

Principles of Programming Languages

<http://www.di.unipi.it/~andrea/Didattica/PLP-16/>

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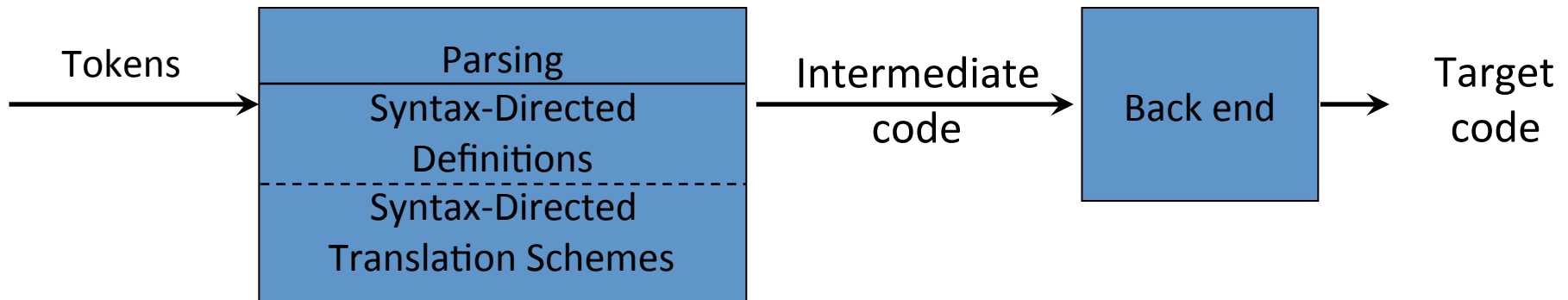
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Lesson 11

- Intermediate-Code Generation
 - Intermediate representations
 - Syntax-directed translation to three address code

Intermediate Code Generation (II)

- Facilitates *retargeting*: enables attaching a back end for the new machine to an existing front end



Summary

- Intermediate representations
- Three address statements and their implementations
- Syntax-directed translation to three address statements
 - Expressions and statements
 - Logical and relational expressions
 - Translating short-circuit Boolean expressions and flow-of-control statements with backpatching lists

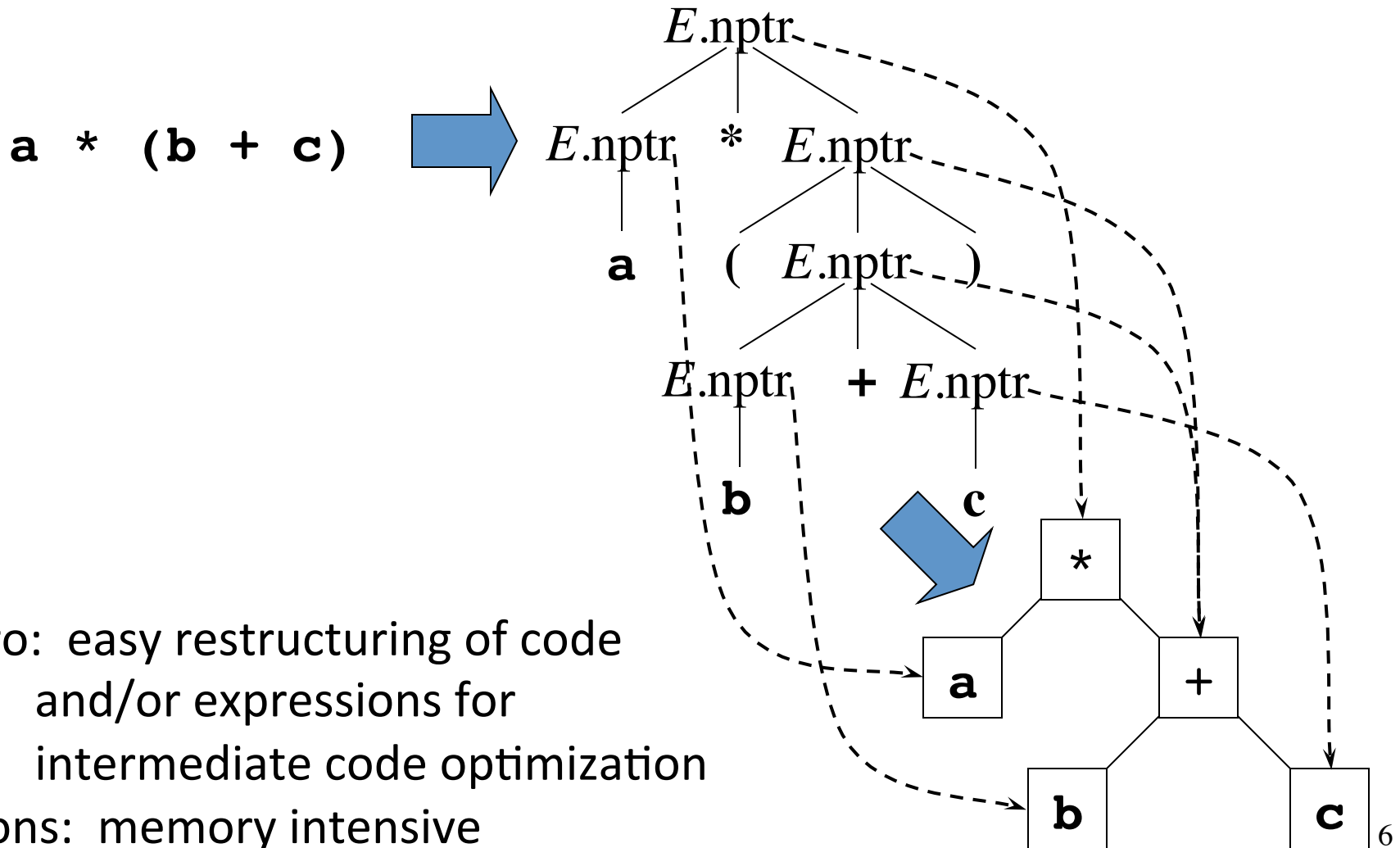
Intermediate Representations

- *Graphical representations* (e.g. AST and DAGs)
- *Postfix notation*: operations on values stored on operand stack (similar to JVM bytecode)
- *Three-address code*: (e.g. *triples* and *quads*)
 $x := y \text{ op } z$
- *Two-address code*:
 $x := \text{op } y$
which is the same as $x := x \text{ op } y$

Syntax-Directed Translation of Abstract Syntax Trees

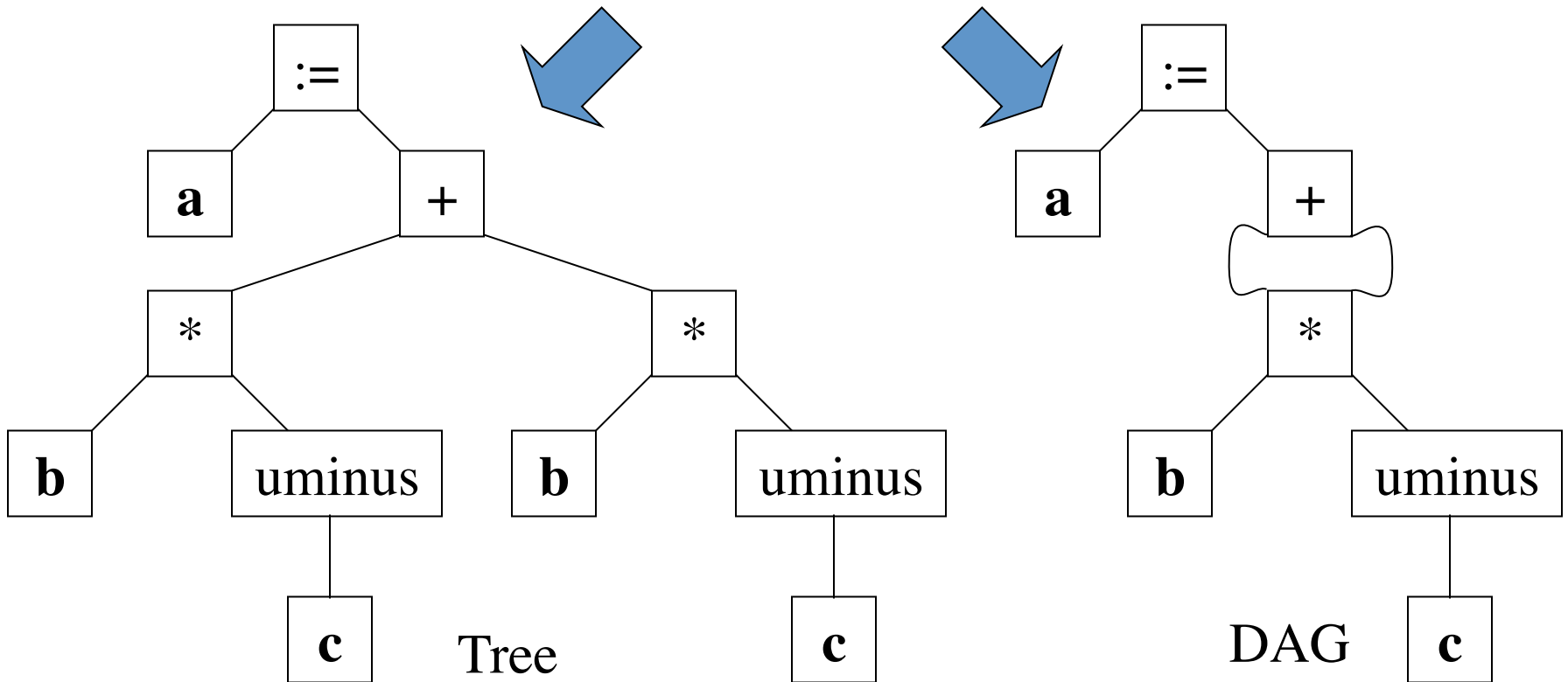
Production	Semantic Rule
$S \rightarrow \mathbf{id} := E$	$S.nptr := mknode(':=' , mkleaf(\mathbf{id}, \mathbf{id}.entry), E.nptr)$
$E \rightarrow E_1 + E_2$	$E.nptr := mknode('+' , E_1.nptr, E_2.nptr)$
$E \rightarrow E_1 * E_2$	$E.nptr := mknode('*' , E_1.nptr, E_2.nptr)$
$E \rightarrow - E_1$	$E.nptr := mknode('uminus' , E_1.nptr)$
$E \rightarrow (E_1)$	$E.nptr := E_1.nptr$
$E \rightarrow \mathbf{id}$	$E.nptr := mkleaf(\mathbf{id}, \mathbf{id}.entry)$

Abstract Syntax Trees



Abstract Syntax Trees versus DAGs

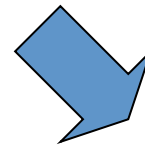
a := b * -c + b * -c



- Repeated subtrees are shared
- Implementation: *mkleaf* and *makenode* are redefined. They do not create a new node if it exists already.

Postfix Notation

a := b * -c + b * -c



a b c uminus * b c uminus * + assign

Postfix notation represents
operations on a stack

Pro: easy to generate

Cons: stack operations are more
difficult to optimize

Bytecode (for example)

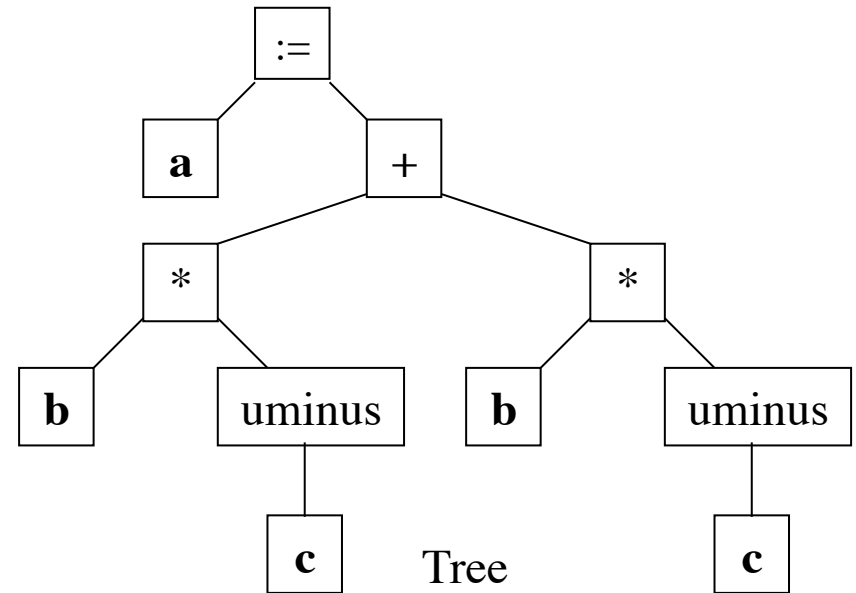
```
iload 2 // push b
iload 3 // push c
ineg // uminus
imul // *
iload 2 // push b
iload 3 // push c
ineg // uminus
imul // *
iadd // +
istore 1 // store a 8
```


Three-Address Code (1)

a := b * -c + b * -c



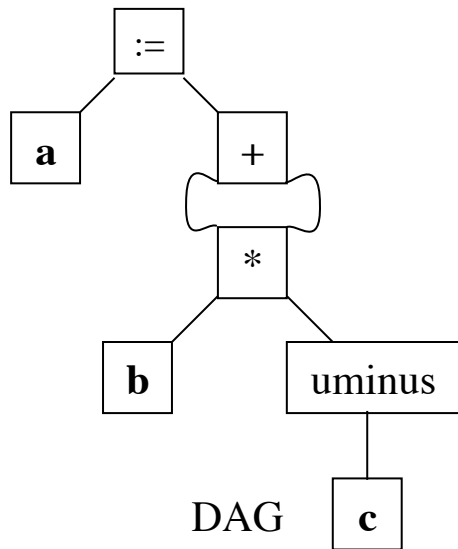
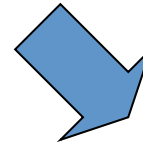
```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a := t5
```



Linearized representation
of a syntax tree

Three-Address Code (2)

a := b * -c + b * -c



```
t1 := - c
t2 := b * t1
t5 := t2 + t2
a := t5
```

Linearized representation
of a syntax DAG

Three-Address Statements

“Addresses” are *names, constants or temporaries*

- Assignment statements: $x := y \text{ op } z$, $x := \text{op } y$
- Indexed assignments: $x := y[i]$, $x[i] := y$
- Pointer assignments: $x := \&y$, $x := *y$, $*x := y$
- Copy statements: $x := y$
- Unconditional jumps: **goto** *lab*
- Conditional jumps: **if** $x \text{ relop } y$ **goto** *lab*
- Function calls: **param** $x\dots$; **call** p, n
(or $y = \text{call } p, n$); **return** y

Implementation of Three-Address Statements: **Quads**

Sample expression

a := b * -c + b * -c

Three-address code

t1 := - c

t2 := b * t1

t3 := - c

t4 := b * t3

t5 := t2 + t4

a := t5

#	Op	Arg1	Arg2	Res
(0)	uminus	c		t1
(1)	*	b	t1	t2
(2)	uminus	c		t3
(3)	*	b	t3	t4
(4)	+	t2	t4	t5
(5)	:=	t5		a

Quads (quadruples)

Pro: easy to rearrange code for global optimization

Cons: lots of temporaries

Implementation of Three-Address Statements: Triples

Sample expression

a := b * -c + b * -c

Three-address code

t1 := - c

t2 := b * t1

t3 := - c

t4 := b * t3

t5 := t2 + t4

a := t5

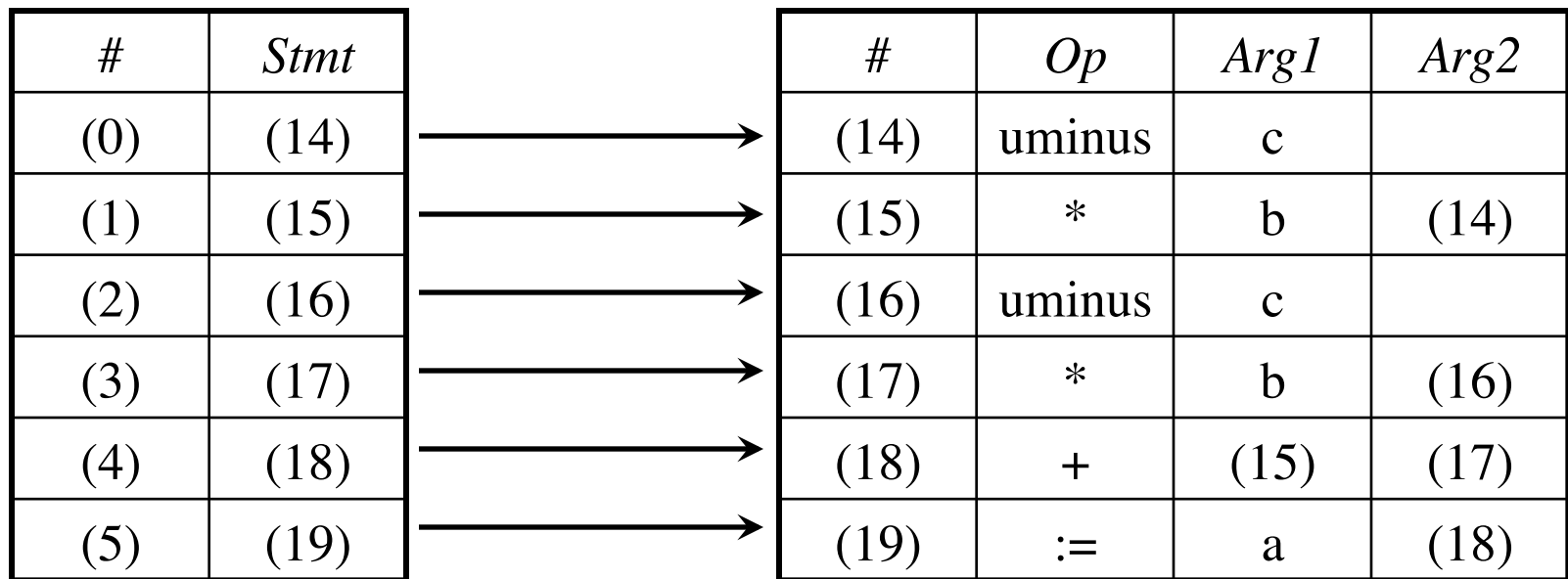
#	Op	Arg1	Arg2
(0)	uminus	c	
(1)	*	b	(0)
(2)	uminus	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	:=	a	(4)

Triples

Pro: temporaries are implicit

Cons: difficult to rearrange code

Implementation of Three-Address Statements: **Indirect Triples**



Program

Triple container

Pro: temporaries are implicit & easier to rearrange code

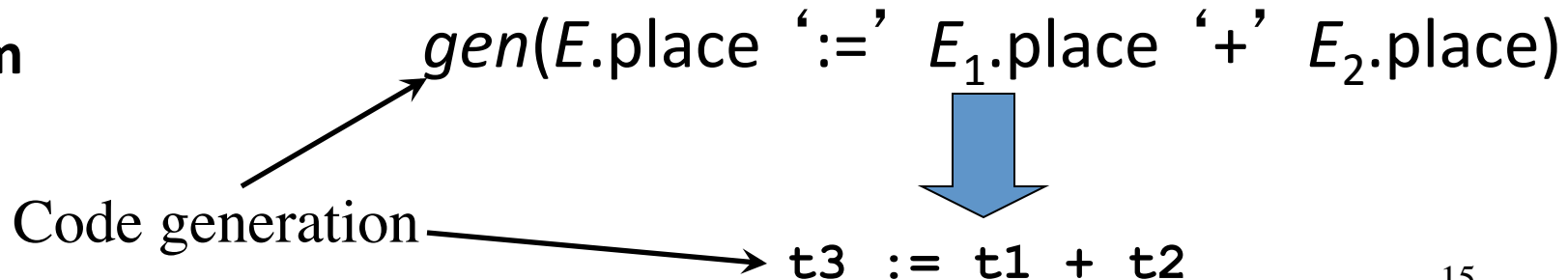
Syntax-Directed Translation into Three-Address Code

Productions

$S \rightarrow$ `id := E`
| `while E do S`
| `S ; S`
 $E \rightarrow$ `E + E`
| `E * E`
| `- E`
| `(E)`
| `id`
| `num`

Synthesized attributes:

$S.code$ three-address code for S
 $S.begin$ label to start of S or nil
 $S.after$ label to end of S or nil
 $E.code$ three-address code for E
 $E.place$ a name holding the value of E



Syntax-Directed Translation into Three-Address Code (cont'd)

Productions

Semantic rules

$S \rightarrow \mathbf{id} := E$	$S.code := E.code \parallel gen(\mathbf{id}.place \text{ ':=' } E.place); S.begin := S.after := nil$
$S \rightarrow \mathbf{while} E$ $\mathbf{do} S_1$	(see next slide)
$E \rightarrow E_1 + E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '+' } E_2.place)$
$E \rightarrow E_1 * E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place \text{ ':=' } E_1.place \text{ '*' } E_2.place)$
$E \rightarrow - E_1$	$E.place := newtemp();$ $E.code := E_1.code \parallel gen(E.place \text{ ':=' } \text{'uminus'} E_1.place)$
$E \rightarrow (E_1)$	$E.place := E_1.place$ $E.code := E_1.code$
$E \rightarrow \mathbf{id}$	$E.place := \mathbf{id}.name$ $E.code := \text{''}$
$E \rightarrow \mathbf{num}$	$E.place := newtemp();$ $E.code := gen(E.place \text{ ':=' } \mathbf{num}.value)$
$S \rightarrow S_1 ; S_2$	$S.code := S_1.code \parallel S_2.code$ $S.begin := S_1.begin$ $S.after := S_2.after_{16}$

Syntax-Directed Translation into Three-Address Code (cont'd)

Production

$S \rightarrow \text{while } E \text{ do } S_1$

Semantic rule

$S.\text{begin} := \text{newlabel}()$

$S.\text{after} := \text{newlabel}()$

$S.\text{code} := \text{gen}(S.\text{begin} \text{ ':' }) \parallel$

$E.\text{code} \parallel$

$\text{gen}(\text{'if' } E.\text{place} \text{ '=' '0' 'goto' } S.\text{after}) \parallel$

$S_1.\text{code} \parallel$

$\text{gen}(\text{'goto' } S.\text{begin}) \parallel$

$\text{gen}(S.\text{after} \text{ ':' })$

$S.\text{begin}:$

$E.\text{code}$

if $E.\text{place} = 0$ **goto** $S.\text{after}$

$S.\text{code}$

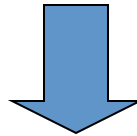
goto $S.\text{begin}$

$S.\text{after}:$

...

Example (check it at home!)

```
i := 2 * n + k;  
while i do  
    i := i - k
```



```
t1 := 2  
t2 := t1 * n  
t3 := t2 + k  
i := t3  
L1: if i = 0 goto L2  
    t4 := i - k  
    i := t4  
    goto L1  
L2:
```

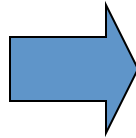
How does the code access names?

- The three-address code generated by the syntax-directed definitions shown is simplistic
- It assumes that the names of variables can be easily resolved by the back-end in global or local variables
- We need **local symbol tables** to record global declarations as well as local declarations in procedures, blocks, and records (structs) to resolve names
- We will see all this later in the course

Translating Logical and Relational Expressions

Boolean expressions intended to represent values:

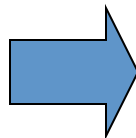
a or b and not c



```
t1 := not c  
t2 := b and t1  
t3 := a or t2
```

Boolean expressions used to alter the control flow:

a < b



```
if a < b goto L1  
t1 := 0  
goto L2  
L1: t1 := 1  
L2:
```

Short-Circuit Code

- The boolean operators `&&`, `||` and `!` are translated into jumps.
- Example:

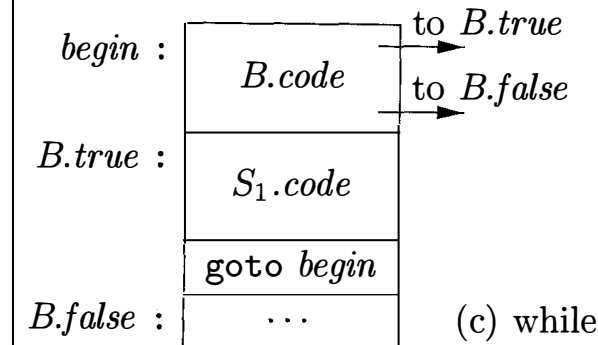
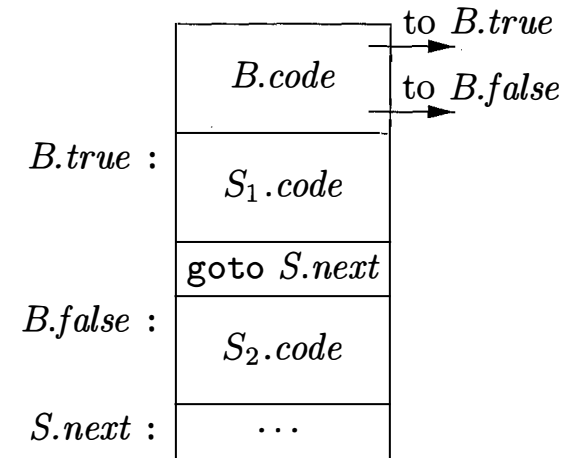
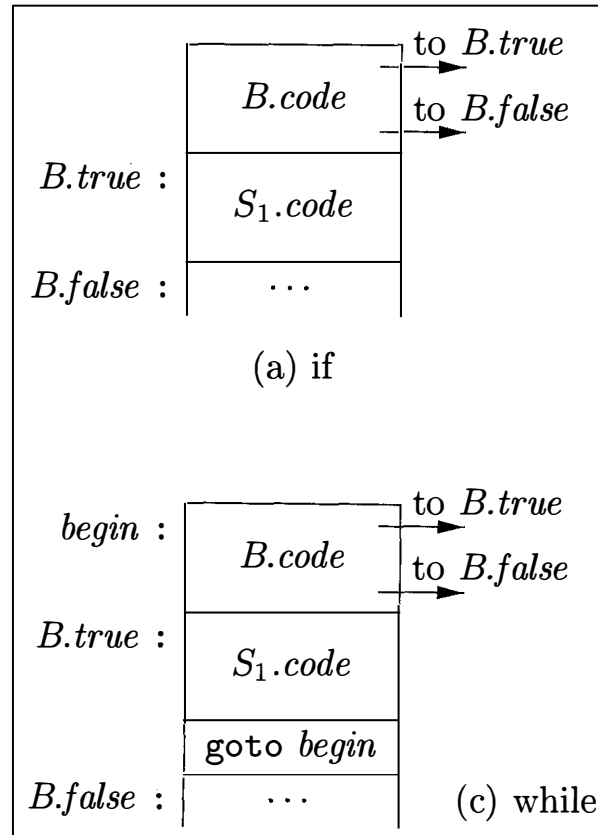
```
if ( x < 100 || x > 200 && x != y ) x = 0;
```

may be translated into:

```
    if x < 100 goto L2
    ifFalse x > 200 goto L1
    ifFalse x != y goto L1
L2: x=0
L1:
```

Translating Flow-of-control Statements

$S \rightarrow \text{if} (B) S_1$
 $S \rightarrow \text{if} (B) S_1 \text{ else } S_2$
 $S \rightarrow \text{while} (B) S_1$



Synthesized Attributes:

$S.code$, $B.Code$

Inherited Attributes:

labels for jumps:

$B.true$, $B.false$, $S.next$

PRODUCTION	SEMANTIC RULES
$P \rightarrow S$	$S.next = newlabel()$ $P.code = S.code \parallel label(S.next)$
$S \rightarrow \text{assign}$	$S.code = \text{assign}.code$
$S \rightarrow \text{if} (B) S_1$	$B.true = newlabel()$ $B.false = S_1.next = S.next$ $S.code = B.code \parallel label(B.true) \parallel S_1.code$
$S \rightarrow \text{if} (B) S_1 \text{ else } S_2$	$B.true = newlabel()$ $B.false = newlabel()$ $S_1.next = S_2.next = S.next$ $S.code = B.code$ $\parallel label(B.true) \parallel S_1.code$ $\parallel gen('goto' S.next)$ $\parallel label(B.false) \parallel S_2.code$
$S \rightarrow \text{while} (B) S_1$	$begin = newlabel()$ $B.true = newlabel()$ $B.false = S.next$ $S_1.next = begin$ $S.code = label(begin) \parallel B.code$ $\parallel label(B.true) \parallel S_1.code$ $\parallel gen('goto' begin)$
$S \rightarrow S_1 S_2$	$S_1.next = newlabel()$ $S_2.next = S.next$ $S.code = S_1.code \parallel label(S_1.next) \parallel S_2.code$

Not relevant for control flow

Inherited Attributes

Translation of Boolean Expressions

PRODUCTION	SEMANTIC RULES
$B \rightarrow B_1 \parallel B_2$	$B_1.true = B.true$ $B_1.false = newlabel()$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \parallel label(B_1.false) \parallel B_2.code$
$B \rightarrow B_1 \ \&\& \ B_2$	$B_1.true = newlabel()$ $B_1.false = B.false$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \parallel label(B_1.true) \parallel B_2.code$
$B \rightarrow ! B_1$	$B_1.true = B.false$ $B_1.false = B.true$ $B.code = B_1.code$
$B \rightarrow E_1 \ \mathbf{rel} \ E_2$	$B.code = E_1.code \parallel E_2.code$ $\parallel gen('if' \ E_1.addr \ rel.op \ E_2.addr \ 'goto' \ B.true)$ $\parallel gen('goto' \ B.false)$
$B \rightarrow \mathbf{true}$	$B.code = gen('goto' \ B.true)$
$B \rightarrow \mathbf{false}$	$B.code = gen('goto' \ B.false)$

Inherited Attributes

Example

```
if ( x < 100 || x > 200 && x != y ) x = 0;
```

is translated into:

```
    if x < 100 goto L2
    goto L3
L3:  if x > 200 goto L4
    goto L1
L4:  if x != y goto L2
    goto L1
L2:  x=0
L1:
```

By removing several redundant jumps we can obtain the equivalent:

```
    if x < 100 goto L2
    ifFalse x > 200 goto L1
    ifFalse x != y goto L1
L2:  x=0
L1:
```

Translating Short-Circuit Expressions Using Backpatching

Idea: **avoid using inherited attributes** by generating partial code. Addresses for jumps will be inserted when known.

$E \rightarrow E$ or $M E$

| E and $M E$

| not E

| (E)

| id relop id

| true

| false

M : marker nonterminal

Synthesized attributes:

E .truelist

backpatch list for jumps on true

E .falselist

backpatch list for jumps on false

M .quad

location of current three-address quad

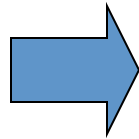
$M \rightarrow \varepsilon$

Backpatch Operations with Lists

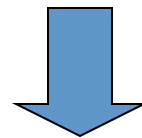
- *makelist(i)* creates a new list containing three-address location i , returns a pointer to the list
- *merge(p_1, p_2)* concatenates lists pointed to by p_1 and p_2 , returns a pointer to the concatenated list
- *backpatch(p, i)* inserts i as the target label for each of the statements in the list pointed to by p

Backpatching with Lists: Example

$a < b$ or $c < d$ and $e < f$



```
100: if a < b goto _  
101: goto _  
102: if c < d goto _  
103: goto _  
104: if e < f goto _  
105: goto _
```



backpatch

```
100: if a < b goto TRUE →  
101: goto 102  
102: if c < d goto 104  
103: goto FALSE →  
104: if e < f goto TRUE →  
105: goto FALSE →
```

Backpatching with Lists: Translation Scheme

$M \rightarrow \varepsilon$ { $M.\text{quad} := \text{nextquad}()$ }

$E \rightarrow E_1$ **or** $M E_2$
 { $\text{backpatch}(E_1.\text{falselist}, M.\text{quad});$
 $E.\text{truelist} := \text{merge}(E_1.\text{truelist}, E_2.\text{truelist});$
 $E.\text{falselist} := E_2.\text{falselist}$ }

$E \rightarrow E_1$ **and** $M E_2$
 { $\text{backpatch}(E_1.\text{truelist}, M.\text{quad});$
 $E.\text{truelist} := E_2.\text{truelist};$
 $E.\text{falselist} := \text{merge}(E_1.\text{falselist}, E_2.\text{falselist});$ }

$E \rightarrow$ **not** E_1 { $E.\text{truelist} := E_1.\text{falselist};$
 $E.\text{falselist} := E_1.\text{truelist}$ }

$E \rightarrow (E_1)$ { $E.\text{truelist} := E_1.\text{truelist};$
 $E.\text{falselist} := E_1.\text{falselist}$ }

Backpatching with Lists: Translation Scheme (cont'd)

```
 $E \rightarrow id_1 \text{ relop } id_2$ 
    { E.truelist := makelist(nextquad());
      E.falselist := makelist(nextquad() + 1);
      emit( 'if' id1.place relop.op id2.place 'goto _' );
      emit( 'goto _' ) }

 $E \rightarrow \text{true}$     { E.truelist := makelist(nextquad());
                      E.falselist := nil;
                      emit( 'goto _' ) }

 $E \rightarrow \text{false}$   { E.falselist := makelist(nextquad());
                      E.truelist := nil;
                      emit( 'goto _' ) }
```

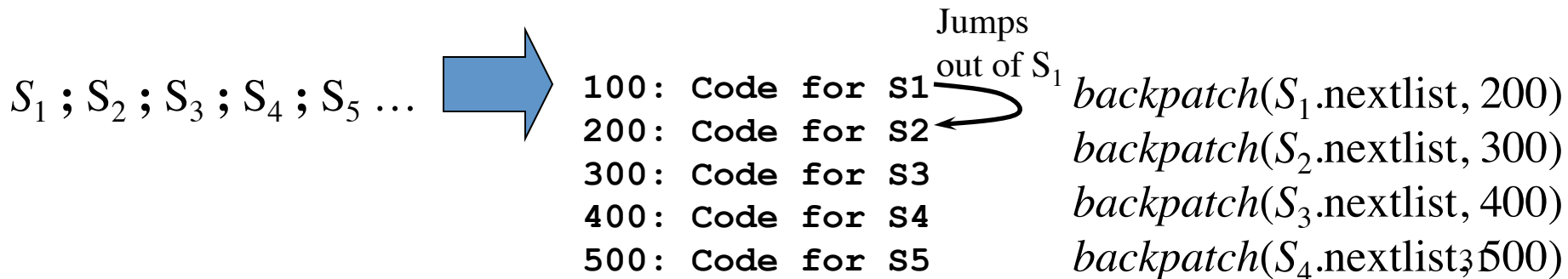
Flow-of-Control Statements and Backpatching: Grammar

$S \rightarrow$ **if** E **then** S
 | **if** E **then** S **else** S
 | **while** E **do** S
 | **begin** L **end**
 | A
 $L \rightarrow$ $L ; S$
 | S

Synthesized attributes:

$S.nextlist$ backpatch list for jumps to the next statement after S (or nil)

$L.nextlist$ backpatch list for jumps to the next statement after L (or nil)



Flow-of-Control Statements and Backpatching

The grammar is modified adding suitable marking non-terminals

$S \rightarrow A \quad \{ S.nextlist := nil \}$

$S \rightarrow \mathbf{begin} L \mathbf{end}$
 $\quad \{ S.nextlist := L.nextlist \}$

$S \rightarrow \mathbf{if} E \mathbf{then} M S_1$
 $\quad \{ \mathit{backpatch}(E.truelist, M.quad);$
 $\quad \quad S.nextlist := \mathit{merge}(E.falselist, S_1.nextlist) \}$

$L \rightarrow L_1 ; M S \quad \{ \mathit{backpatch}(L_1.nextlist, M.quad);$
 $\quad \quad L.nextlist := S.nextlist; \}$

$L \rightarrow S \quad \{ L.nextlist := S.nextlist; \}$

$M \rightarrow \varepsilon \quad \{ M.quad := \mathit{nextquad}() \}$

$A \rightarrow \dots$ *Non-compound statements, e.g. assignment, function call*

Flow-of-Control Statements and Backpatching (cont'd)

$S \rightarrow \text{if } E \text{ then } M_1 S_1 N \text{ else } M_2 S_2$
 { *backpatch*(*E*.truelist, *M*₁.quad);
 backpatch(*E*.falselist, *M*₂.quad);
 S.nextlist := *merge*(*S*₁.nextlist,
 merge(*N*.nextlist, *S*₂.nextlist)) }

$S \rightarrow \text{while } M_1 E \text{ do } M_2 S_1$
 { *backpatch*(*S*₁.nextlist, *M*₁.quad);
 backpatch(*E*.truelist, *M*₂.quad);
 S.nextlist := *E*.falselist;
 emit('goto *M*₁.quad') }

$N \rightarrow \varepsilon$ { *N*.nextlist := *makelist*(*nextquad*());
 emit('goto _') }

Summarizing...

- Translation from source code to intermediate representation can be performed in a syntax-directed way during parsing
- We considered translation of expressions and statements to three address code, with a simplified handling of names (for example: no definitions)
- More effective translation of boolean expressions for flow control require inherited attributes
- They can be avoided using **backpatching**