

Principles of Programming Languages

<http://www.di.unipi.it/~andrea/Didattica/PLP-14/>

Prof. Andrea Corradini

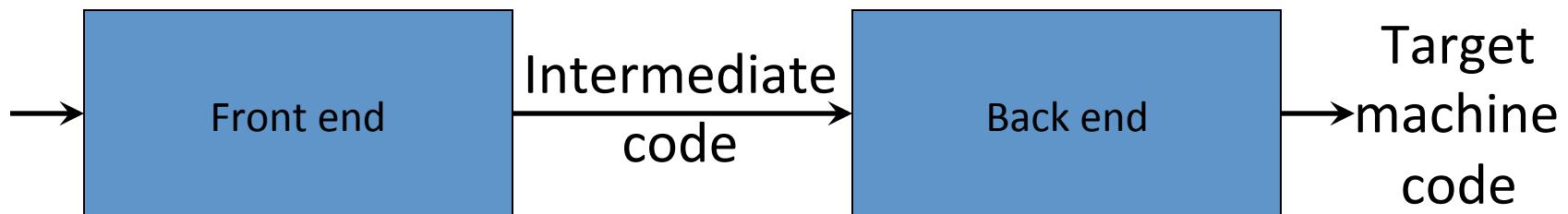
Department of Computer Science, Pisa

Lesson 12

- Intermediate-Code Generation
 - Three-address code

Intermediate Code Generation

- Facilitates *retargeting*: enables attaching a back end for the new machine to an existing front end



- Enables machine-independent code optimization

Summary

- Intermediate representations
- Three address statements and their implementations
- Syntax-directed translation to three address statements
 - Expressions and statements
- Handling local names and scopes with symbol tables
- Syntax-directed translation of
 - Declarations in scope
 - Expressions in scope
 - Statements in scope

Intermediate Representations

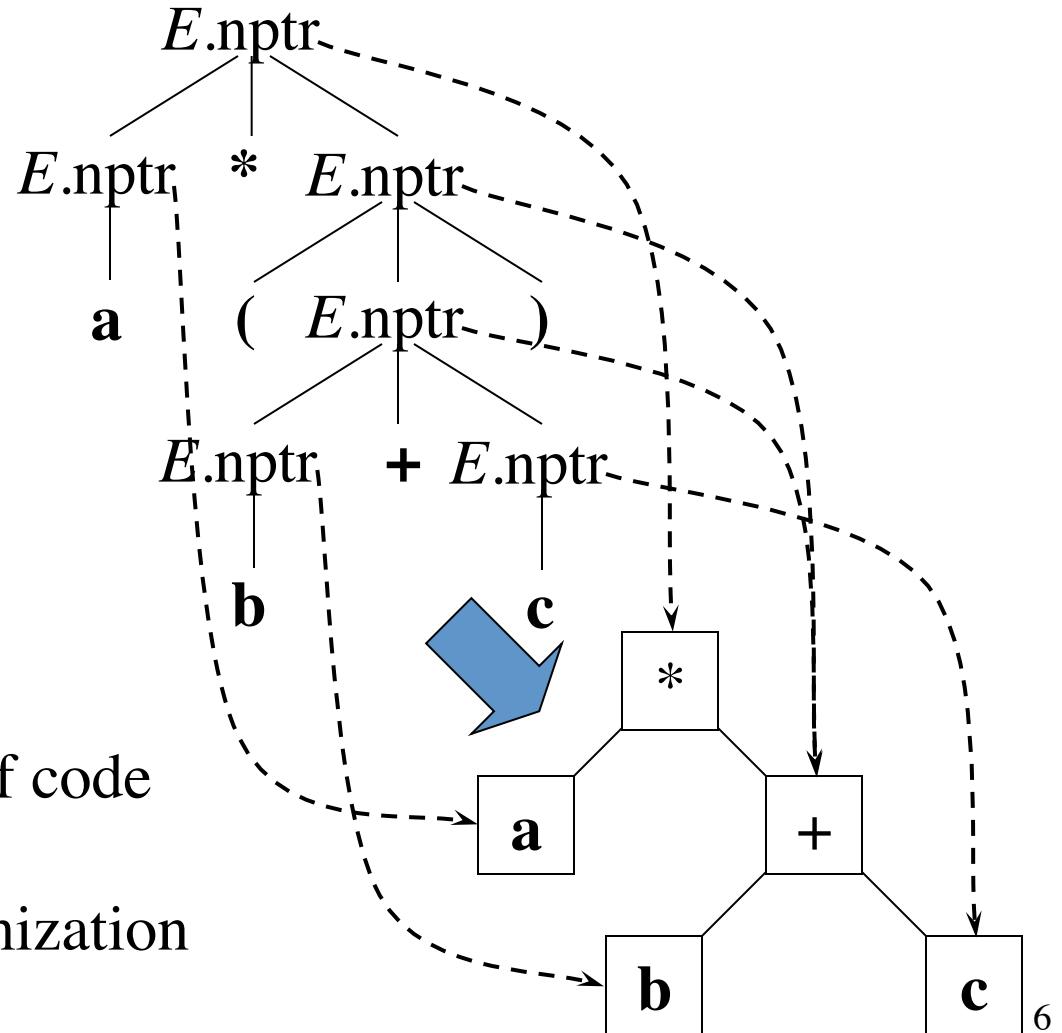
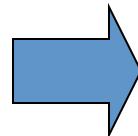
- *Graphical representations* (e.g. AST)
- *Postfix notation*: operations on values stored on operand stack (similar to JVM bytecode)
- *Three-address code*: (e.g. *triples* and *quads*)
 $x := y \text{ op } z$
- *Two-address code*:
 $x := \text{op } y$
which is the same as $x := x \text{ op } y$

Syntax-Directed Translation of Abstract Syntax Trees

Production	Semantic Rule
$S \rightarrow \mathbf{id} := E$	$S.\text{nptr} := \text{mknode}(\text{'':=}', \text{mkleaf}(\mathbf{id}, \mathbf{id}.\text{entry}), E.\text{nptr})$
$E \rightarrow E_1 + E_2$	$E.\text{nptr} := \text{mknode}(\text{'+'}, E_1.\text{nptr}, E_2.\text{nptr})$
$E \rightarrow E_1 * E_2$	$E.\text{nptr} := \text{mknode}(\text{'*'}, E_1.\text{nptr}, E_2.\text{nptr})$
$E \rightarrow -E_1$	$E.\text{nptr} := \text{mknode}(\text{'uminus'}, E_1.\text{nptr})$
$E \rightarrow (E_1)$	$E.\text{nptr} := E_1.\text{nptr}$
$E \rightarrow \mathbf{id}$	$E.\text{nptr} := \text{mkleaf}(\mathbf{id}, \mathbf{id}.\text{entry})$

Abstract Syntax Trees

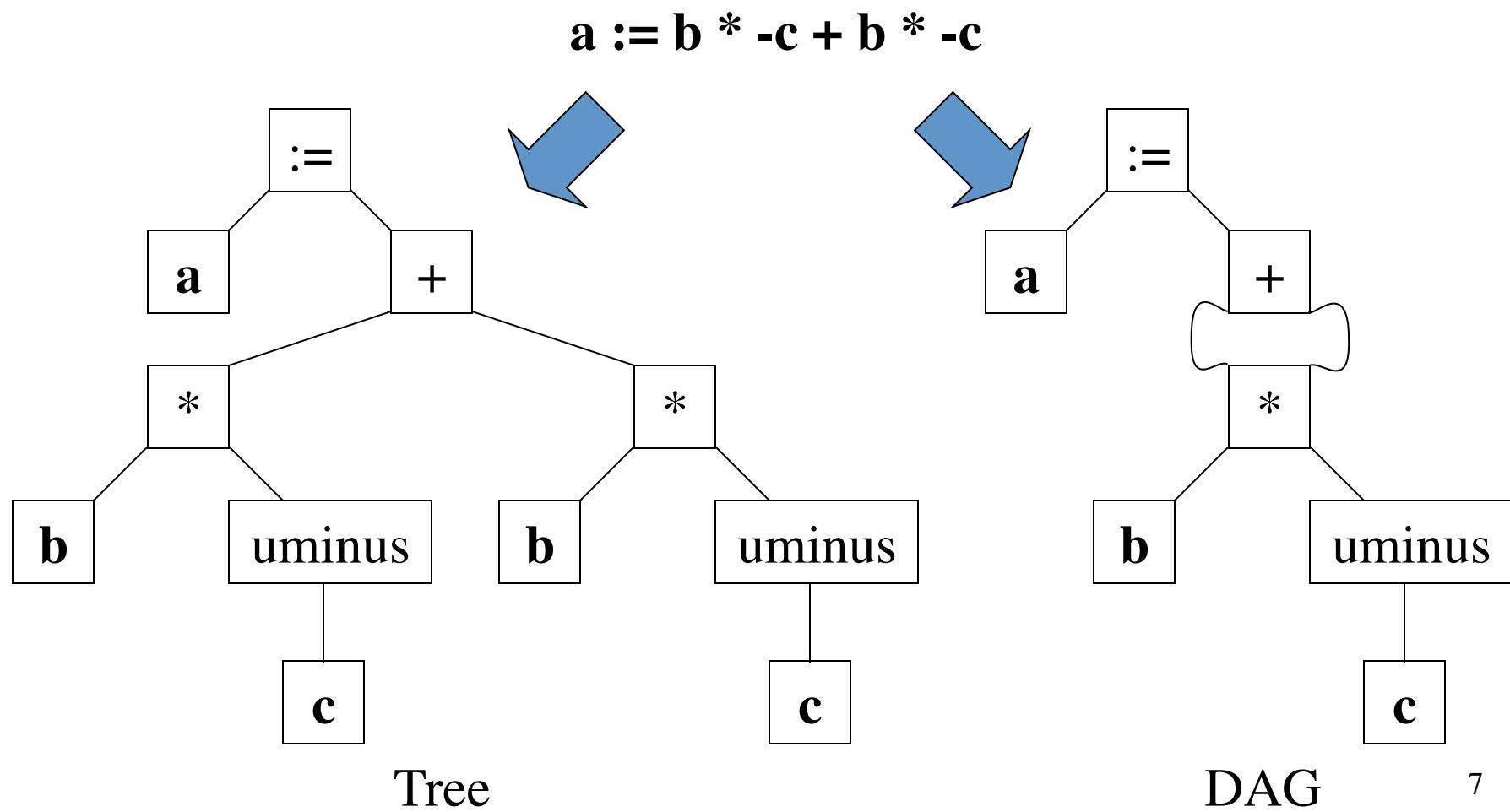
$a * (b + c)$



Pro: easy restructuring of code
and/or expressions for
intermediate code optimization

Cons: memory intensive

Abstract Syntax Trees versus DAGs



Postfix Notation

$a := b * -c + b * -c$



a b c uminus * b c uminus * + assign

Postfix notation represents operations on a stack

Pro: easy to generate

Cons: stack operations are more difficult to optimize

Bytecode (for example)

```
iload 2    // push b
iload 3    // push c
ineg       // uminus
imul       // *
iload 2    // push b
iload 3    // push c
ineg       // uminus
imul       // *
iadd       // +
istore 1   // store a 8
```

Three-Address Code

$a := b * -c + b * -c$



```
t1 := - c  
t2 := b * t1  
t3 := - c  
t4 := b * t3  
t5 := t2 + t4  
a   := t5
```

```
t1 := - c  
t2 := b * t1  
t5 := t2 + t2  
a   := t5
```

Linearized representation
of a syntax tree

Linearized representation
of a syntax DAG

Three-Address Statements

“Addresses” are *names*, *constants* or *temporaries*

- Assignment statements: $x := y \ op \ z$, $x := op \ y$
- Indexed assignments: $x := y[i]$, $x[i] := y$
- Pointer assignments: $x := \&y$, $x := *y$, $*x := y$
- Copy statements: $x := y$
- Unconditional jumps: **goto** *lab*
- Conditional jumps: **if** *x relop y goto* *lab*
- Function calls: **param** *x... ; call p, n*
(or *y = call p, n ; return y*)

Implementation of Three-Address Statements: Quads

Sample expression

$a := b * -c + b * -c$

Three-address code

```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a := t5
```

#	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>	<i>Res</i>
(0)	uminus	c		t1
(1)	*	b	t1	t2
(2)	uminus	c		t3
(3)	*	b	t3	t4
(4)	+	t2	t4	t5
(5)	:=	t5		a

Quads (quadruples)

- Pro: easy to rearrange code for global optimization
- Cons: lots of temporaries

Implementation of Three-Address Statements: Triples

Sample expression

$a := b * -c + b * -c$

Three-address code

```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a := t5
```

#	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>
(0)	uminus	c	
(1)	*	b	(0)
(2)	uminus	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	:=	a	(4)

Triples

Pro: temporaries are implicit

Cons: difficult to rearrange code

Implementation of Three-Address Statements: Indirect Triples

#	Stmt		#	Op	Arg1	Arg2
(0)	(14)	→	(14)	uminus	c	
(1)	(15)	→	(15)	*	b	(14)
(2)	(16)	→	(16)	uminus	c	
(3)	(17)	→	(17)	*	b	(16)
(4)	(18)	→	(18)	+	(15)	(17)
(5)	(19)	→	(19)	:=	a	(18)

Program

Triple container

Pro: temporaries are implicit & easier to rearrange code

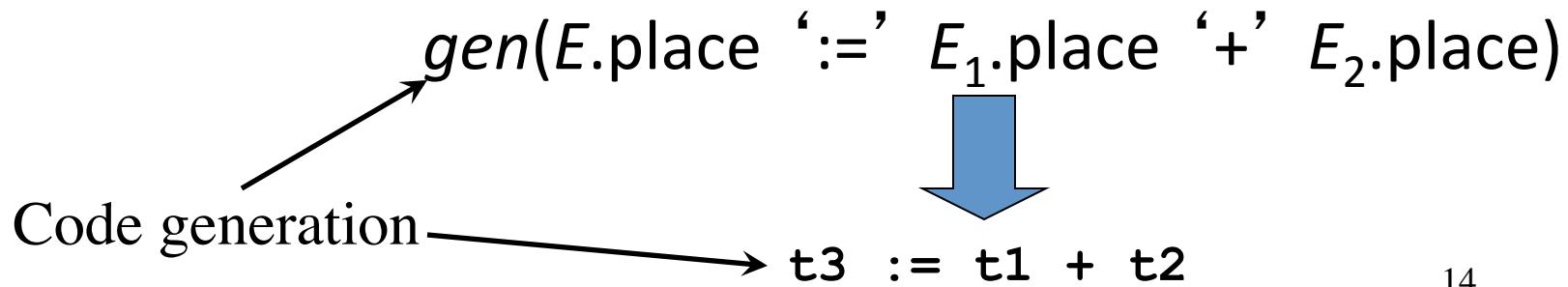
Syntax-Directed Translation into Three-Address Code

Productions

$$\begin{aligned} S \rightarrow & \mathbf{id} := E \\ & | \text{while } E \text{ do } S \\ E \rightarrow & E + E \\ & | E * E \\ & | -E \\ & | (E) \\ & | \mathbf{id} \\ & | \mathbf{num} \end{aligned}$$

Synthesized attributes:

$S.\text{code}$	three-address code for S
$S.\text{begin}$	label to start of S or nil
$S.\text{after}$	label to end of S or nil
$E.\text{code}$	three-address code for E
$E.\text{place}$	a name holding the value of E



Syntax-Directed Translation into Three-Address Code (cont'd)

Productions	Semantic rules
$S \rightarrow \mathbf{id} := E$	$S.\text{code} := E.\text{code} \parallel \text{gen}(\mathbf{id}.\text{place} \text{ `:='} E.\text{place}); S.\text{begin} := S.\text{after} := \text{nil}$ <i>(see next slide)</i>
$S \rightarrow \mathbf{while } E$ $\mathbf{do } S_1$	
$E \rightarrow E_1 + E_2$	$E.\text{place} := \text{newtemp}();$ $E.\text{code} := E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(E.\text{place} \text{ `:='} E_1.\text{place} \text{ `+' } E_2.\text{place})$
$E \rightarrow E_1 * E_2$	$E.\text{place} := \text{newtemp}();$ $E.\text{code} := E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(E.\text{place} \text{ `:='} E_1.\text{place} \text{ `*' } E_2.\text{place})$
$E \rightarrow - E_1$	$E.\text{place} := \text{newtemp}();$ $E.\text{code} := E_1.\text{code} \parallel \text{gen}(E.\text{place} \text{ `:='} \text{'uminus'} E_1.\text{place})$
$E \rightarrow (E_1)$	$E.\text{place} := E_1.\text{place}$ $E.\text{code} := E_1.\text{code}$
$E \rightarrow \mathbf{id}$	$E.\text{place} := \mathbf{id}.\text{name}$ $E.\text{code} := \text{`'}$
$E \rightarrow \mathbf{num}$	$E.\text{place} := \text{newtemp}();$ $E.\text{code} := \text{gen}(E.\text{place} \text{ `:='} \mathbf{num}.\text{value})$

Syntax-Directed Translation into Three-Address Code (cont'd)

Production

$S \rightarrow \text{while } E \text{ do } S_1$

Semantic rule

$S.\text{begin} := \text{newlabel}()$

$S.\text{after} := \text{newlabel}()$

$S.\text{code} := \text{gen}(S.\text{begin} ':') \parallel$

$E.\text{code} \parallel$

$\text{gen}(\text{'if'} \ E.\text{place} \ '=' \ '0' \ \text{'goto'} \ S.\text{after}) \parallel$

$S_1.\text{code} \parallel$

$\text{gen}(\text{'goto'} \ S.\text{begin}) \parallel$

$\text{gen}(S.\text{after} ':')$

$S.\text{begin}:$

$E.\text{code}$

$\text{if } E.\text{place} = 0 \text{ goto } S.\text{after}$

$S.\text{code}$

$\text{goto } S.\text{begin}$

\dots

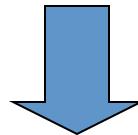
$S.\text{after}:$

Example

i := 2 * n + k

while i do

i := i - k



t1 := 2

t2 := t1 * n

t3 := t2 + k

i := t3

L1: if i = 0 goto L2

t4 := i - k

i := t4

goto L1

L2:

Names and Scopes

- The three-address code generated by the syntax-directed definitions shown is simplistic
- It assumes that the names of variables can be easily resolved by the back-end in global or local variables
- We need local symbol tables to record global declarations as well as local declarations in procedures, blocks, and structs to resolve names

Symbol Tables for Scoping

```
struct S  
{ int a;  
    int b;  
} s;
```

We need a symbol table for the *fields* of struct S

```
void swap(int& a, int& b)  
{ int t;  
    t = a;  
    a = b;  
    b = t;  
}
```

Need symbol table for *global* variables and functions

```
void somefunc()  
{ ...  
    swap(s.a, s.b);  
    ...  
}
```

Need symbol table for *arguments* and *locals* for each function

Check: **s** is global and has fields **a** and **b**
Using symbol tables we can generate code to access **s** and its fields

Offset and Width for Runtime Allocation

```
struct S  
{ int a;  
  int b;  
} s;
```

```
void swap(int& a, int& b)  
{ int t;  
  t = a;  
  a = b;  
  b = t;  
}
```

```
void somefunc()  
{ ...  
  swap(s.a, s.b);  
  ...  
}
```

The fields **a** and **b** of struct **S** are located at *offsets* 0 and 4 from the start of **S**

The *width* of **S** is 8

a	(0)
b	(4)

Subroutine frame holds arguments **a** and **b** and local **t** at *offsets* 0, 4, and 8

Subroutine frame

fp[0]=	a	(0)
fp[4]=	b	(4)
fp[8]=	t	(8)

The *width* of the frame is 12

Symbol Tables for Scoping

```
struct S
{ int a;
  int b;
} s;

void swap(int& a, int& b)
{ int t;
  t = a;
  a = b;
  b = t;
}

void foo()
{
  ...
  swap(s.a, s.b);
  ...
}
```

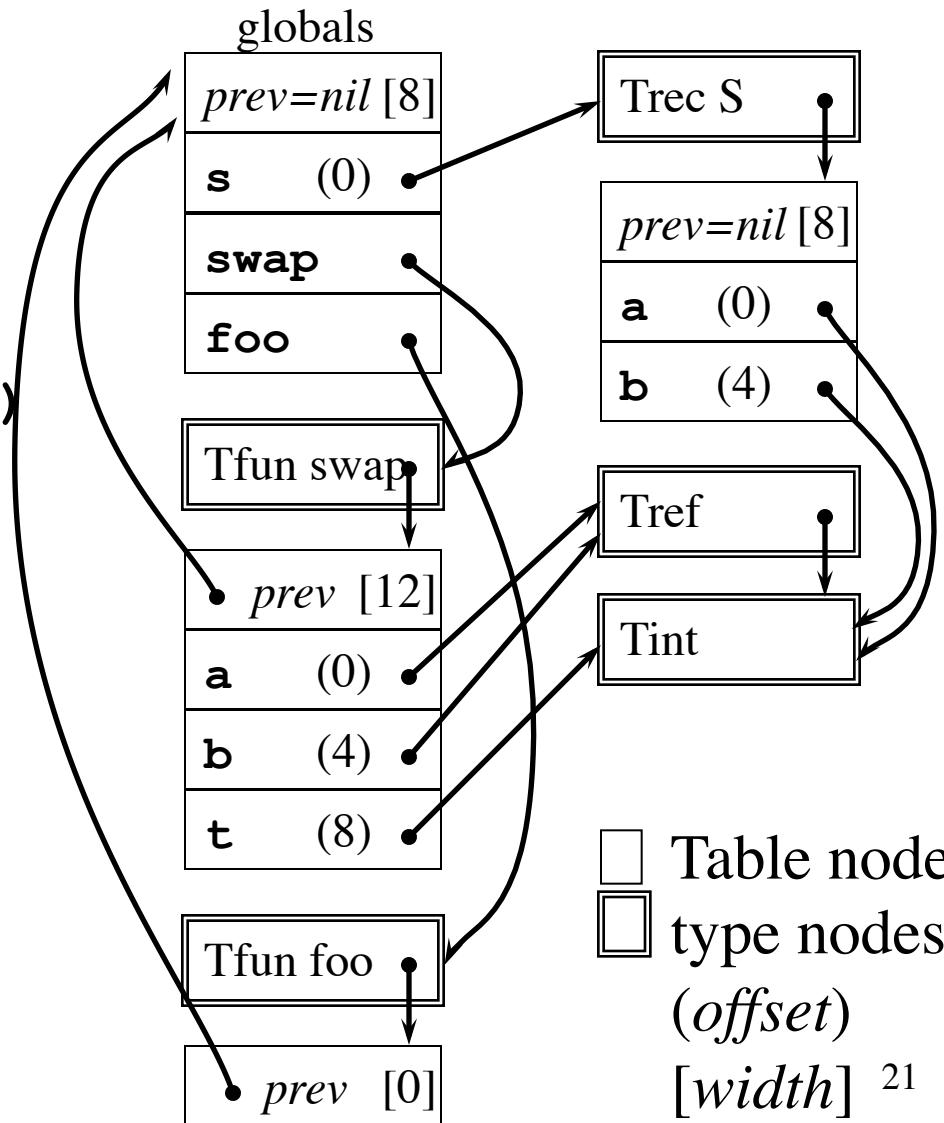


Table nodes
type nodes
(offset)
[width] 21

Hierarchical Symbol Table Operations

- $mktabc(previous)$ returns a pointer to a new (empty) table that is linked to a previous table in the outer scope
- $enter(table, name, type, offset)$ creates a new entry in $table$
- $addwidth(table, width)$ accumulates the total width of all entries in $table$
- $enterproc(table, name, newtable)$ creates a new entry in $table$ for procedure with local scope $newtable$
- $lookup(table, name)$ returns a pointer to the entry in the table for $name$ by following linked tables

Syntax-Directed Translation of Declarations in Scope

Productions

$$P \rightarrow D ; S$$

$$D \rightarrow D ; D$$

$$| \text{id} : T$$

$$| \text{proc id} ; D ; S$$

$$T \rightarrow \text{integer}$$

$$| \text{real}$$

$$| \text{array [num] of } T$$

$$| ^T$$

$$| \text{record } D \text{ end}$$

$$S \rightarrow S ; S$$

$$| \text{id} := E$$

$$| \text{call id (} A \text{)}$$

Productions (*cont'd*)

$$E \rightarrow E + E$$

$$| E * E$$

$$| - E$$

$$| (E)$$

$$| \text{id}$$

$$| E ^$$

$$| \& E$$

$$| E . \text{id}$$

$$A \rightarrow A , E$$

$$| E$$

Synthesized attributes:

T.type pointer to type

T.width storage width of type (bytes)

E.place name of temp holding value of *E*

Global data to implement scoping:

tblptr stack of pointers to tables

offset stack of offset values

Syntax-Directed Translation of Declarations in Scope (cont'd)

$P \rightarrow \{ t := \text{mktable}(\text{nil}); \text{push}(t, \text{tblptr}); \text{push}(0, \text{offset}) \}$
 $D ; S$

$D \rightarrow \mathbf{id} : T$
 $\{ \text{enter}(\text{top}(\text{tblptr}), \mathbf{id}.\text{name}, T.\text{type}, \text{top}(\text{offset}));$
 $\quad \text{top}(\text{offset}) := \text{top}(\text{offset}) + T.\text{width} \}$

$D \rightarrow \mathbf{proc} \, \mathbf{id} \, ;$
 $\{ t := \text{mktable}(\text{top}(\text{tblptr})); \text{push}(t, \text{tblptr}); \text{push}(0, \text{offset}) \}$
 $D_1 ; S$
 $\{ t := \text{top}(\text{tblptr}); \text{addwidth}(t, \text{top}(\text{offset}));$
 $\quad \text{pop}(\text{tblptr}); \text{pop}(\text{offset});$
 $\quad \text{enterproc}(\text{top}(\text{tblptr}), \mathbf{id}.\text{name}, t) \}$

$D \rightarrow D_1 ; D_2$

Syntax-Directed Translation of Declarations in Scope (cont'd)

$T \rightarrow \text{integer} \quad \{ T.\text{type} := \text{'integer'}; T.\text{width} := 4 \}$

$T \rightarrow \text{real} \quad \{ T.\text{type} := \text{'real'}; T.\text{width} := 8 \}$

$T \rightarrow \text{array} [\text{num}] \text{ of } T_1$

$\{ T.\text{type} := \text{array}(\text{num}.val, T_1.\text{type});$
 $T.\text{width} := \text{num}.val * T_1.\text{width} \}$

$T \rightarrow ^\wedge T_1$

$\{ T.\text{type} := \text{pointer}(T_1.\text{type}); T.\text{width} := 4 \}$

$T \rightarrow \text{record}$

$\{ t := \text{mkttable}(\text{nil}); \text{push}(t, tblptr); \text{push}(0, offset) \}$

$D \text{ end}$

$\{ T.\text{type} := \text{record}(\text{top}(tblptr)); T.\text{width} := \text{top}(offset);$
 $\text{addwidth}(\text{top}(tblptr), \text{top}(offset)); \text{pop}(tblptr); \text{pop}(offset) \}$

Example

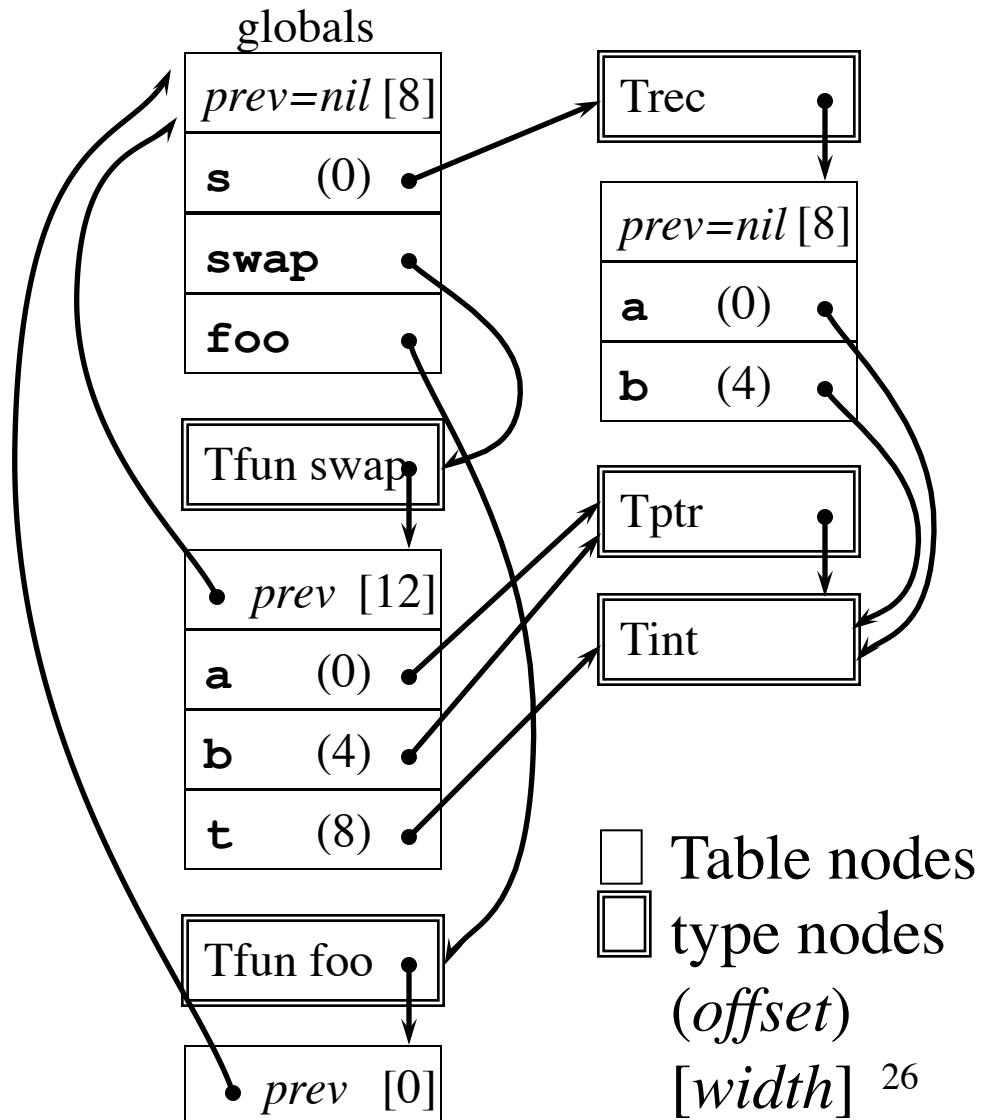
```

s: record
    a: integer;
    b: integer;
end;

proc swap;
    a: ^integer;
    b: ^integer;
    t: integer;
    t := a^;
    a^ := b^;
    b^ := t;

proc foo;
    call swap(&s.a, &s.b);

```



Syntax-Directed Translation of Statements in Scope

$S \rightarrow S ; S$

$S \rightarrow \mathbf{id} := E$

```
{ p := lookup(top(tblptr), id.name);
  if p = nil then
    error()
  else if p.level = 0 then // global variable
    emit(id.place ':=' E.place)
  else // local variable in subroutine frame
    emit(fp[p.offset] ':=' E.place) }
```

Globals

s	(0)
x	(8)
y	(12)

Subroutine
frame

fp[0]=	a	(0)
fp[4]=	b	(4)
fp[8]=	t	(8)
...		

Syntax-Directed Translation of Expressions in Scope

```
 $E \rightarrow E_1 + E_2 \quad \{ E.place := newtemp();$ 
 $\qquad \qquad \qquad emit(E.place ':= ' E_1.place '+' E_2.place) \}$ 
 $E \rightarrow E_1 * E_2 \quad \{ E.place := newtemp();$ 
 $\qquad \qquad \qquad emit(E.place ':= ' E_1.place '*' E_2.place) \}$ 
 $E \rightarrow - E_1 \quad \{ E.place := newtemp();$ 
 $\qquad \qquad \qquad emit(E.place ':= ' 'uminus' E_1.place) \}$ 
 $E \rightarrow ( E_1 ) \quad \{ E.place := E_1.place \}$ 
 $E \rightarrow \mathbf{id} \{ p := lookup(top(tblptr), \mathbf{id}.name);$ 
 $\qquad \mathbf{if} \ p = \text{nil} \ \mathbf{then} \ error()$ 
 $\qquad \mathbf{else if} \ p.level = 0 \ \mathbf{then} \ // \ global \ variable$ 
 $\qquad \qquad \qquad emit(E.place ':= ' \mathbf{id}.place)$ 
 $\qquad \mathbf{else} \ // \ local \ variable \ in \ frame$ 
 $\qquad \qquad \qquad emit(E.place ':= ' fp[p.offset]) \ }$ 
```

Syntax-Directed Translation of Expressions in Scope (cont'd)

$E \rightarrow E_1 \wedge \{ E.place := newtemp();$
 $\quad \quad \quad emit(E.place ':=*' E_1.place) \}$

$E \rightarrow \& E_1 \{ E.place := newtemp();$
 $\quad \quad \quad emit(E.place ':= '& E_1.place) \}$

$E \rightarrow \mathbf{id}_1 . \mathbf{id}_2 \{ p := lookup(top(tblptr), \mathbf{id}_1.name);$
 $\quad \quad \quad \mathbf{if} \ p = \text{nil} \ \mathbf{or} \ p.type \ != \ \text{Trec} \ \mathbf{then} \ error()$
 $\quad \quad \quad \mathbf{else}$
 $\quad \quad \quad \quad q := lookup(p.type.table, \mathbf{id}_2.name);$
 $\quad \quad \quad \quad \mathbf{if} \ q = \text{nil} \ \mathbf{then} \ error()$
 $\quad \quad \quad \quad \mathbf{else \ if} \ p.level = 0 \ \mathbf{then} \ // \ global \ variable$
 $\quad \quad \quad \quad \quad emit(E.place ':= \mathbf{id}_1.place[q.offset])$
 $\quad \quad \quad \quad \mathbf{else} \ // \ local \ variable \ in \ frame$
 $\quad \quad \quad \quad \quad emit(E.place ':= fp[p.offset+q.offset])\}$