## Computing an Array Address of an array A[low:high]

A[i]

- @A+(i-low) x sizeof(A[i])
- In general: base(A) + (i low) x sizeof(A[i])

Color Code: Invariant Varying

Depending on how A is declared, @A may be
•an offset from the ARP,
•an offset from some global label, or
•an arbitrary address.
The first two are compile time constants.

Computing an Array Address A[low:high]

where w = sizeof(A[i]) A[i] • @A + ( i - low ) × w In general: base(A) + (i - low) x w Almost always a power of 2, known at compile-time  $\rightarrow$  use a shift for speed

If the compiler knows low it can fold the subtraction into @A

$$A_0 = @A - (low * w)$$

The false zero of A

A[2..7] 
$$A_0 = @A - (low * w)$$

## computing A[i] with A

loadI	@A	$\Rightarrow r_{@A}$
subI	$r_i, 2$	$\Rightarrow r_1$
lshiftI	$r_1, 2$	$\Rightarrow r_2$
loadA0	$r_{@A}, r_2$	$\Rightarrow r_v$

## computing A[i] with AO

loadI	$@A_0$	$\Rightarrow r_{@A_0}$
lshiftI	$r_i, 2$	$\Rightarrow r_1$
loadA0	$r_{@A_0}, r_1$	$\Rightarrow r_v$

How does the compiler handle A[i,j]?

#### First, must agree on a storage scheme

Row-major order

Lay out as a sequence of consecutive rows Rightmost subscript varies fastest A[1,1], A[1,2], A[1,3], A[2,1], A[2,2], A[2,3]

Column-major order

Lay out as a sequence of columns Leftmost subscript varies fastest A[1,1], A[2,1], A[1,2], A[2,2], A[1,3], A[2,3]

Indirection vectors

Vector of pointers to pointers to ... to values

Takes much more space, trades indirection for arithmetic

Not amenable to analysis

(most languages)

(Fortran)

(Java)

## Laying Out Arrays

### The Concept

These can have distinct & different cache behavior

Row-major order

A	1,1	1,2	1,3	1,4	2,1	2,2	2,3	2,4
---	-----	-----	-----	-----	-----	-----	-----	-----

Column-major order

Α	1,1	2,1	1,2	2,2	1,3	2,3	1,4	2,4
---	-----	-----	-----	-----	-----	-----	-----	-----

Indirection vectors A 2,1 2,2 2,3 2,4

## Computing an Array Address

A[i]

where w = sizeof(A[1,1])

- @A + ( i low ) × w
- In general: base(A) + (i low) x w

What about  $A[i_1, i_2]$ ?

This stuff looks expensive! Lots of implicit +, -, x ops

1,2

2,2

1,3

2,3

hight<sub>2</sub>

1,4

2,4

 $low_1 low_2$ 

hight<sub>1</sub>

Row-major order, two dimensions

 $(a_1 - b_1) \times (b_2 - b_2 + 1) + b_2 - b_2 \times w$ A[2,3]  $(a_1 - b_2) \times 4 + (3-1)$ 

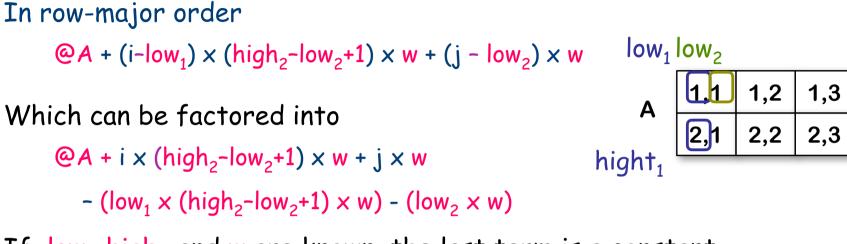
Column-major order, two dimensions

 $@A + ((i_2 - low_2) \times (high_1 - low_1 + 1) + i_1 - low_1) \times w$ 

Indirection vectors, two dimensions

\*(A[i<sub>1</sub>])[i<sub>2</sub>] — where A[i<sub>1</sub>] is, itself, a 1-d array reference e.g., @A + (  $i_1$  - low ) × w

## Optimizing Address Calculation for A[i,j]

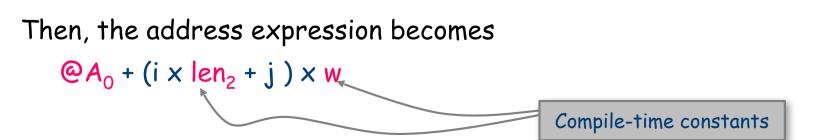


If low<sub>i</sub>, high<sub>i</sub>, and w are known, the last term is a constant

Define @A<sub>0</sub> as

 $@A - (low_1 \times (high_2 - low_2 + 1) \times w - low_2 \times w)$ 

And  $len_2$  as (high<sub>2</sub>-low<sub>2</sub>+1)



If **@A** is known, **@A**<sub>0</sub> is a known constant. hight<sub>2</sub>

1.4

2,4

## Array References

### What about arrays as actual parameters?

Whole arrays, as call-by-reference parameters

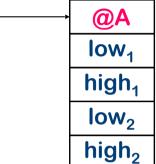
- Need dimension information  $\Rightarrow$  build a dope vector
- Store the values in the calling sequence
- Pass the address of the dope vector in the parameter slot
- Generate complete address polynomial at each reference

### Some improvement is possible

- Choose the address polynomial based on the false zero
- Pre-compute the fixed terms in prologue sequence

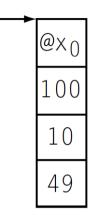
What about call-by-value?

- Most languages pass arrays by reference
- This is a language design issue



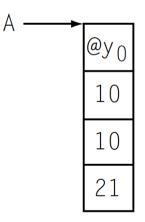
## The Dope vector

```
program main;
  begin;
    declare x(1:100,1:10,2:50),
         y(1:10,1:10,15:35) float;
     . . .
    call fee(x)
    call fee(y);
  end main;
procedure fee(A)
  declare A(*,*,*) float;
  begin;
    declare x float:
      declare i, j, k fixed binary;
       . . .
      x = A(i,j,k);
  end fee;
```



А

At the First Call



At the Second Call

## Range checking

A program that refers out-of-the-bound array elements is not well formed.

Some languages like Java requires out-of-the-bound accesses be detected and reported.

In other languages compilers have included mechanisms to detect and report out-of-the-bound accesses.

The easy way is to introduce is to introduce a runtime check that verifies that the index value falls in the array range

the compiler has to prove Expensive!! that a given reference cannot generate an out-of-bounds reference

Information on the bounds in the dope vector

## Array Address Calculations

### Array address calculations are a major source of overhead

- Scientific applications make extensive use of arrays and array-like structures
  - Computational linear algebra, both dense & sparse
- Non-scientific applications use arrays, too
  - Representations of other data structures
    - → Hash tables, adjacency matrices, tables, structures, ...

### Array calculations tend iterate over arrays

- Loops execute more often than code outside loops
- Array address calculations inside loops make a huge difference in efficiency of many compiled applications

Reducing array address overhead has been a major focus of optimization since the 1950s.

## Example: Array Address Calculations in a Loop

A, B are declared as conformablefloating-point arraysA[I,J] = A[I,J] + B[I,J]In column-major order $A_0 + (j \times len_1 + i) \times w$ number of rows!

Naïve: Perform the address calculation twice

DO J = 1, N  

$$R1 = @A_0 + (J \times len_1 + I) \times W$$
  
 $R2 = @B_0 + (J \times len_1 + I) \times W$   
 $MEM(R1) = MEM(R1) + MEM(R2)$   
END DO

Example: Array Address Calculations in a Loop

```
DO J = 1, N
A[I,J] = A[I,J] + B[I,J]
END DO
```

More sophisticated: Move common calculations out of loop

```
R1 = I \times w

c = len<sub>1</sub> × w ! Compile-time constant

R2 = @A<sub>0</sub> + R1

R3 = @B<sub>0</sub> + R1

DO J = 1, N

a = J × c

R4 = R2 + a

R5 = R3 + a

MEM(R4) = MEM(R4) + MEM(R5)

END DO
```

## Example: Array Address Calculations in a Loop

```
DO J = 1, N
A[I,J] = A[I,J] + B[I,J]
END DO
```

Very sophisticated: Convert multiply to add

R1 =  $I \times w$ c = len<sub>1</sub> x w ! Compile-time constant R2 = @A<sub>0</sub> + R1 ; R3 = @B<sub>0</sub> + R1; DO J = 1, N R2 = R2 + c R3 = R3 + c MEM(R2) = MEM(R2) + MEM(R3)

END DO

Operator Strength Reduction (§ 10.4.2 in EaC)

J is now bookkeeping

A good compiler would

rewrite the end-of-

loop test to operate

(Linear function test

on R2 or R3

replacement)

## Representing and Manipulating Strings

Character strings differ from scalars, arrays, & structures

- Languages support can be different:
  - In C most manipulations takes the form of calls to library routines
  - Other languages provvide first-class mechanism to specify substrings or concatenate them
- Fundamental unit is a character
  - Typical sizes are one or two bytes
  - Target ISA may (or may not) support character-size operations

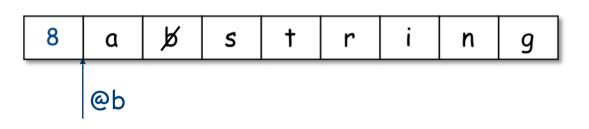
### String operation can be costly

- Older CISC architectures provide extensive support for string manipulation
- Modern RISC architectures rely on compiler to code this complex operations using a set a of simpler operations

Representing and Manipulating Strings

Two common representations of string "a string"

• Explicit length field



Length field may take more space than terminator

Null termination

- Language design issue
  - Fixed-length versus varying-length strings (1 or 2 length fields)

## Representing and Manipulating Strings

### Each representation as advantages and disadvantages

Operation	Explicit Length	Null Termination
Assignment	Straightforward	Straightforward
Checked Assignment	Checking is easy	Must count length
Length	O(1)	O(n)
Concatenation	Must copy data	Length + copy data

Unfortunately, null termination is almost considered normal

- Hangover from design of C
- Embedded in OS and API designs

Single character assignment

- With character operations
  - Compute address of rhs, load character
  - Compute address of lhs, store character
- With only word operations
  - Compute address of word containing rhs & load it
  - Move character to destination position within word
  - Compute address of word containing lhs & load it
  - Mask out current character & mask in new character
  - Store lhs word back into place

# a[1]=b[2]

### (>1 char per word)

### Multiple character assignment

Two strategies

- 1. Wrap a loop around the single character code, or
- 2. Work up to a word-aligned case, repeat whole word moves, and handle any partial-word end case

With character operations

With only word operations

### Concatenation

- String concatenation is a length computation followed by a pair of whole-string assignments
  - Touches every character
  - There can be length problems!

### Length Computation

- Representation determines cost
  - Explicit length turns length(b) into a memory reference
  - Null termination turns length(b) into a loop of memory references and arithmetic operations
- Length computation arises in other contexts
  - Whole-string or substring assignment
  - Checked assignment (buffer overflow)
  - Concatenation
  - Evaluating call-by-value actual parameter

How should the compiler represent them?

• Answer depends on the target machine

Implementation of booleans, relational expressions & control flow constructs varies widely with the ISA

Two classic approaches

- Numerical (explicit) representation
- Positional (implicit) representation

Best choice depends on both context and ISA Some cases works better with the first representation other ones with the second!

## **Boolean & Relational Expressions**

### First, we need to recognize boolean & relational expressions

Expr	$\rightarrow$	Expr v AndTerm	NumExpr	$\rightarrow$	NumExpr + Term
		AndTerm			NumExpr - Term
AndTerm	$\rightarrow$	AndTerm <pre></pre>			Term
	I	RelExpr	Term	$\rightarrow$	Term × Value
RelExpr	$\rightarrow$	RelExpr < NumExpr			Term ÷ Value
	Ι	RelExpr ≤NumExpr			Value
	I	RelExpr = NumExpr	Value	$\rightarrow$	- Factor
	I	RelExpr ≠ NumExpr		I	Factor
	I	RelExpr ≥NumExpr	Factor		( Expr )
		RelExpr > NumExpr			number

## **Boolean & Relational Values**

Next, we need to represent the values

### Numerical representation

- Assign numerical values to TRUE and FALSE
- Use hardware AND, OR, and NOT operations
- Use comparison to get a boolean from a relational

If the target machine supports boolean operations that computethe boolean resultcmp\_LT rx,ry-> r1r1=True if rx<=ry, r1=False otherwise</td>

 $\begin{array}{lll} x < y & becomes & cmp\_LT & r_x, r_y & \Rightarrow r_1 \\ \\ \mbox{if } (x < y) & & \\ \mbox{then stmt}_1 & becomes & cmp\_LT & r_x, r_y & \Rightarrow r_1 \\ \\ \mbox{then stmt}_2 & & cmp\_LT & r_x, r_y & \Rightarrow r_1 \\ \\ \mbox{cbr} & r_1 & \rightarrow \_stmt_1, \_stmt_2 \end{array}$ 

## **Boolean & Relational Values**

What if the target machine uses a condition code?

cmp r1,r2 -> cc sets cc with code for LT,LE,EQ,GE,GT,NE

- Must use a conditional branch to interpret result of compare
- If the target machine computes a code result of the comparison and we need to store the result of the boolean operation

	x < y	becomes		cmp	r <sub>x</sub> ,r <sub>y</sub>	$\Rightarrow$	CC <sub>1</sub>
				cbr_LT	CC <sub>1</sub>	$\rightarrow$	L <sub>T</sub> ,L <sub>F</sub>
aha   T aa  2	 ว		L <sub>T</sub> :	loadl	1	$\Rightarrow$	r <sub>2</sub>
cbr_LT cc 12,13 sets PC=12 if C		:13 otherwise		br		$\rightarrow$	LE
			L <sub>F</sub> :	loadl	0	$\Rightarrow$	r <sub>2</sub>
			L <sub>E</sub> :	oti	her state	ements	5

The last example actually encoded result in r2

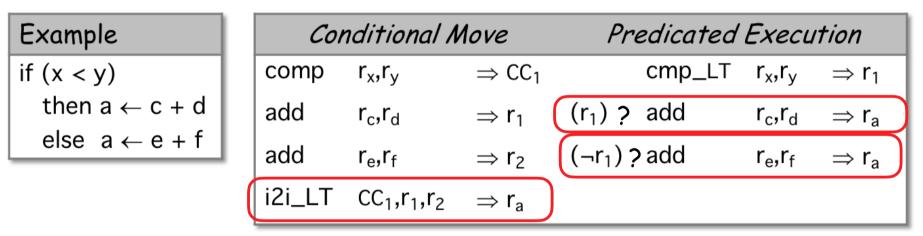
If result is used to control an operation, that may suffice

	Str	aight Col	nditiol	n Codes	E	Boolean C	ompar	isons
Example		comp	r <sub>x</sub> ,r <sub>y</sub>	$\Rightarrow$ CC <sub>1</sub>		cmp_LT	r <sub>x</sub> ,r <sub>y</sub>	$\Rightarrow$ r <sub>1</sub>
if (x < y)		cbr_LT	$CC_1$	$\rightarrow L_1, L_2$		cbr		$\rightarrow L_1, L_2$
then $a \leftarrow c + d$	L <sub>1</sub> :	add	r <sub>c</sub> ,r <sub>d</sub>	$\Rightarrow$ r <sub>a</sub>	L <sub>1</sub> :	add	r <sub>c</sub> ,r <sub>d</sub>	$\Rightarrow$ r <sub>a</sub>
else a ← e + f		br		$\rightarrow L_{OUT}$		br		$\rightarrow L_{OUT}$
	L <sub>2</sub> :	add	r <sub>e</sub> ,r <sub>f</sub>	$\Rightarrow$ r <sub>a</sub>	L <sub>2</sub> :	add	r <sub>e</sub> ,r <sub>f</sub>	$\Rightarrow$ r <sub>a</sub>
		br		$\rightarrow L_{OUT}$		br		$\rightarrow L_{OUT}$
	L <sub>OUT</sub> :	nop			L <sub>OUT</sub> :	nop		

Positional encoding!

### Other Architectural Variations

### Conditional move & predication both simplify this code



i2i\_LT cc,r1,r2->r3 copy r1 in r3 if cc matches LT, copy r2 in r3 otherwise

(r1)? add r2,r3 ->r4 the add operation executes if r1 is true

Both versions avoid the branches

Both are shorter than cond'n codes or Boolean-valued compare

Are they equivalent to the initial code? Not always!

Are they better? does code size matter? or execution time?

## **Boolean & Relational Values**

### Consider the assignment $x \leftarrow a < b \land c < d$

Sti	raight Co	nditic	on Codes	Boolean Compare
	comp	r <sub>a</sub> ,r <sub>b</sub>	$\Rightarrow$ CC <sub>1</sub>	cmp_LT $r_a, r_b \Rightarrow r_1$
	cbr_LT	$CC_1$	$\rightarrow L_1, L_2$	cmp_LT $r_c, r_d \Rightarrow r_2$
L <sub>1</sub> :	comp	r <sub>c</sub> ,r <sub>d</sub>	$\Rightarrow$ CC <sub>2</sub>	and $r_1, r_2 \implies r_x$
	cbr_LT	$CC_2$	$\rightarrow L_3, L_2$	
L <sub>2</sub> :	loadl	0	$\Rightarrow$ r <sub>x</sub>	
	br		$\rightarrow L_{OUT}$	
L <sub>3</sub> :	loadl	1	$\Rightarrow$ r <sub>x</sub>	
L <sub>OUT</sub> :	nop			

Here, Boolean compare produces much better code

## **Boolean & Relational Values**

### Conditional move & predication help here, too

	Со	nditional N	Nove	Predica	ted Ex	Recution
	comp	r <sub>a</sub> ,r <sub>b</sub>	$\Rightarrow$ CC <sub>1</sub>	cmp_LT	r <sub>a</sub> ,r <sub>b</sub>	$\Rightarrow$ r <sub>1</sub>
	i2i_LT	$CC_1, r_T, r_F$	$\Rightarrow$ r <sub>1</sub>	cmp_LT	r <sub>c</sub> ,r <sub>d</sub>	$\Rightarrow$ r <sub>2</sub>
x	comp	r <sub>c</sub> ,r <sub>d</sub>	$\Rightarrow$ CC <sub>2</sub>	and	r <sub>1</sub> ,r <sub>2</sub>	$\Rightarrow$ r <sub>x</sub>
	i2i_LT	$CC_2, r_T, r_F$	$\Rightarrow$ r <sub>2</sub>			
	and	<b>r</b> <sub>1</sub> , <b>r</b> <sub>2</sub>	$\Rightarrow$ r <sub>x</sub>			

i2i\_LT cc,r1,r2->r3 copy r1 in r3 if cc matches LT, copy r2 in r3 otherwise

Conditional move is worse than Boolean compare Predication is identical to Boolean compares

The bottom line:

 $\Rightarrow$  Context & hardware determine the appropriate choice

### If-then-else

- Follow model for evaluating relationals & booleans with branches (if the if-then-else statement have trivial parts )
- Using predicate for large blocks in the then and else part wastes execution cycles

### Branching versus predication

- Frequency of execution
  - Uneven distribution  $\Rightarrow$  do what it takes to speed common case
- Amount of code in each case
  - Unequal amounts means predication may waste issue slots
- Control flow inside the construct
  - Any branching activity within the construct complicates the predicates and makes branches attractive

Optimize boolean expression evaluation (lazy evaluation)

- Once value is determined, skip rest of the evaluation if (x or y and z) then ...
  - If x is true, need not evaluate y or z
    - → Branch directly to the "then" clause
  - On a PDP-11 or a VAX, short circuiting saved time
- Modern architectures may favor evaluating full expression
  - Rising branch latencies make the short-circuit path expensive
  - Conditional move and predication may make full path cheaper
- Past: compilers analyzed code to insert short circuits
- Future: compilers analyze code to prove legality of full path evaluation where language specifies short circuits

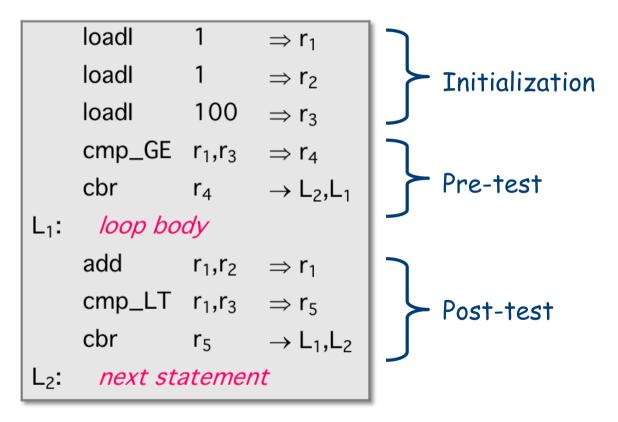
## Loops Evaluate condition before loop (if needed) • Evaluate condition after loop Pre-test Branch back to the top (if needed) Loop body Post-test while, for, do, & until all fit this basic model Next block



## **Control Flow**

## Implementing Loops

for (i = 1; i< 100; 1) { loop body }
next statement</pre>



### Break statements

Many modern programming languages include a break

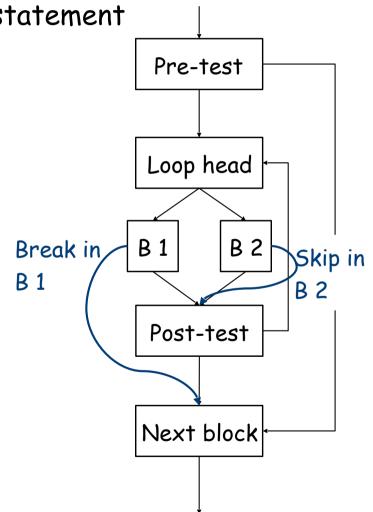
Exits from the innermost control-flow statement

- Out of the innermost loop
- Out of a case statement

Translates into a jump

- Targets statement outside controlflow construct
- Creates multiple-exit construct
- Skip in loop goes to next iteration

Only make sense if loop has > 1 block



- 1 Evaluate the controlling expression
- 2 Branch to the selected case
- 3 Execute the code for that case
- 4 Branch to the statement after the case

Parts 1, 3, & 4 are well understood,

part 2 is the key:

need an efficient method to locate the designated code

many compilers provvide several different search schemas each one can be better in some cases.

### Case Statements

- 1 Evaluate the controlling expression
- 2 Branch to the selected case
- 3 Execute the code for that case
- 4 Branch to the statement after the case

(use break)

Parts 1, 3, & 4 are well understood, part 2 is the key

### Strategies

- Linear search (nested if-then-else constructs)
- Build a table of case expressions & binary search it
- Directly compute address (requires dense case set)

swite	ch $(e_1)$	{		
cas	se 0:	blocko	;	
		break:		
Ć a s	se 1:	blockl	•	
		break;		
cas	se 3:	block <sub>3</sub>	;	
		break;		
def	fault:	blockd	;	
		break;		
}				

 $t_1 \leftarrow e_1$ if  $(t_1 = 0)$ then block\_0 else if  $(t_1 = 1)$ then block\_1 else if  $(t_1 = 2)$ then block\_2 else if  $(t_1 = 3)$ then block\_3

else block<sub>d</sub>

Switch Statement

### Implementing as a Linear Search

## **Binary Search**

#### switch $(e_1)$ {

case	0:	block <sub>0</sub>
		break;
case	15:	$block_{15}$
		break;
case	23:	$block_{23}$
		break;
 case	99:	block99
 case	99:	<i>block</i> 99 break;
 case defau		break;
		break;

Value	Label
0	LBO
15	LB <sub>15</sub>
23	LB <sub>23</sub>
37	LB <sub>37</sub>
41	LB <sub>41</sub>
50	LB <sub>50</sub>
68	LB <sub>68</sub>
72	LB72
83	LB <sub>83</sub>
99	LB99

Malus I alsol

### $t_1 \leftarrow e_1$

Switch Statement

}

# Search Table

Code for Binary Search

## **Direct Address Computation**

### • requires dense case set

```
switch (e_1) {
```

case 0:	block <sub>0</sub>
	break;
case 1:	block
	break;
case 2:	block <sub>2</sub>
	break;
case 9:	block9
case 9:	<i>block</i> g break;
case 9: default:	100
	break;

Label	
LBO	
LB1	
LB2	
LB3	
LB4	
LB <sub>5</sub>	
LB <sub>6</sub>	
LB7	
LB8	
LBg	

```
Jump Table
```

 $\begin{array}{rl} t_1 \leftarrow e_1 \\ \text{if } (0 > t_1 \text{ or } t_1 > 9) \\ \text{then jump to } LB_d \\ \text{else} \\ t_2 \leftarrow @Table + t_1 \times 4 \\ t_3 \leftarrow memory(t_2) \\ \text{jump to } t_3 \end{array}$ 

Code for Address Computation

Switch Statement