

# Lexical Analysis

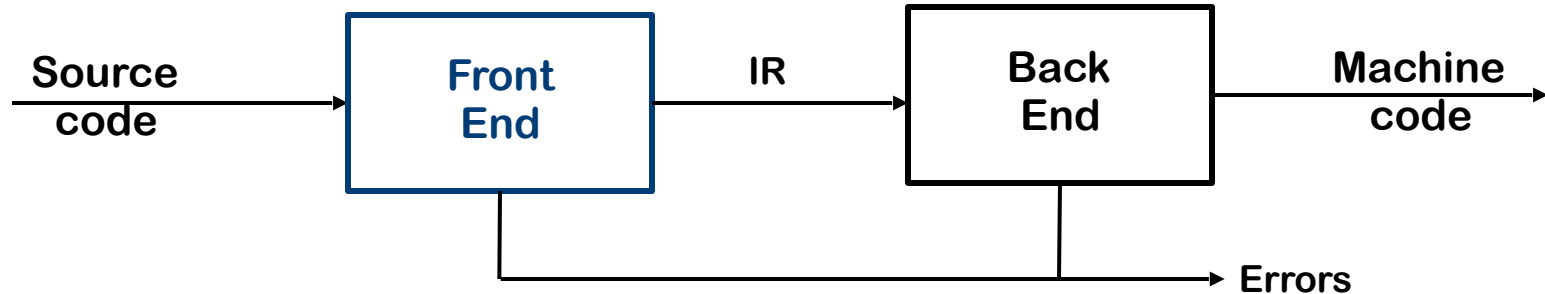
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# The Front End

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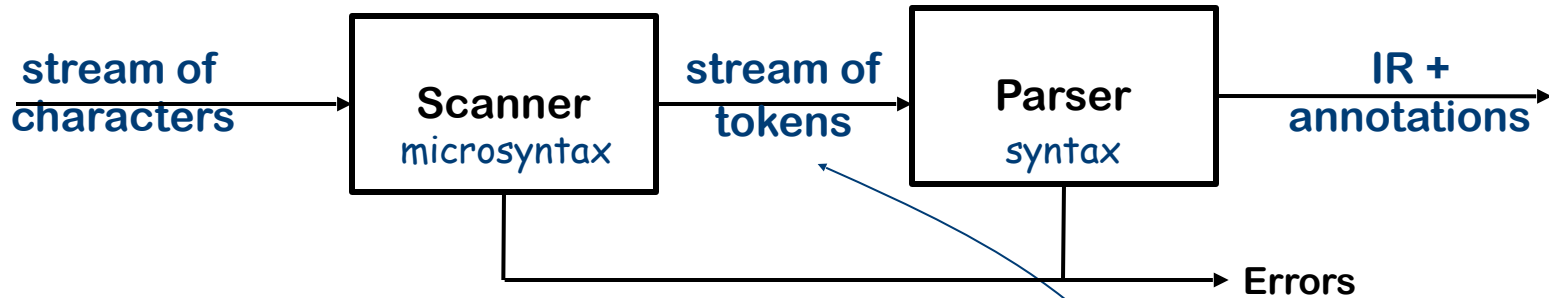
The purpose of the front end is to deal with the input language

- Perform a membership test:  $\text{code} \in \text{source language?}$
- Is the program well-formed (semantically) ?
- Build an IR version of the code for the rest of the compiler

The front end deals with form (syntax) & meaning (semantics)

# The Front End

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Scanner is only pass that touches every character of the input.

## Why separate the scanner and the parser?

- Scanner classifies words
- Parser constructs grammatical derivations
- Parsing is harder and slower

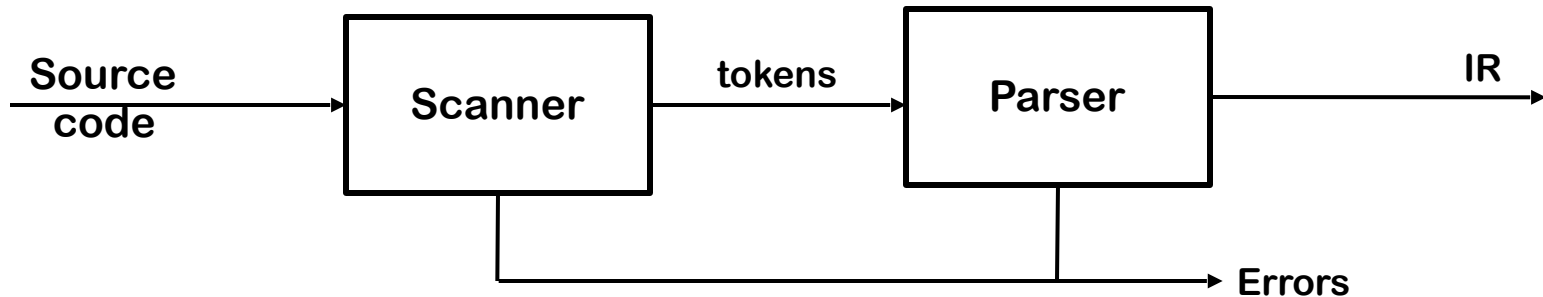
## Separation simplifies the implementation

- Scanners are simple
- Scanner leads to a faster, smaller parser

token is a pair  
<part of speech, lexeme >

# Our setting: the Front End

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## Implementation Strategy

	Scanning	Parsing
Specify Syntax	regular expressions	context-free grammars
Implement Recognizer	deterministic finite automaton	push-down automaton
Perform Work	Actions on transitions in automaton	

# Lexical Analysis

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Relates to the words of the vocabulary of a language, (as opposed to grammar, i.e., correct construction of sentences).

**Lexical Analyzer**, a.k.a. **lexer**, **scanner** or **tokenizer**, splits the input program, seen as a stream of characters, into a sequence of tokens.

**Tokens** are the words of the (programming) language, e.g., keywords, numbers, comments, parenthesis, semicolon.

Tokens are classes of concrete input (called **lexeme**).

# Example

## Token created

int	Keyword
maximum	Identifier
(	Operator
int	Keyword
x	Identifier
,	Operator
int	Keyword
y	Identifier
(	Operator
{	Operator
if	Keyword

```
#include <stdio.h>
int maximum(int x, int y) {
    // This will compare 2 numbers
    if (x > y)
        return x;
    else {
        return y;
    }
}
```

## Non-Token

Comment	// This will compare 2 numbers
Pre-processor directive	#include <stdio.h>
Pre-processor directive	#define NUMS 8,9
Macro	NUMS

# Lexical analysis

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- Lexical analysis is the very **first phase** in the compiler designing, the only one that analyses the entire code
- A **lexeme** is a sequence of characters that are included in the source program according to the matching pattern of a **token**
- Lexical analyzer helps to **identify token** into the symbol table
- A character sequence which is not possible to scan into any valid token is a **lexical error**

# Constructing a Lexical Analyser

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- By hand - Identify lexemes in input and return tokens
- Automatically - **Lexical-Analyser generator**: it compiles the patterns that specify the lexemes into a code (the lexical analyser).

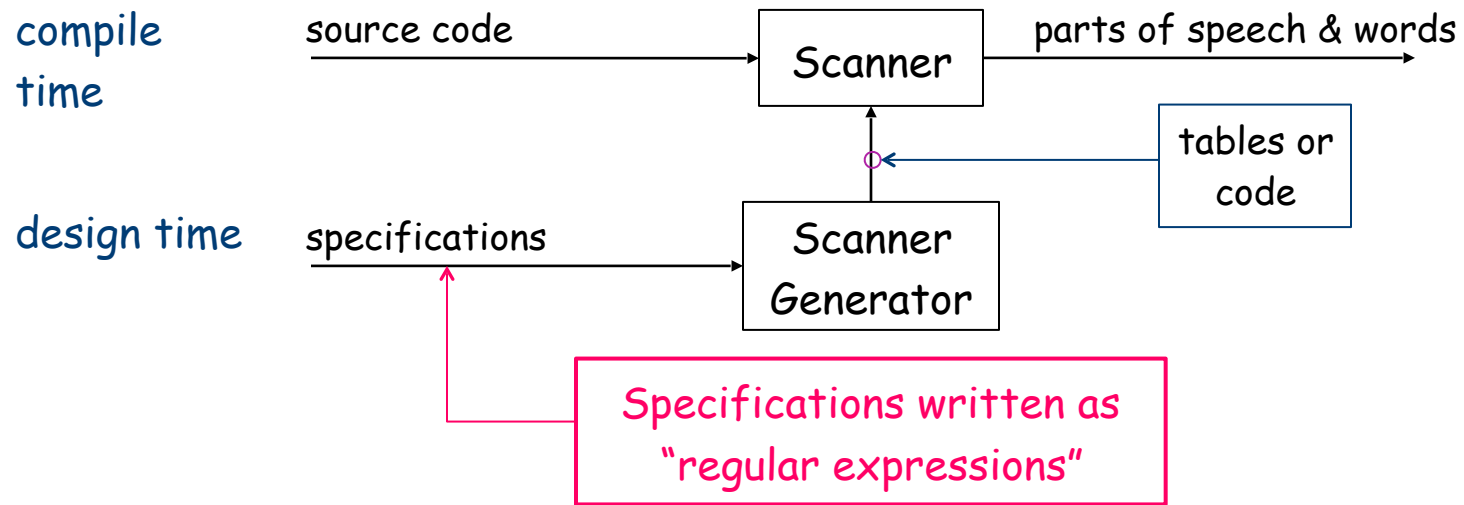
Lexical analysis decides whether the individual tokens are well formed, this can be expressed by a **regular** language.



# Automatic Scanner Construction

Why study automatic scanner construction?

- Avoid writing scanners by hand



In practice, many scanners are hand coded. Even if you build a hand-coded scanner, it is useful to write down the specification and the automaton.

## The syntax can be expressed by a regular grammar

The **syntax** of a programming language can be expressed by a **regular grammar**

Example

The following grammar generates all the legal identifier

$$S \rightarrow aT \mid \dots \mid zT \mid AT \mid \dots \mid ZT$$
$$T \rightarrow \varepsilon \mid 0T \mid \dots \mid 9T \mid S$$

that can be more neatly be expressed using a **regular expression!**

$$(a \mid \dots \mid z \mid A \mid \dots \mid Z) (a \mid \dots \mid z \mid A \mid \dots \mid Z \mid 0 \mid \dots \mid 9)^*$$

# Examples of Regular Expressions

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## Identifiers:

Letter  $\rightarrow$  (a|b|c | ... | z|A|B|C | ... | Z)

Digit  $\rightarrow$  (0|1|2 | ... | 9)

Identifier  $\rightarrow$  Letter ( Letter | Digit )\*

$(\underline{a}|\underline{b}|\underline{c} | \dots | \underline{z}|\underline{A}|\underline{B}|\underline{C} | \dots | \underline{Z}) (\underline{a}|\underline{b}|\underline{c} | \dots | \underline{z}|\underline{A}|\underline{B}|\underline{C} | \dots | \underline{Z}) | (\underline{0}|\underline{1}|\underline{2} | \dots | \underline{9})^*$

shorthand  
for

## Numbers:

Integer  $\rightarrow$  (+|-|ε) (0| (1|2|3 | ... | 9)(Digit \*) )

Decimal  $\rightarrow$  Integer . Digit \*

Real  $\rightarrow$  ( Integer | Decimal ) E (+|-|ε) Digit \*

Complex  $\rightarrow$  ( Real . Real )

Numbers can get much more complicated!

underlining indicates a letter in the input stream

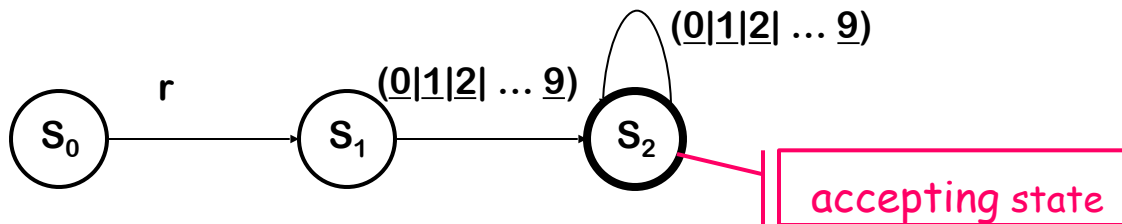
# Example

Consider the problem of recognizing ILOC register names

Register  $\rightarrow r (0|1|2| \dots | 9) (0|1|2| \dots | 9)^*$

- Allows registers of arbitrary number
- Requires at least one digit

RE corresponds to a recognizer (or DFA)



Recognizer for Register

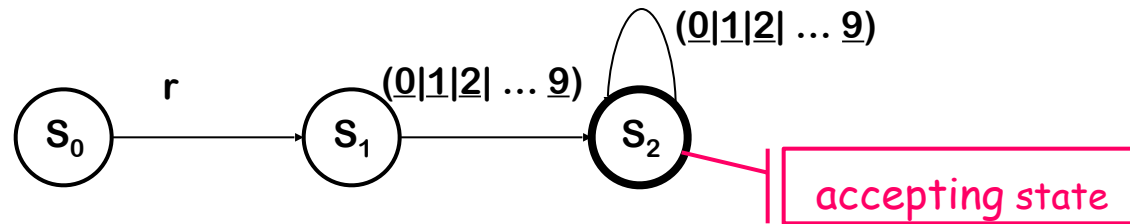
Transitions on other inputs go to an error state,  $s_e$

# Example

(continued)

DFA operation

- Start in state  $S_0$  & make transitions on each input character

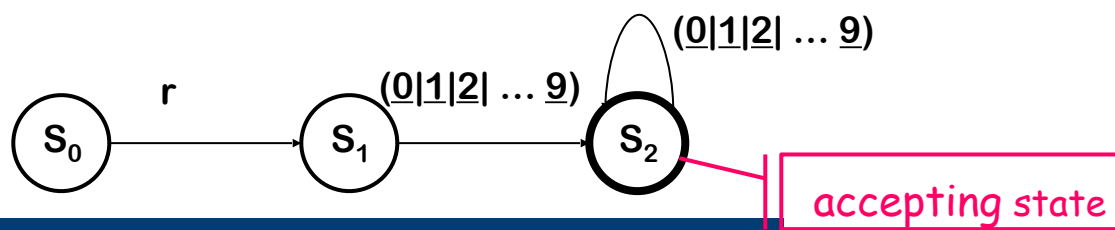


So,

Recognizer for Register

- r17 takes it through  $s_0, s_1, s_2$  and accepts
- r takes it through  $s_0, s_1$  and fails
- a takes it straight to  $s_e$

# Example



To be useful, the recognizer must be converted into code

```
Char ← next character
State ← s0

while (Char ≠ EOF)
    State ← δ(State,Char)
    Char ← next character

if (State is a final state)
    then report success
else report failure
```

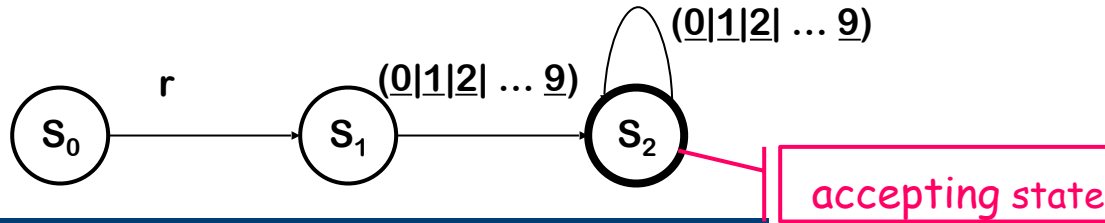
Skeleton recognizer

$\delta$	r	0,1,2,3,4, 5,6,7,8,9	All others
s <sub>0</sub>	s <sub>1</sub>	s <sub>e</sub>	s <sub>e</sub>
s <sub>1</sub>	s <sub>e</sub>	s <sub>2</sub>	s <sub>e</sub>
s <sub>2</sub>	s <sub>e</sub>	s <sub>2</sub>	s <sub>e</sub>
s <sub>e</sub>	s <sub>e</sub>	s <sub>e</sub>	s <sub>e</sub>

Table encoding the RE

O(1) cost per character (or per transition)

# Example



We can add "actions" to each transition

```

Char ← next character
State ← s0

while (Char ≠ EOF)
    Next ← δ(State,Char)
    Act ← α(State,Char)
    perform action Act
    State ← Next
    Char ← next character

if (State is a final state)
    then report success
    else report failure
    
```

Skeleton recognizer

$\delta$	$\alpha$	0,1,2,3,4, 5,6,7,8,9	All others
s <sub>0</sub>	s <sub>1</sub> start	s <sub>e</sub> error	s <sub>e</sub> error
s <sub>1</sub>	s <sub>e</sub> error	s <sub>2</sub> add	s <sub>e</sub> error
s <sub>2</sub>	s <sub>e</sub> error	s <sub>2</sub> add	s <sub>e</sub> error
s <sub>e</sub>	s <sub>e</sub> error	s <sub>e</sub> error	s <sub>e</sub> error

Table encoding RE

Typical action is to capture the lexeme

# What if we need a tighter specification?

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$\underline{r}$  Digit Digit\* allows arbitrary numbers

- Accepts r00000
- Accepts r99999
- What if we want to limit it to r0 through r31 ?

Write a tighter regular expression

- Register  $\rightarrow \underline{r} ( (\underline{0}|\underline{1}|\underline{2}) (\text{Digit} | \epsilon) | (\underline{4}|\underline{5}|\underline{6}|\underline{7}|\underline{8}|\underline{9}) | (\underline{3}|\underline{30}|\underline{31}) )$
- Register  $\rightarrow \underline{r0}|\underline{r1}|\underline{r2} | \dots | \underline{r31}|\underline{r00}|\underline{r01}|\underline{r02} | \dots | \underline{r09}$

Produces a more complex DFA

- DFA has more states
- DFA has same cost per transition
- DFA has same basic implementation

More states implies a larger table. The larger table might have mattered when computers had 128 KB or 640 KB of RAM. Today, when a cell phone has megabytes and a laptop has gigabytes, the concern seems outdated.

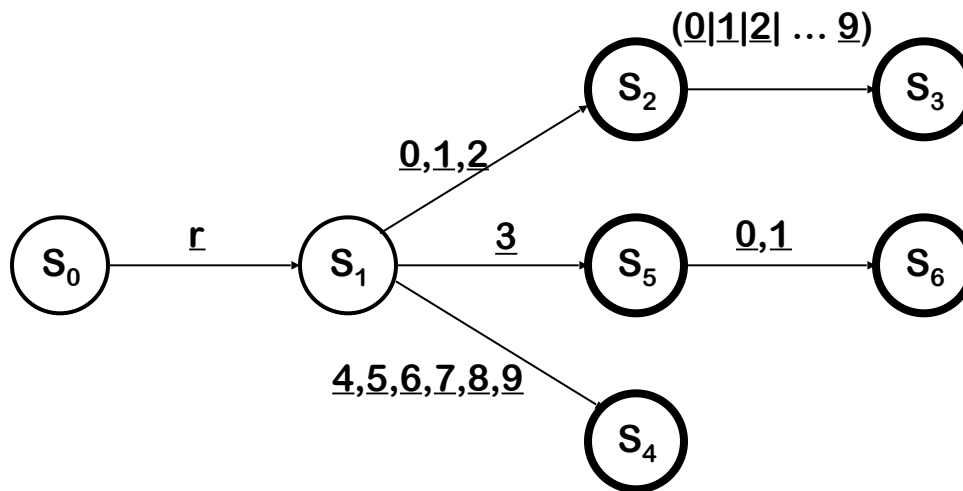


# Tighter register specification

(continued)

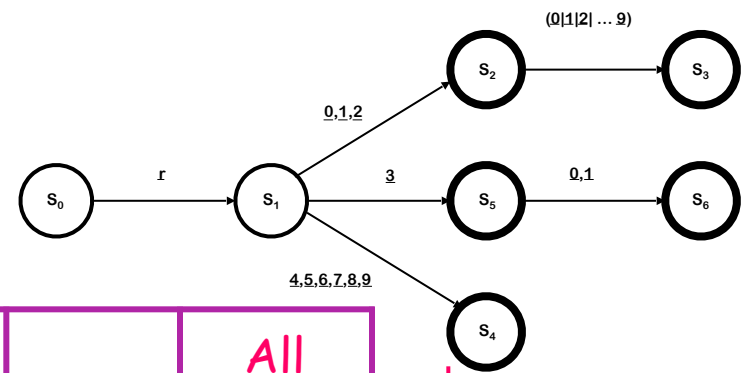
The DFA for

Register  $\rightarrow$  r ( (0|1|2) (Digit |  $\epsilon$ ) | (4|5|6|7|8|9) | (3|30|31) )



- Accepts a more constrained set of register names
- Same set of actions, more states

# Tighter register specification

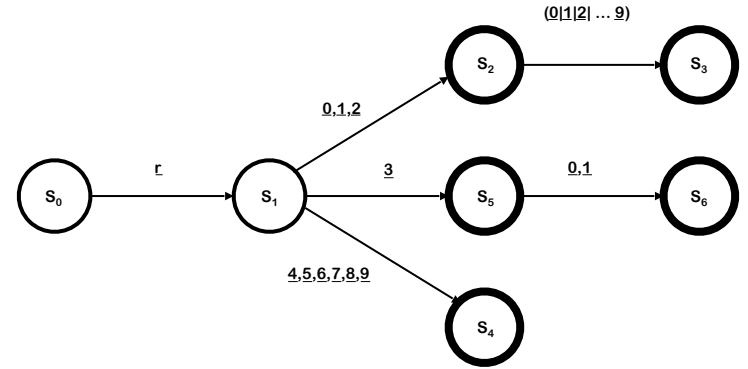


$\delta$	$r$	0,1	2	3	4-9	All others
$s_0$	$s_1$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$
$s_1$	$s_e$	$s_2$	$s_2$	$s_5$	$s_4$	$s_e$
$s_2$	$s_e$	$s_3$	$s_3$	$s_3$	$s_3$	$s_e$
$s_3$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$
$s_4$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$
$s_5$	$s_e$	$s_6$	$s_e$	$s_e$	$s_e$	$s_e$
$s_6$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$
$s_e$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$	$s_e$

This table runs in the same skeleton recognizer

Table encoding RE for the tighter register specification

# Tighter register specification



State Action	r	0,1	2	3	4,5,6 7,8,9	other
0	1 start	e	e	e	e	e
1	e	2 add	2 add	5 add	4 add	e
2	e	3 add	3 add	3 add	3 add	e exit
3,4,6	e	e	e	e	e	e exit
5	e	6 add	e	e	e	e exit
e	e	e	e	e	e	e

# Automating Scanner Construction

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To convert a specification into code:

- 1 Write down the RE for the input language
- 1 Build a  $\epsilon$ -NFA collecting all the NFA for the RE
- 2 Build a NFA corresponding to the  $\epsilon$ -NFA
- 3 Build the DFA that simulates the NFA
- 4 Systematically minimise the DFA
- 5 Turn it into code

Scanner generators

- Lex and Flex work along these lines
- Algorithms are well-known and well-understood
- Key issue is interface to parser
- You could build one in a weekend!

The overall construction: RE  $\rightarrow$   $\epsilon$ -NFA  $\rightarrow$  NFA  $\rightarrow$  DFA  $\rightarrow$  minimized DFA

---

How we transform a DFA into code? 3 different approaches

- Table driven scanners
- Direct code scanners
- Hand-coded scanners

all will simulate the DFA!

## The actions in common

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- They repeatedly read the next character in the input and simulate the corresponding DFA transition
- This process stops when the DFA recognises a word: there are not outgoing transition from the state  $s$  with the input character
- If  $s$  is an accepting state the scanner recognises the word and its syntactic category
- If  $s$  is a nonaccepting state the scanner must determine whether or not it passes a final state at some point, if yes the scanner should **roll back** its internal state and its input stream and report success

# The differences

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- Table driven scanners
- Direct code scanners
- Hand-coded scanners

All constant cost per character (with different constants) +  
the cost of rollback

Differs from the way they implement the transition table  
and simulate the operations of the DFA

# Table-Driven Scanners

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- Table(s) + Skeleton Scanner

- So far, we have used a simplified skeleton

- state  $\leftarrow s_0$ ;

- while (state  $\neq s_{\text{error}}$ ) do

- char  $\leftarrow \text{NextChar}()$  // read next character

- state  $\leftarrow \delta(\text{state}, \text{char})$ ; // take the transition

- In practice, the skeleton is more complex

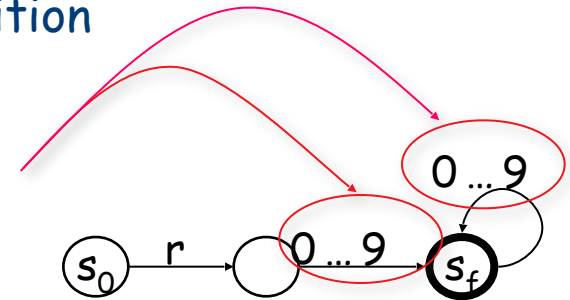
- Character classification for table compression

- Building the lexeme

- Recognizing subexpressions

- Practice is to combine all the REs into one DFA

- Must recognize individual words without hitting EOF





# Table-Driven Scanners

## Character Classification

- Group together characters by their actions in the DFA
  - Combine identical columns in the transition table,  $\delta$
  - Indexing  $\delta$  by class shrinks the table

$state \leftarrow s_0;$

while ( $state \neq s_{error}$ ) do

$char \leftarrow NextChar( )$                    // read next character

$cat \leftarrow CharCat(char)$                // classify character

$state \leftarrow \delta(state, cat)$          // take the transition

r	0, 1, 2, ..., 9	EOF	Other
Register	Digit	Other	Other

The Classifier Table, *CharCat*

	Register	Digit	Other
$s_0$	$s_1$	$s_e$	$s_e$
$s_1$	$s_e$	$s_2$	$s_e$
$s_2$	$s_e$	$s_2$	$s_e$
$s_e$	$s_e$	$s_e$	$s_e$

The Transition Table,  $\delta$

# Table-Driven Scanners

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## Building the Lexeme

- Scanner produces syntactic category (part of speech)
    - Most applications want the lexeme (word), too
- ```
state ← s0
lexeme ← empty string
while (state ≠ serror) do
    char ← NextChar( )           // read next character
    lexeme ← lexeme + char       // concatenate onto lexeme
    cat ← CharCat(char)         // classify character
    state ← δ(state,cat)        // take the transition
```
- This problem is trivial
    - Save the characters

# Table-Driven Scanners

---

## Choosing a Category from an Ambiguous RE

- We want one DFA, so we combine all the REs into one
  - Some strings may fit RE for more than 1 syntactic category
    - Keywords versus general identifiers
    - Would like to encode them into the RE & recognize them
  - Scanner must choose a category for ambiguous final states
    - Classic answer: specify priority by order of REs (return 1<sup>st</sup>)

### Identifiers:

Letter → (a|b|c| ... |z|A|B|C| ... |Z)

Digit → (0|1|2| ... |9)

Identifier → Letter ( Letter | Digit )\*

### Keywords:

key → if | ...                      ife

# A table driven scanner for register names

initialization

```
NextWord()
  state ← s0;
  lexeme ← “ ”;
  clear stack;
  push(bad);
```

scanning loop

```
while (state ≠ se) do
  NextChar(char);
  lexeme ← lexeme + char;
  if state ∈ SA final states
    then clear stack;
  push(state);
  cat ← CharCat[char];
  state ← δ[state, cat];
end;
```

roll-back

```
while (state ∉ SA and
      state ≠ bad) do
  state ← pop();
  truncate lexeme;
  RollBack();
end;
```

final-section

```
if state ∈ SA
  then return Type[state];
else return invalid;
```

| r        | 0, 1, 2, ..., 9 | EOF   | Other |
|----------|-----------------|-------|-------|
| Register | Digit           | Other | Other |

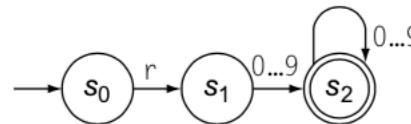
The Classifier Table, *CharCat*

|                | Register       | Digit          | Other          |
|----------------|----------------|----------------|----------------|
| s <sub>0</sub> | s <sub>1</sub> | s <sub>e</sub> | s <sub>e</sub> |
| s <sub>1</sub> | s <sub>e</sub> | s <sub>2</sub> | s <sub>e</sub> |
| s <sub>2</sub> | s <sub>e</sub> | s <sub>2</sub> | s <sub>e</sub> |
| s <sub>e</sub> | s <sub>e</sub> | s <sub>e</sub> | s <sub>e</sub> |

The Transition Table,  $\delta$

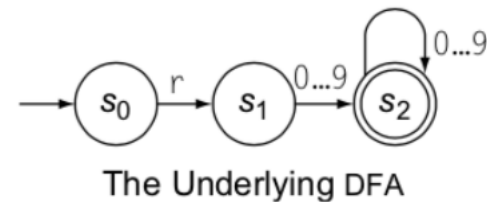
| s <sub>0</sub> | s <sub>1</sub> | s <sub>2</sub> | s <sub>e</sub> |
|----------------|----------------|----------------|----------------|
| invalid        | invalid        | register       | invalid        |

The Token Type Table, *Type*



The Underlying DFA

# Direct-Coded scanners



For each character, the table driven scanner performs two table lookups, one in `CharCat` and the other in  $\delta$

```
sinit : lexeme ← “ ”;  
       clear stack;  
       push(bad);  
       goto s0;  
  
s0 : NextChar(char);  
     lexeme ← lexeme + char;  
     if state ∈ SA  
       then clear stack;  
     push(state);  
     if (char='r')  
       then goto s1;  
       else goto sout;  
  
s1 : NextChar(char);  
     lexeme ← lexeme + char;  
     if state ∈ SA  
       then clear stack;  
     push(state);  
     if ('0' ≤ char ≤ '9')  
       then goto s2;  
       else goto sout;
```

```
s2 : NextChar(char);  
     lexeme ← lexeme + char;  
     if state ∈ SA  
       then clear stack;  
     push(state);  
     if '0' ≤ char ≤ '9'  
       then goto s2;  
       else goto sout  
  
sout : while (state ∉ SA and  
            state ≠ bad) do  
        state ← pop();  
        truncate lexeme;  
        RollBack();  
      end;
```

If end of state test is complex (e.g., many cases), scanner generator should consider other schemes

- Table lookup (with classification?)
- Binary search

# Building Scanners

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## The point

- All this technology lets us automate scanner construction
- Implementer writes down the regular expressions
- Scanner generator builds NFA, DFA, minimal DFA, and then writes out the (table-driven or direct-coded) code
- This reliably produces fast, robust scanners

## For most modern language features, this works

- You should think twice before introducing a feature that defeats a DFA-based scanner
- The ones we've seen (e.g., insignificant blanks, non-reserved keywords) have not proven particularly useful or long lasting

Of course, not everything fits into a regular language ...

# What About Hand-Coded Scanners?

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Many (most?) modern compilers use hand-coded scanners

- Starting from a DFA simplifies design & understanding
- Avoiding straight-jacket of a tool allows flexibility
  - Computing the value of an integer
    - In LEX or FLEX, many folks use `sscanf()`
    - Can use old assembly trick and compute value as it appears
  - Combine similar states
- Scanners are fun to write
  - Compact, comprehensible, easy to debug