i+3)$   
end

Achieves much of the savings with lower code growth

- Reduces tests & branches by 25%
- LVN will eliminate duplicate adds and redundant expressions
- Less overhead per useful operation

But, it relied on knowledge of the loop bounds...

# Loop Unrolling

## Unrolling with unknown bounds

Need to generate guard loops

do 
$$i = 1$$
 to n by 1  
 $a(i) \leftarrow b(i) * c(i)$   
end



Achieves most of the savings

- Reduces tests & branches by 25%
- LVN still works on loop body
- Guard loop takes some space

```
i ← 1
do while (i+3 < n)
    a(i) \leftarrow b(i) * c(i)
    a(i+1) \leftarrow b(i+1) * c(i+1)
    a(i+2) \leftarrow b(i+2) * c(i+2)
    a(i+3) \leftarrow b(i+3) * c(i+3)
   i ←i + 4
    end
do while (i < n)
    a(i) \leftarrow b(i) * c(i)
   i \leftarrow i + 1
    end
```

Can generalize to arbitrary upper & lower bounds, unroll factors

$$i=1,...100 : a(i)=a(i)+b(i)+b(i-1)$$

### One other unrolling trick

Eliminate copies at the end of a loop

```
t1 ← b(0)

do i = 1 to 100 by 1

t2 \leftarrow b(i)

a(i) \leftarrow a(i) + t1 + t2

t1 ← b(0)

do i = 1 to 100 by 2

t2 \leftarrow b(i)

a(i) \leftarrow a(i) + t1 + t2

t1 ← b(i+1)

a(i+1) \leftarrow a(i+1) + t2 + t1

end

Unroll
```

- Eliminates the copies, which were a naming artifact
- Achieves some of the benefits of unrolling
  - Lower overhead, longer blocks for local optimization
- Situation occurs in more cases than you might suspect

## Sources of Degradation

- It increases the size of the code
- The unrolled loop may have more demand for registers
- If the demand for registers forces additional register spills (store and reloads) then the resulting memory traffic may overwhelm the potential benefits of unrolling