Principles of Programming Languages

http://www.di.unipi.it/~andrea/Didattica/PLP-14/

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Lesson 15

• Code generation (1)
Recap (last lecture)

• *Static checking vs. Dynamic checking of program properties*

• Type checking
  – Type expressions
  – Name/Structural Equivalence of types
  – Type systems: inference rules in Post system notation
  – Type conversion and coercion
On Code Generation

• Code produced by compiler must be correct
  – Source-to-target program transformation should be semantics preserving

• Code produced by compiler should be of high quality
  – Effective use of target machine resources
  – Heuristic techniques should be used to generate good but suboptimal code, because generating optimal code is undecidable
Position of a Code Generator in the Compiler Model

Source program → Front-End → Intermediate code → Code Optimizer → Intermediate code → Code Generator → Target program

Symbol Table

Lexical error
Syntax error
Semantic error
Code Generation: tasks

• Code generation has three primary tasks:
  – Instruction selection
  – Register allocation and assignment
  – Instruction ordering

• The compiler can include an optimization phase (mapping IR to optimized IR) before the code generation

• We consider some rudimentary optimizations only
Input of the Code Generator

• The input of code generation is the IR of the source program, with info in the symbol table

• Assumptions:
  – In general we assume that the IR is three-address code
  – Values and names in the IR can be manipulated directly by the target machine
  – The IR is free of syntactic and static semantic errors
  – Type conversion operators have been introduced where needed
Target Program Code

• The back-end code generator of a compiler may generate different forms of code, depending on the requirements:
  – Absolute machine code (executable code)
  – Relocatable machine code (object files for linker: allows separate compilation of subprograms)
  – Assembly language (facilitates debugging, but requires an assembly step)
Target Machine Architecture

• Defines the instruction-set, including addressing modes: high impact on the code generator
• **RISC** (*reduced instruction set computer*): many register, three address instructions, simple addressing modes
• **CISC** (*complex instruction set computer*): complex addressing modes, several register classes, variable-length instructions (possibly with side effects)
• **Stack-based machines**: operands are put on the stack and operations act on top of stack (held in register). In general less efficient.
  – Revived thanks to bytecode forms for interpreters like the Java Virtual Machine
Our Target Machine

- We consider a RISC-like machine with some CISC-like addressing modes
- Assembly code as target language (for readability)
- Our (hypothetical) machine:
  - Byte-addressable (word = 4 bytes)
  - Has $n$ general purpose registers $R0, R1, \ldots, R_{n-1}$
  - Simplified instruction-set: all operands are integer
  - Three-address instructions of the form $op\ dest, src1, src2$
The Target Machine: Instruction Set

- **LD r, x**  (load operation: \( r = x \))
- **ST x, r**   (store operation: \( x = r \))
- **OP dst, src1, src2** where OP = ADD, SUB, …: apply OP to src1 and src2, placing the result in dst).
- **BR L**      (unconditional jump: goto L)
- **Bcond r, L** (conditional jump: if \( \text{cond}(r) \) goto L)
  - **BLTZ r, L**  (if \( r < 0 \) goto L)
## The Target Machine: Addressing Modes

- **Addressing modes** ($c$ is an integer):

<table>
<thead>
<tr>
<th>Mode</th>
<th>Form</th>
<th>Address</th>
<th>Added Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Absolute</td>
<td>$M$</td>
<td>$M$</td>
<td>1</td>
</tr>
<tr>
<td>Register</td>
<td>$R$</td>
<td>$R$</td>
<td>0</td>
</tr>
<tr>
<td>Indexed</td>
<td>$c(R)$</td>
<td>$c + \text{contents}(R)$</td>
<td>1</td>
</tr>
<tr>
<td>Indirect register</td>
<td>$*R$</td>
<td>$\text{contents}(R)$</td>
<td>0</td>
</tr>
<tr>
<td>Indirect indexed</td>
<td>$*c(R)$</td>
<td>$\text{contents}(c + \text{contents}(R))$</td>
<td>1</td>
</tr>
<tr>
<td>Literal</td>
<td>#$c$</td>
<td>N/A</td>
<td>1</td>
</tr>
</tbody>
</table>
Instruction Costs

• Machine is a simple, non-super-scalar processor with fixed instruction costs
• Realistic machines have deep pipelines, various kinds of caches, parallel instructions, etc.
• Define:

\[
\text{cost (OP dst, src1, src2) = 1 + cost(dst-mode)}
\]

\[
+ \text{cost(src1-mode)}
\]

\[
+ \text{cost(src2-mode)}
\]
## Examples

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Operation</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>LD R0,R1</td>
<td>Load content(R1) into register R0</td>
<td>1</td>
</tr>
<tr>
<td>LD R0,M</td>
<td>Load content(M) into register R0</td>
<td>2</td>
</tr>
<tr>
<td>ST M,R0</td>
<td>Store content(R0) into memory location R0</td>
<td>2</td>
</tr>
<tr>
<td>BR 20(R0)</td>
<td>Jump to address 20+contents(R0))</td>
<td>2</td>
</tr>
<tr>
<td>ADD R0 R0 #1</td>
<td>Increment R0 by 1</td>
<td>2</td>
</tr>
<tr>
<td>MUL R0,M,*12(R1)</td>
<td>Multiply contents(M) by contents(12+contents(R1)) and store the result in R0</td>
<td>3</td>
</tr>
</tbody>
</table>
Instruction Selection

- Instruction selection depends on (1) the level of the IR, (2) the instruction-set architecture, (3) the desired quality (e.g. efficiency) of the generated code.

- Suppose we translate three-address code

\[ x := y + z \]

to:

\[
\begin{align*}
\text{LD} &\quad R0, y \quad \\text{R0} = y \\
\text{ADD} &\quad R0, R0, z \quad \\text{R0} = \text{R0} + z \\
\text{ST} &\quad x, R0 \quad \\text{x} = \text{R0}
\end{align*}
\]

- Then

\[ a := a + 1 \]

Better

\[
\begin{align*}
\text{ADD} &\quad a, a, \#1 \quad \text{Cost} = 4 \\
\text{INC} &\quad a \quad \text{Cost} = 2 \\
\end{align*}
\]

(If available)

Best

Cost = 6
Need for Global Machine-Specific Code Optimizations

- Suppose we translate three-address code
  \[ x := y + z \]
  to:

  \[
  \begin{align*}
  & LD \ R0, y \quad \quad \quad \quad R0 = y \\
  & ADD \ R0, R0, z \quad \quad R0 = R0 + z \\
  & ST \ x, R0 \quad \quad \quad \quad \quad x = R0
  \end{align*}
  \]

- Then, we translate
  \[ a := b + c \]
  \[ d := a + e \]
  to:

  \[
  \begin{align*}
  & LD \ R0, b \\
  & ADD \ R0, R0, c \\
  & ST \ a, R0 \\
  & LD \ R0, a \\
  & ADD \ R0, R0, e \\
  & ST \ d, R0 \\
  \end{align*}
  \]

- We can choose among several equivalent instruction sequences \( \rightarrow \) Dynamic programming algorithms
Register Allocation and Assignment

• Efficient utilization of the limited set of registers is important to generate good code

• Registers are assigned by
  – Register allocation to select the set of variables that will reside in registers at a point in the code
  – Register assignment to pick the specific register that a variable will reside in

• Finding an optimal register assignment in general is NP-complete
Choice of Instruction Ordering

• When instructions are independent, their evaluation order can be changed

\[
\begin{align*}
t_1 &= a + b \\
t_2 &= c + d \\
t_3 &= e \cdot t_2 \\
t_4 &= t_1 - t_3
\end{align*}
\]

• The reordered sequence could lead to a better target code

\[
\begin{align*}
t_2 &= c + d \\
t_3 &= e \cdot t_2 \\
t_1 &= a + b \\
t_4 &= t_1 - t_3
\end{align*}
\]
Towards Flow Graphs

• In order to improve *instruction selection, register allocation and selection*, and *instruction ordering*, we structure the input three-address code as a *flow graph*

• This allows to make explicit certain dependencies among instructions of the IR

• Simple optimization techniques are based on the analysis of such dependencies
  – Better register allocation knowing how variables are defined and used
  – Better instruction selection looking at *sequences* of three-address code statements
Flow Graphs

- A *flow graph* is a graphical representation of a sequence of instructions with control flow edges
- A flow graph can be defined at the intermediate code level or target code level
- Nodes are *basic blocks*, sequences of instructions that are always executed together
- Arcs are execution order dependencies
Basic Blocks

• A *basic block* is a sequence of instructions s.t.:
  – Control enters through the first instruction only
  – Control leaves the block without branching, except possibly at the last instruction

2) \( j=1 \)
3) \( t_1=10*i \)
4) \( t_2=t_1+j \)
5) \( t_3=8*t_2 \)
6) \( t_4=t_3-88 \)
7) \( a[t_4]=0.0 \)
8) \( j=j+1 \)
9) if \( j\leq=10 \) goto (3)
10) \( i=i+1 \)
11) if \( i\leq=10 \) goto(2)
12) \( i=1 \)
Basic Blocks and Control Flow Graphs

- A control flow graph (CFG) is a directed graph with basic blocks $B_i$ as vertices and with edges $B_i \rightarrow B_j$ iff $B_j$ can be executed immediately after $B_i$.

- Then $B_i$ is a predecessor of $B_j$, $B_j$ is a successor of $B_i$.

```
2) j=1
3) t1=10*i
4) t2=t1+j
5) t3=8*t2
6) t4=t3-88
7) a[t4]=0.0
8) j=j+1
9) if j<=10 goto (3)
10) i=i+1
11) if i<=10 goto(2)
12) i=1
```
Partition Algorithm for Basic Blocks

Input: A sequence of three-address statements
Output: A list of basic blocks with each three-address statement in exactly one block

1. Determine the set of leaders, the first statements in basic blocks
   a) The first statement is the leader
   b) Any statement that is the target of a goto is a leader
   c) Any statement that immediately follows a goto is a leader
2. For each leader, its basic block consist of the leader and all statements up to but not including the next leader or the end of the program
Partition Algorithm for Basic Blocks:
Example

1) \( i=1 \) (a)
2) \( j=1 \) (b)
3) \( t1=10*i \) (b)
4) \( t2=t1+j \)
5) \( t3=8*t2 \)
6) \( t4=t3-88 \)
7) \( a[t4]=0.0 \)
8) \( j=j+1 \)
9) if \( j<=10 \) goto(3)
10) \( i=i+1 \) (c)
11) if \( i<=10 \) goto(2)
12) \( i=1 \) (c)
13) \( t5=i-1 \) (b)
14) \( t6=88*t5 \)
15) \( a[t6] = 1.0 \)
16) \( i=i+1 \)
17) if \( i<=10 \) goto(13)

Leaders
Loops

• Programs spend most of the time executing loops
• Identifying and optimizing loops is important during code generation
• A loop is a collection of basic blocks, such that
  – All blocks in the collection are strongly connected
  – The collection has a unique entry, and the only way to reach a block in the loop is through the entry
Loops (Example)

Strongly connected components:

SCC={ {B2, B3, B4}, {B3}, {B6} }

Entries:
B2, B3, B6
Transformations on Basic Blocks

• A code-improving transformation is a code optimization to improve speed or reduce code size
• Global transformations are performed across basic blocks
• Local transformations are only performed on single basic blocks
• Transformations must be safe and preserve the meaning of the code
  – A local transformation is safe if the transformed basic block is guaranteed to be equivalent to its original form
• We will sketch several local optimization techniques
Equivalence of Basic Blocks

- Two basic blocks are (semantically) equivalent if they compute the same set of expressions.

```
| b   | := | 0  |
| t1  | := | a + b |
| t2  | := | c * t1 |
| a   | := | t2  |
```

```
| a   | := | c * a       |
| b   | := | 0           |
```

Blocks are equivalent, assuming `t1` and `t2` are dead: no longer used (no longer live).
DAG representation of basic blocks

1. One leaf for the initial value of each variable in the block
2. One node N for each statement s. Children are statements producing values of needed operands
3. Node N is labeled by the operator of s, and by the list of variables for which it defines the last value in the block
4. “Output nodes” are labeled by live on exit variables, determined with global analysis

Example:

\[
\begin{align*}
  a &:= b + c \\
  b &:= a - d \\
  c &:= b + c \\
  d &:= a - d \\
\end{align*}
\]
Common-Subexpression Elimination

• Remove redundant computations

```
a := b + c
b := a - d
c := b + c
d := a - d
```

```
a := b + c
b := a - d
c := b + c
d := b
```

```
t1 := b * c
t2 := a - t1
t3 := b * c
t4 := t2 + t3
```

```
t1 := b * c
t2 := a - t1
t4 := t2 + t1
```
Dead Code Elimination

- Remove unused statements

\[
\begin{align*}
\text{if true goto L2} \\
b &:= x + y \\
\ldots
\end{align*}
\]

Removing unreachable code

- In the DAG: remove any root having no live variable attached, and iterate

\[
\begin{align*}
b &:= a + 1 \\
a &:= b + c \\
\ldots
\end{align*}
\]

Assuming \texttt{a} is dead (not used)
Algebraic Transformations

- Change arithmetic operations to transform blocks to algebraic equivalent forms

\[
\begin{align*}
t_1 & := a - a \\
t_2 & := b + t_1 \\
t_3 & := 2 * t_2
\end{align*}
\]

\[
\begin{align*}
t_1 & := 0 \\
t_2 & := b \\
t_3 & := t_2 \ll 1
\end{align*}
\]

- Algebraic identities (e.g. comm/assoc of operators)
  → has to conform the language specification
- Reduction in strength
- Constant folding
Renaming Temporary Variables

• Temporary variables that are dead at the end of a block can be safely renamed

\[
\begin{align*}
t_1 &: = b + c \\
t_2 &: = a - t_1 \\
t_1 &: = t_1 \times d \\
d &: = t_2 + t_1
\end{align*}
\]

\[
\begin{align*}
t_1 &: = b + c \\
t_2 &: = a - t_1 \\
t_3 &: = t_1 \times d \\
d &: = t_2 + t_3
\end{align*}
\]

Normal-form block
Interchange of Statements

- Independent statements can be reordered

```
  t1 := b + c
  t2 := a - t1
  t3 := t1 * d
  d := t2 + t3
```

```
  t1 := b + c
  t3 := t1 * d
  t2 := a - t1
  d := t2 + t3
```

Note that normal-form blocks permit all statement interchanges that are possible