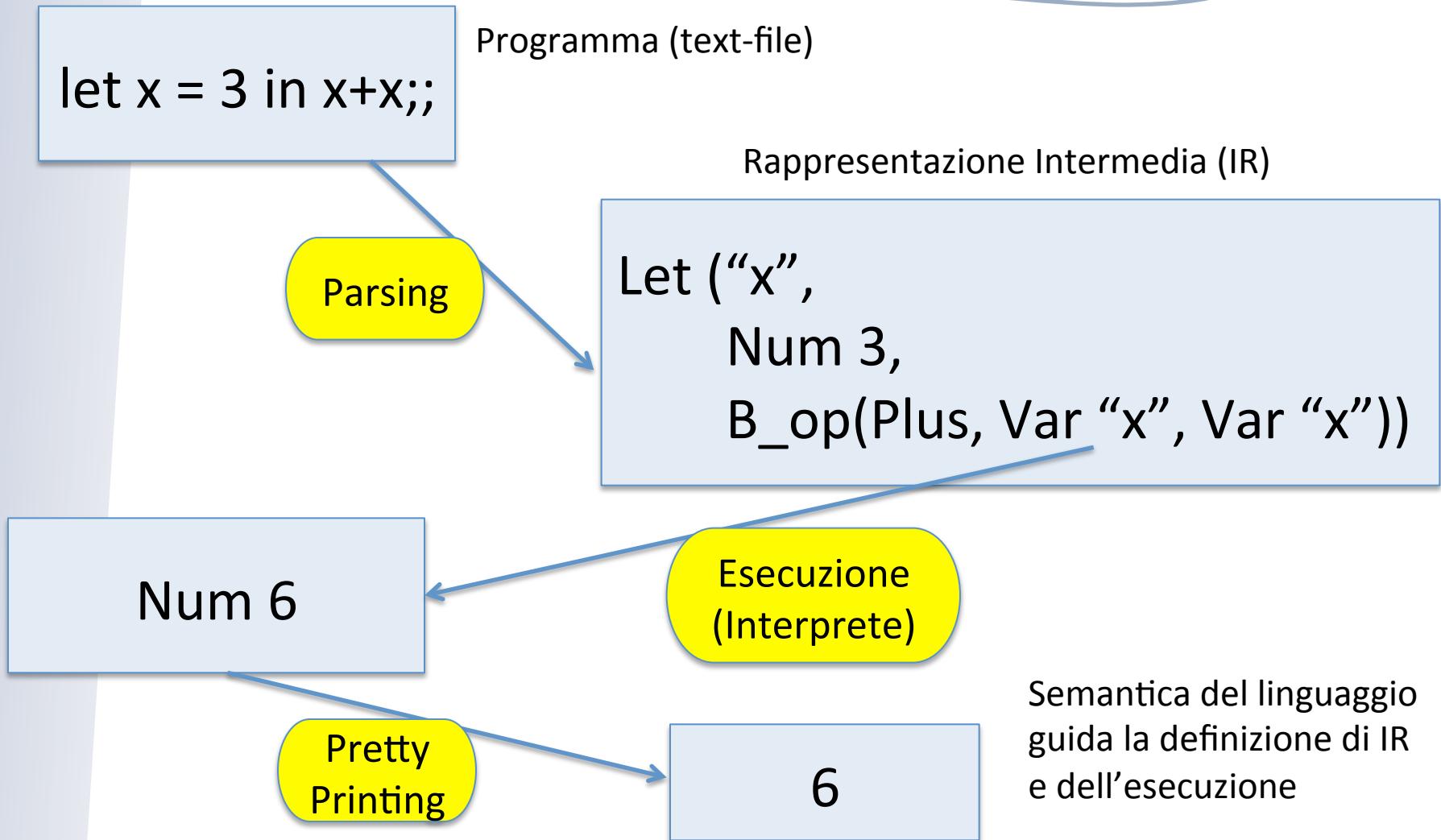


AA 2016-2017

17. Realizzare un interprete in OCaml



La struttura





La struttura nel dettaglio

OCAML Type per descrivere la rappresentazione intermedia

```
type variable = string
```

```
type op = Plus | Minus | Times | ...
```

```
type exp =
| Int_e of int
| Op_e of exp * op * exp
| Var_e of variable
| Let_e of variable * exp * exp
```

```
type value = exp
```



La struttura nel dettaglio

```
type variable = string
```

```
type op = Plus | Minus | Times | ...
```

```
type exp =
| Int_e of int
| Op_e of exp * op * exp
| Var_e of variable
| Let_e of variable * exp * exp
```

```
type value = exp
```

*Rappresentazione di
“3 + 17”*

```
let e1 = Int_e 3
let e2 = Int_e 17
let e3 = Op_e (e1, Plus, e2)
```



```
let x = 30 in  
let y =  
(let z = 3 in  
  z*4) in  
y+y;;
```

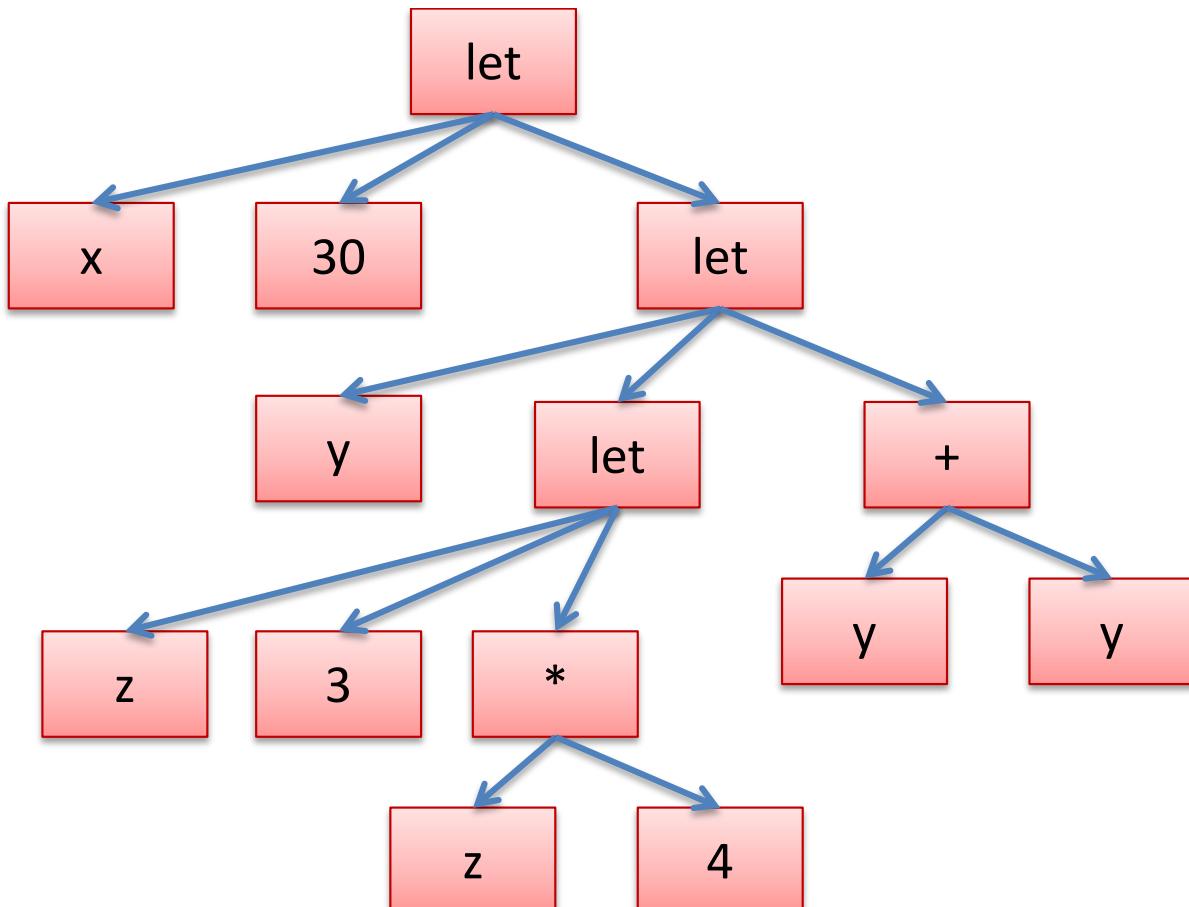
Programma OCaml

Exp

```
Let_e("x", Int_e 30,  
      Let_e("y",  
            Let_e("z", Int_e 3,  
                  Op_e(Var_e "z", Times, Int_e 4)),  
                  Op_e(Var_e "y", Plus, Var_e "y"))
```



AST



Variabili: dichiarazione e uso



```
type variable = string
```

```
type exp =
| Int_e of int
| Op_e of exp * op * exp
| Var_e of variable
| Let_e of variable * exp * exp
```

Run time: operazione di supporto

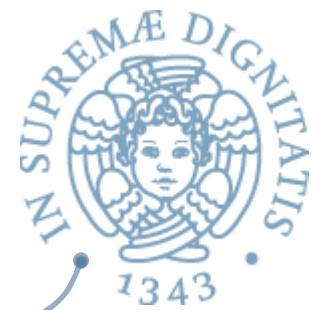


```
let is_value (e : exp) : bool =  
    match e with  
        | Int_e_ -> true  
        | ( Op_e_ _ ) -> false;  
        | Let_e_ _ -> false;  
        | Var_e_ _ -> false;;
```

eval_op : value -> op -> value -> value

substitute : value -> variable -> exp -> exp

Variabili: dichiarazione e uso

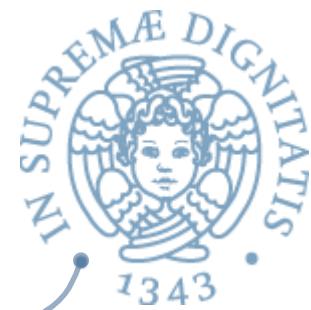


Type variable = string

```
type exp =
  | Int_e of int
  | Op_e of exp * op * exp
  | Var_e of variable
  | Let_e of variable * exp * exp
```

**Uso di
una
variabile**

Variabili: dichiarazione e uso



Type variable = string

```
type exp =
  | Int_e of int
  | Op_e of exp * op * exp
  | Var_e of variable
  | Let_e of variable * exp * exp
```

**Uso di
una
variabile**

**Dichiarazione
di variable**



L'interprete

RTS **is_value** : exp -> bool
 eval_op : value -> op -> value -> value
 substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | Int_e i ->
  | Op_e(e1,op,e2) ->
  | Let_e(x,e1,e2) ->
```



L'interprete

RTS **is_value** : exp -> bool
 eval_op : value -> op -> value -> value
 substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | Int_e i -> Int_e i
  | Op_e(e1,op,e2) ->
  | Let_e(x,e1,e2) ->
```



L'interprete

RTS **is_value** : exp -> bool
eval_op : value -> op -> value -> value
substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | Int_e i -> Int_e i
  | Op_e(e1,op,e2) -> let v1 = eval e1 in
                           let v2 = eval e2 in
                           eval_op v1 op v2
  | Let_e(x,e1,e2) ->
```



L'interprete

RTS **is_value** : exp -> bool
eval_op : value -> op -> value -> value
substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | Int_e i -> Int_e i
  | Op_e(e1,op,e2) -> let v1 = eval e1 in
    let v2 = eval e2 in
    eval_op v1 op v2
  | Let_e(x,e1,e2) -> let v1 = eval e1 in
    let e2' = substitute v1 x e2 in
    eval e2'
```



L'interprete

RTS **is_value** : exp -> bool
 eval_op : value -> op -> value -> value
 substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | Int_e i -> Int_e i
  | Op_e(e1,op,e2) -> eval_op eval e1 op eval e2
  | Let_e(x,e1,e2) -> let v1 = eval e1 in
    let e2' = substitute v1 x e2 in
      eval e2'
```



L'interprete

RTS **is_value** : exp -> bool
eval_op : value -> op -> value -> value
substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =  
  match e with  
  | Int_e i -> Int_e i  
  | Op_e(e1,op,e2) -> eval_op eval e1 op eval e2  
  | Let_e(x,e1,e2) -> let v1 = eval e1 in  
                           let e2' = substitute v1 x e2 in  
                           eval e2'
```

Come avviene la valutazione?

Usare **let** per definirne l'ordine



L'interprete

RTS **is_value** : exp -> bool
eval_op : value -> op -> value -> value
substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =  
  match e with  
  | Int_e i -> Int_e i  
  | Op_e(e1,op,e2) -> eval_op eval e1 op eval e2  
  | Let_e(x,e1,e2) -> let v1 = eval e1 in  
    let e2' = substitute v1 x e2 in  
      eval e2'  
  | Var_e x -> ???
```

Non dovremmo incontrare una variabile – l'avremmo già dovuta sostituire con un valore!!

Questo è un errore di tipo



L'interprete

RTS **is_value** : exp -> bool
eval_op : value -> op -> value -> value
substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp option =
  match e with
  | Int_e i -> Some(Int_e i)
  | Op_e(e1,op,e2) -> eval_op eval e1 op eval e2
  | Let_e(x,e1,e2) -> let v1 = eval e1 in
    let e2' = substitute v1 x e2 in
    eval e2'
  | Var_e x -> None
```



Questo complica l'interprete:
matching sui risultati delle
chiamate ricorsive di eval



L'interprete

RTS **is_value** : exp -> bool
 eval_op : value -> op -> value -> value
 substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =  
  match e with  
  | Int_e i -> Int_e i  
  | Op_e(e1,op,e2) -> eval_op eval e1 op eval e2  
  | Let_e(x,e1,e2) -> let v1 = eval e1 in  
    let e2' = substitute v1 x e2 in  
    eval e2'  
  | Var_e x -> raise (UnboundVariable x)
```

Tali eccezioni fanno parte del RTS



RTS: eval_op

```
let eval_op (v1:exp) (op:operand) (v2:exp) : exp =  
  match v1, op, v2 with  
    | Int_e i, Plus, Int_e j -> Int_e (i + j)  
    | Int_e i, Minus, Int_e j -> Int_e (i - j)  
    | Int_e i, Times, Int_e j -> Int_e (i * j)  
    | _, (Plus | Minus | Times), _ ->  
        if is_value v1 && is_value v2  
          then raise Type Error  
          else raise Not Value
```



RTS: substitution

```
let substitute (v:value) (x:variable) (e:expr) : expr =  
  let rec subst (e:expr) : expr =  
    match e with  
      | Int_e _ ->  
      | Op_e(e1,op,e2) ->  
      | Var_e y -> ... use x ...  
      | Let_e (y,e1,e2) -> ... use x ...  
  
in subst e
```



RTS: substitution

```
let substitute (v:value) (x:variable) (e:expr) : expr =  
  let rec subst (e:expr) : expr =  
    match e with  
      | Int_e _ -> e  
      | Op_e(e1,op,e2) ->  
      | Var_e y -> ... use x ...  
      | Let_e (y,e1,e2) -> ... use x ...  
  
in subst e
```



RTS: substitution

```
let substitute (v:value) (x:variable) (e:expr) : expr =  
let rec subst (e:expr) : expr =  
    match e with  
        | Int_e _ -> e  
        | Op_e(e1,op,e2) -> Op_e(subst e1,op,subst e2)  
        | Var_e y -> ... use x ...  
        | Let_e (y,e1,e2) -> ... use x ...
```

in subst e

x, v impliciti

RTS: substitution



```
let substitute (v:value) (x:variable) (e:expr) : expr =  
  let rec subst (e:expr) : expr =  
    match e with  
      | Int_e _ -> e  
      | Op_e(e1,op,e2) -> Op_e(subst e1,op,subst e2)  
      | Var_e y -> if x = y then v else e  
      | Let_e (y,e1,e2) -> ... use x ...
```

in subst e

RTS: substitution



```
let substitute (v:value) (x:variable) (e:expr) : expr =  
let rec subst (e:expr) : expr =  
    match e with  
        | Int_e _ -> e  
        | Op_e(e1,op,e2) -> Op_e(subst e1,op,subst e2)  
        | Var_e y -> if x = y then v else e  
        | Let_e (y,e1,e2) -> Let_e (y,subst e1,subst e2)
```

in subst e



RTS: substitution

```
let substitute (v:value) (x:variable) (e:expr) : expr =  
let rec subst (e:expr) : expr =  
    match e with  
        | Int_e _ -> e  
        | Op_e(e1,op,e2) -> Op_e(subst e1,op,subst e2)  
        | Var_e y -> if x = y then v else e  
        | Let_e (y,e1,e2) -> Let_e (y,subst e1,subst e2)
```

in subst e

ERRORE



RTS: substitution

```
let substitute (v:value) (x:variable) (e:expr) : expr =  
let rec subst (e:expr) : expr =  
    match e with  
        | Int_e _ -> e  
        | Op_e(e1,op,e2) -> Op_e(subst e1,op,subst e2)  
        | Var_e y -> if x = y then v else e  
        | Let_e (y,e1,e2) -> Let_e (y,subst e1,  
                                         if x = y then e2 else subst e2)
```

in subst e

*If $x = y$...
shadow scope!!*

Funzioni





Sintassi

```
type exp = Int_e of int | Op_e of exp * op * exp  
| Var_e of variable | Let_e of variable * exp * exp  
| Fun_e of variable * exp | FunCall_e of exp * exp
```



Sintassi

```
type exp = Int_e of int | Op_e of exp * op * exp  
| Var_e of variable | Let_e of variable * exp * exp  
| Fun_e of variable * exp | FunCall_e of exp * exp
```

La sintassi OCaml **fun x e** viene rappresentata come **Fun_e(x, e)**

La chiamata **fact 3** viene rappresentata come
FunCall_e (Var_e "fact", Int_e 3)



Estendiamo il RTS

```
let is_value (e : exp) : bool =  
    match e with  
        | Int_e _ -> true  
        | Fun_e (_,_) -> true  
        | ( Op_e (_,_,_) )  
        | Let_e (_,_,_)  
        | Var_e _  
        | FunCall_e (_,_) ) -> false
```

Le funzioni sono valori!!



Interprete ++

is_value : exp -> bool

eval_op : value -> op -> value -> value

substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
    match e with
    | :
    | Var_e x -> raise (UnboundVariable x)
    | Fun_e (x, e) -> Fun_e (x, e)
    | FunCall_e (e1, e2) ->
        match eval e1, eval e2 with
        | Fun_e (x, e), v2 -> eval (substitute v2 x e)
        | _ -> raise (TypeError)
```



Funzioni ricorsive

```
type exp = Int_e of int | Op_e of exp * op * exp  
| Var_e of variable | Let_e of variable * exp * exp  
| Fun_e of variable * exp | FunCall_e of exp * exp  
| Rec_e of variable * variable * exp  
  
let g = rec f x -> f (x + 1) in g 3  
Let_e ("g",  
    Rec_e ("f", "x",  
        FunCall_e (Var_e "f", Op_e (Var_e "x", Plus, Int_e 1))  
    ),  
    FunCall (Var_e "g", Int_e 3)  
)
```

Le funzioni ricorsive sono valori



```
let is_value (e : exp) : bool =  
    match e with  
        | Int_e _ -> true  
        | Fun_e (_,_) -> true  
        | Rec_e of (_,_,_) -> true  
        | ( Op_e (_,_,_)  
            | Let_e (_,_,_)  
            | Var_e _  
            | FunCall_e (_,_) ) -> false
```



La nozione di sostituzione

- ☞ Sostituire il valore v al posto della variabile x nella espressione e : **$e [v / x]$**
- ☞ $(x + y) [7/y]$ diventa $(x + 7)$
- ☞ $(\text{let } x = 30 \text{ in let } y = 40 \text{ in } x + y) [7/y]$ diventa
 $(\text{let } x = 30 \text{ in let } y = 40 \text{ in } x + y)$
- ☞ $(\text{let } y = y \text{ in let } y = y \text{ in } y + y) [7/y]$ diventa
 $(\text{let } y = 7 \text{ in let } y = y \text{ in } y + y)$

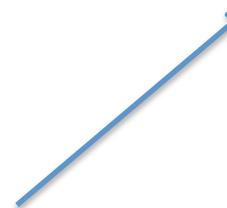
Come valutare le funzioni ricorsive



IDEA

(rec f x = body) arg --> body [arg/x] [rec f x = body/f]

Passaggio parametri



JIT compilation del body



```
let g = rec f x ->
    if x <= 0 then x
        else x + f (x - 1)
in g 3
```

La dichiarazione

```
g 3 [rec f x ->
    if x <= 0 then x
        else x + f (x-1) / g]
```

La sostituzione

```
(rec f x ->
    if x <= 0 then x else x + f (x - 1))
3
```

Risultato finale



(if $x \leq 0$ then x else $x + f(x - 1)$)

[3 / x]

[rec f x ->

if $x \leq 0$ then x

else $x + f(x - 1) / f$]

(if $3 \leq 0$ then 3 else $3 +$

(rec f x ->

if $x \leq 0$ then x

else $x + f(x - 1)) (3 - 1)$



Interprete

is_value : exp -> bool

eval_op : value -> op -> value -> value

substitute : value -> variable -> exp -> exp

```
let rec eval (e : exp) : exp =
  match e with
  | :
  | FunCall_e (e1, e2) ->
    match eval e1 with
    | Fun_e (x, e) -> let v = eval e2 in substitute e x v
    | (Rec_e (f, x, e)) as g -> let v = eval e2 in
        substitute (substitute e x v) f g
```

Cosa abbiamo imparato?



- ☞ OCaml può essere usato come linguaggio per la simulazione della semantica operazionale di un linguaggio (incluso se stesso!)
- ☞ Vantaggio: simulazione dell'implementazione
- ☞ Svantaggio: complicato per le operazioni da effettuare con i tipi di Ocaml
 - Op_e(e1, Plus, e2) rispetto a “e1 + e2”