

Five aspects of learning a PL

1. **Syntax:** How do you write language constructs?
 2. **Semantics:** What do programs mean? (Type checking, evaluation rules)
 3. **Idioms:** What are typical patterns for using language features to express your computation?
 4. **Libraries:** What facilities does the language (or a well-known project) provide “standard”? (E.g., file access, data structures)
 5. **Tools:** What do language implementations provide to make your job easier? (E.g., top-level, debugger, GUI editor, ...)
- All are essential for good programmers to understand
 - Breaking a new PL down into these pieces makes it easier to learn

Expressions

Expressions (aka *terms*):

- primary building block of OCaml programs
- akin to *statements* or *commands* in imperative languages
- can get arbitrarily large since any expression can contain subexpressions, etc.

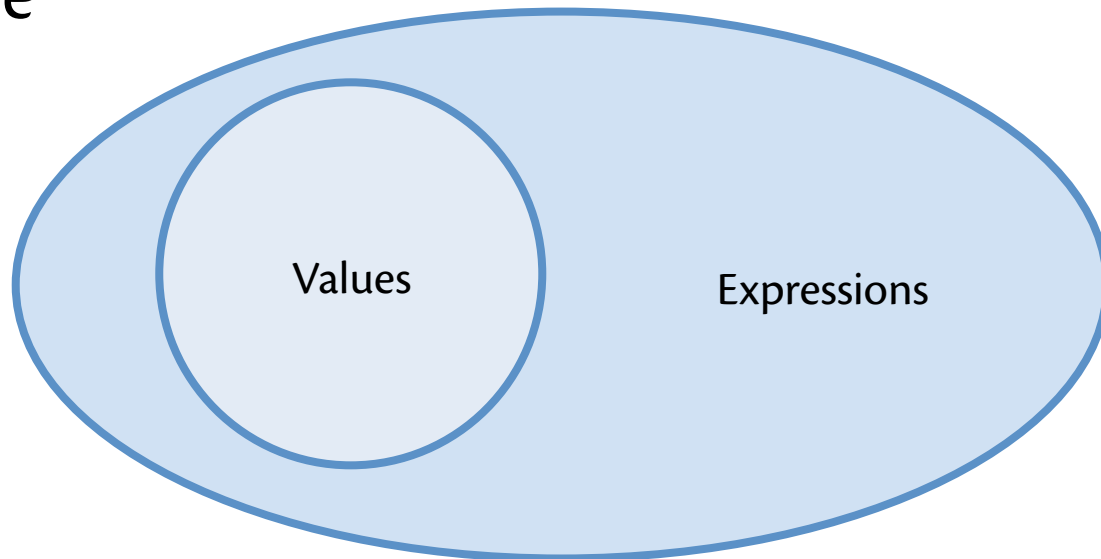
Every kind of expression has:

- **Syntax**
- **Semantics:**
 - **Type-checking rules:** produce a type or fail with an error message
 - **Evaluation rules:** produce a *value*
 - (or exception or infinite loop)
 - Used only on expressions that type-check

Values

A **value** is an expression that does not need any further evaluation

- **34** is a value of type **int**
- **34+17** is an expression of type **int** but is not a value



Let expressions

Syntax:

```
let x = e1 in e2
```

x is an *identifier*

e1 and **e2** are *expressions*

let x = e1 in e2 is itself an expression

x = e1 is a *binding*

e.g.

```
let x = 2 in x+x
```

```
let inc x = x+1 in inc 10
```

```
let y = "zar" in (let z = "doz" in y^z)
```

Let expressions

let **x** = **e1** **in** **e2**

Evaluation:

- Evaluate **e1** to a value **v1**
- Substitute **v1** for **x** in **e2**, yielding a new expression **e2'**
- Evaluate **e2'** to **v**
- Result of evaluation is **v**

Let expressions

let x = 1+4 in x*3

--> Evaluate **e1** to a value **v1**

let x = 5 in x*3

--> Substitute **v1** for **x** in **e2**, yielding a new expression **e2'**

5*3

--> Evaluate **e2'** to **v**

15

Result of evaluation is **v**

Let expressions in REPL

Syntax:

let **x** = **e**

Implicitly, “**in** *rest of what you type*”

E.g., you type:

```
let a="zar";;  
let b="doz";;  
let c=a^b;;
```

OCaml understands as

```
let a="zar" in  
  let b="doz" in  
    let c=a^b in...
```

Scope

Bindings are in effect only in the *scope* (the “block”) in which they occur.

```
let x=42 in  
  (* y is not in scope here *)  
x + (let y="3110" in  
  (* y is in scope here *)  
  int_of_string y)
```

Exactly what you're used to from (e.g.) Java

Overlapping scope

Overlapping bindings of the same name is usually bad **idiom** (and darn confusing)

```
let x = 5 in ( (let x = 6 in x ) + x )
```

To what value does the above expression evaluate?

- 10
- 11
- 12
- None of the above

Substitution

`let x = 5 in ((let x = 6 in x) + x)`

-->

???

Not a choice:

`let x = 5 in (6 + 6)`

Two choices:

A. `((let x = 6 in x) + 5)`

B. `((let x = 6 in 5) + 5)`

Substitution

`let x = 5 in ((let x = 6 in x) + x)`

-->

???

Not a choice:

`let x = 5 in (6 + 6)`

Two choices:

A. `((let x = 6 in x) + 5)`

B. ~~`((let x = 6 in 5) + 5)`~~

Why?

Principle of Name Irrelevance

The name of a variable should not matter.

In math, these are the same functions:

$$f(x) = x^2$$

$$f(y) = y^2$$

So in programming, these should be the same functions:

```
let f x = x*x
```

```
let f y = y*y
```

This principle is also called *alpha equivalence*

Principle of Name Irrelevance

Likewise, these should be the same expressions:

```
(let x = 6 in x)
```

```
(let y = 6 in y)
```

So these should also be the same:

```
let x = 5 in ((let x = 6 in x) + x)
```

```
let x = 5 in ((let y = 6 in y) + x)
```

But if we substitute inside inner **let** expression, they will not be the same:

```
(let x = 6 in 5) + 5 -----> 10
```

```
(let y = 6 in y) + 5 -----> 11
```

Back to substitution

let x = 5 **in** ((**let** x = 6 **in** x) + x)

-->

???

Not a choice:

let x = 5 **in** (6 + 6)

Two choices:

A. ((**let** x = 6 **in** x) + 5)

B. ~~((**let** x = 6 **in** 5) + 5)~~

That's why!

Shadowing

A new binding *shadows* an older binding of the same name

```
let x = 5 in (  + x )
```

Shadowing is not assignment

```
let x = 5 in ((let x = 6 in x) + x)
```

```
-----> 11
```

```
let x = 5 in (x + (let x = 6 in x))
```

```
-----> 11
```


Types

Write **colon** to indicate type of expression

As does the top-level:

```
# let x = 42;;
```

```
val x : int = 42
```

Type-checking of let expression:

If $e1 : t1$,

and if $e2 : t2$ (assuming that $x : t1$),

then $(\text{let } x = e1 \text{ in } e2) : t2$

Let expressions (summary)

- **Syntax:**

let **x** = **e1** **in** **e2**

- **Type-checking:**

If **e1** : **t1**, and if **e2** : **t2** under the assumption that **x** : **t1**, then **let x = e1 in e2** : **t2**

- **Evaluation:**

- Evaluate **e1** to **v1**

- Substitute **v1** for **x** in **e2** yielding new expression **e2'**

- Evaluate **e2'** to **v**

- Result of evaluation is **v**

Function declaration

Functions:

- Like Java methods, have arguments and result
- Unlike Java, no classes, **this**, **return**, etc.

Example *function declaration*:

```
(* requires: y>=0 *)
(* returns: x to the power of y *)
let rec pow x y =
  if y=0 then 1
  else x * pow x (y-1)
```

Note: “**rec**” is required because the body includes a recursive *function call*:
pow (x, y-1)

Function declaration

- **Syntax:**

`let f x1 x2 ... xn = e`

- **Evaluation:**

- No evaluation!
- Just declaring the function
- Will be evaluated when applied to arguments

- **Type-checking:**

- Conclude that $f : t_1 \rightarrow \dots \rightarrow t_n \rightarrow t$ if $e : t$ under assumptions:
 - $x_1 : t_1, \dots, x_n : t_n$ (arguments with their types)
 - $f : t_1 \rightarrow \dots \rightarrow t_n \rightarrow t$ (for recursion)

Writing argument types

Though types can be inferred, you can write them too:

```
let rec pow (x : int) (y : int) : int =  
  if y=0 then 1  
  else x * pow x (y-1)
```

```
let rec pow x y =  
  if y=0 then 1  
  else x * pow x (y-1)
```

```
let cube x = pow x 3
```

```
let cube (x : int) : int = pow x 3
```

Function application

Syntax: e0 e1 ... en

- Parentheses not strictly required around argument(s)
- If there is exactly one argument and you do use parentheses and you leave out the space, syntax looks like C function call: **e0 (e1)**

Function application

Type-checking

if $e_0 : t_1 \rightarrow \dots \rightarrow t_n \rightarrow t$

and $e_1 : t_1, \dots, e_n : t_n$

then $e_0 e_1 \dots e_n : t$

e.g., $\text{pow } 2 \ 3 : \text{int}$

Function application

Evaluation of $e_0 \ e_1 \ \dots \ e_n$

1. Evaluate e_0 to a function
let $f \ x_1 \ \dots \ x_n = e$
2. Evaluate arguments $e_1 \ \dots \ e_n$ to values
 $v_1 \ \dots \ v_n$
3. Substitute v_i for x_i in e yielding new expression e'
4. Evaluate e' to a value v , which is result

Anonymous functions

Something that is *anonymous* has no name.

- **42** is an anonymous **int**
- and we can bind it to a name:
let x = 42
- **(fun x -> x+1)** is an anonymous function
- and we can bind it to a name:
let inc = fun x -> x+1

Anonymous functions

Syntax: $(\text{fun } x_1 \dots x_n \rightarrow e)$

Evaluation:

- A function is already a value: no further computation to do
- In particular, body e is not evaluated until function is applied

Type checking:

$(\text{fun } x_1 \dots x_n \rightarrow e) : t_1 \rightarrow \dots \rightarrow t_n \rightarrow t$
if $e : t$ under assumptions $x_1 : t_1, \dots, x_n : t_n$

Anonymous functions

These two declarations are **syntactically different** but **semantically equivalent**:

```
let inc = fun x -> x+1
```

```
let inc x = x+1
```

Anonymous functions

These two expressions are **syntactically different** but **semantically equivalent**:

```
let x = 7 in x+1
```

```
(fun x -> x+1) 7
```

Functions are values

- Can use them **anywhere** we use values
- Functions can **take** functions as arguments
- Functions can **return** functions as results
 - ...so functions are *higher-order*
- This is not a new language feature; just a consequence of "functions are values"
- But it is a feature with massive consequences

"A language that doesn't affect the way you think about programming is not worth knowing." --Alan Perlis

Alan Jay Perlis



1922-1990

First Winner of Turing Award (1966)

*for his influence in the area of
advanced programming techniques
and compiler construction*

Google "perlisisms" for great quotes
about programming

Higher-order functions

```
(* some base function *)
```

```
let double x = 2*x
```

```
let square x = x*x
```

```
(* apply those functions twice *)
```

```
let quad x = double (double x)
```

```
let fourth x = square (square x)
```

Higher-order functions

```
(* higher order function that  
 * applies f twice to x *)
```

```
let twice f x = f (f x)
```

```
val twice : ('a -> 'a) -> 'a -> 'a
```

'a is a *type variable*: could be any type

Higher-order functions

```
(* higher-order function that  
  * applies f twice to x *)
```

```
let twice f x = f (f x)
```

```
(* define functions using twice *)
```

```
let quad x = twice double x
```

```
let fourth x = twice square x
```

```
(* even better definitions *)
```

```
let quad = twice double
```

```
let fourth = twice square
```