

Predictive Top-Down: Recursive Descent using First and Follow - 1

Using functions First and Follow, we can define possibly linear, recursive descent parser.

Step 1: For each non-terminal A, Let $\{\alpha_i \mid 1 \leq i \leq n, A ::= \alpha_i \in P\}$ be the set of the production right side of the syntactic category A. Then:

```
procedure PA();  
  begin  
    case lookahead of  
      **caseof( $\alpha_1$ )** : **codeof( $\alpha_1$ )**;  
      **caseof( $\alpha_2$ )** : **codeof( $\alpha_2$ )**;  
      .....  
      **caseof( $\alpha_n$ )** : **codeof( $\alpha_n$ )**;  
    end  
  end;
```

Recursive Descent using First and Follow - 2

caseof and codeof

Step 2: For each production right side α_i , the applicability set of the production is *either* $\text{first}(\alpha_i)$ *or* $\text{first}(\alpha_i) \setminus \{\epsilon\} + \text{follow}(A)$. Then:

$$\text{caseof}(\alpha_i) = \begin{cases} \text{first}(\alpha_i) & \text{if } \epsilon \notin \text{first}(\alpha_i) \\ (\text{first}(\alpha_i) - \{\epsilon\}) \cup \text{follow}(A) & \text{otherwise} \end{cases}$$

$\text{codeof}(\alpha_i) = \text{the same of slide 1}$

As an example: The complete definition of $P_{\underline{E}}()$ is:

```
procedure  $P_{\underline{E}}()$ ;  
begin  
  case lookahead of  
    + : begin match(+);  $P_{\underline{F}}$ ;  $P_{\underline{E}}$  end  
    $ : nop  
  end  
end;
```

```
 $\underline{E} ::= F \underline{E}$   
 $\underline{E} ::= + F \underline{E}$   
 $\underline{E} ::= \epsilon$ 
```

Recursive Descent using First and Follow

Conclusive Remarks

Complexity: * linear $O(n)$ for n-words phrases

* No backtrack: A Failure means “out of the language”

One-Pass: * Parser is **moving left-to-right 1 input symbol a time.**

* Once parsed, the phrase is released in the output

Applicability: * **LL(k)** grammars (k=1 if used first as above)

* many PL syntaxes are not LL(K) for any k.

Adaptability-Modifiability: * not at all

* changes in the syntax result in a **deep re-arrangement**, up to a **complete re-definition**

Applicability i.e. $LL(K)_{/k=1}$

Property 1: $\forall A ::= \alpha \mid \beta$ [equally $\{A ::= \alpha, A ::= \beta\}$]
 $\text{first}(\alpha) \cap \text{first}(\beta) = \{\}$

Property 2: $\forall A ::= \alpha \mid \beta$ [...]
if $\alpha \Rightarrow^* \lambda$ then $\text{first}(\beta) \cap \text{follow}(A) = \{\}$

Theorem. Let G be a context free grammar:

- $G \in LL(1)$ if and only if both Properties, 1 and 2, hold
- G admits predictive, linear, 1-Lookahead Symbol Parser if and only if both Properties, 1 and 2, hold

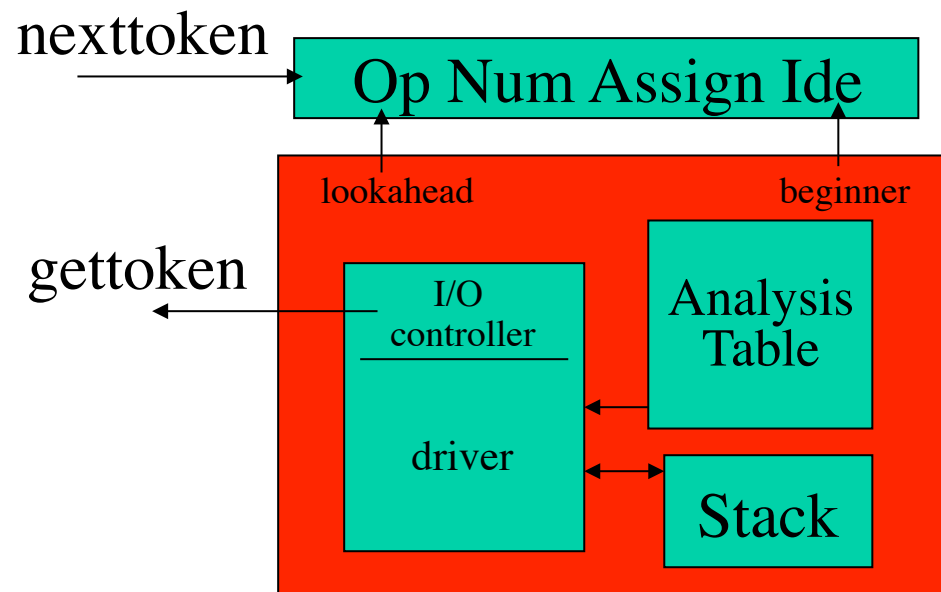
Adaptability of Recursive Descent vs. Adaptive Parser

- The need of a **deep revision of the R.D. parser code**, when syntax has to be changed, is not an inspiring idea;
- The fact that it may happen also when, the **changes are in the grammar**, more than in the syntax, makes its use **even worse** (since grammar changes are in common use, in order to find a good grammar for the syntax)
- Last but not least, the writing from scratch, of all the code for services that do not depend from the specific grammar, is a considerable time waste and source of code errors

**Adaptive Parser is the solution for enhancing adaptability
and also for constructing Parser Generators**

Adaptive Parser - Parser Generator

A view of the Structure



- **Changes** in either the syntax or the grammar **result in changes in the Analysis Table.**

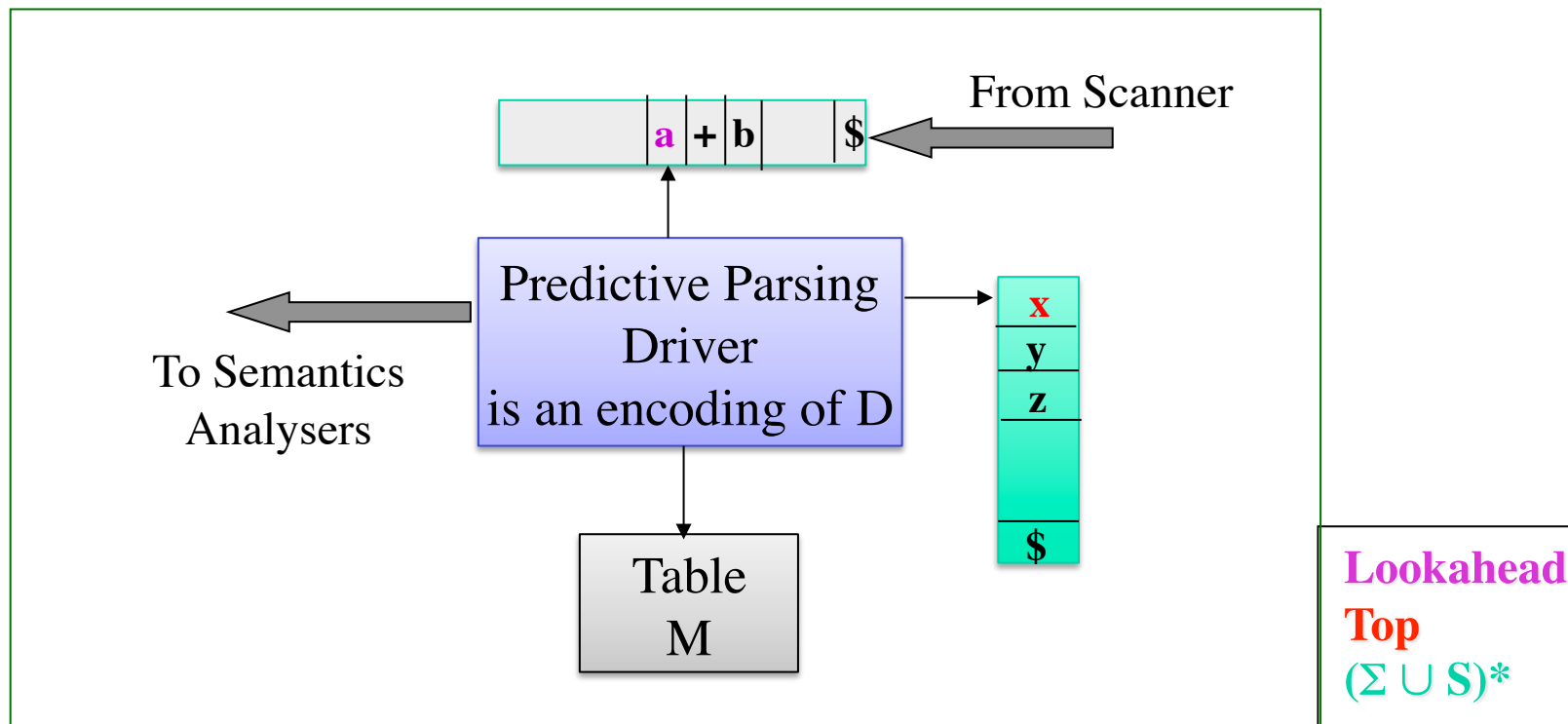
Push-Down Automata

are the perfect supports for predictive parsers

A **Pushdown Automaton** extends FSA and can be defined by the 6-tuple below:

$\langle S, \Sigma, M: S \times \Sigma \rightarrow S, D: M \times (\Sigma \cup S)^* \rightarrow (\Sigma \cup S)^*, s_0 \in S, F \subseteq S \rangle$

where S, Σ, M, s_0, F are the same of FSA, while $(\Sigma \cup S)^*$ is a stack.



Push-Down Automata

The encoding of D for LL(1) grammars

The function D for LL(1)

- top = lookahead = \$: **stop**
- top = lookahead \neq \$: **pop;**
lookahead := nexttoken
- top $\in S$: **pop;**
push(α)
where $M(\text{top}, \text{lookahead}) = \text{top} := \alpha$

Push-Down Automata

The definition of Table M for LL(1) grammars

For each grammar production $A ::= \alpha_i$

+ $\forall a \in (\text{first}(\alpha_i) - \epsilon),$

$M(A, a) := A ::= \alpha_i$

+ if $\epsilon \in \text{first}(\alpha_i)$ then:

$\forall b \in \text{follow}(A),$

$M(A, b) := A ::= \alpha_i$

+ All the remaining table entries are marked “failure”

Predictive Parser: Adaptive/Generator

To Do: In Summary

Grammar Transformation:
Left Factoring
Left Recursion Removal
Kleene's Star Removal



Costruzione tabella M
calcolo FIRST e FOLLOW

Example

Apply the construction of the adaptive/generator to a grammar (already transformed)

- | | |
|--|--|
| 0. $\underline{E} ::= F \underline{E}$ | 5. $\underline{F} ::= T \underline{F}$ |
| 1. $\underline{E} ::= + F \underline{E}$ | 6. $\underline{F} ::= * T \underline{F}$ |
| 2. $\underline{E} ::= \epsilon$ | 7. $\underline{F} ::= \epsilon$ |
| 3. $\underline{T} ::= \text{Num}$ | 8. $\underline{T} ::= \text{Ide } \underline{T}$ |
| 4. $\underline{T} ::= \text{Num}$ | 9. $\underline{T} ::= \epsilon$ |

	'+'	'*'	Ide	Num	\$
E			0	0	
\underline{E}	1				2
F			5	5	
\underline{F}	7	6			7
T			8	3	
\underline{T}	9	9		4	9

$$\begin{aligned} \text{First}(F \underline{E}) &= \{\text{Ide}, \text{Num}\} \\ \text{First}(+ \underline{F} \underline{E}) &= \{+\} \\ \text{First}(T \underline{F}) &= \{\text{Ide}, \text{Num}\} \\ \text{First}(* \underline{T} \underline{F}) &= \{*\} \end{aligned}$$

$$\begin{aligned} \text{Fw}(\underline{E}) &= \text{Fw}(E) = \{\$\} \\ \text{Fw}(\underline{F}) &= \text{Fw}(F) = \text{First}(\underline{E}\$) = \{+, \$\} \\ \text{Fw}(\underline{T}) &= \text{Fw}(T) = \text{First}(\underline{F}) \cup \text{Fw}(F) \\ &= \{*\} \cup \{+, \$\} \end{aligned}$$

Top Down:

Concluding Remarks -1

1. Consider the language $\mathbf{T} = \{u^n v^k z^m \mid n, k, m > 0, n < m\}$

a) Give a grammar G such that $L(G) = \mathbf{T}$

b) Is $G \in \text{LL}(1)$?

c) Have transformations of G , if any, predictive parsers ?

2. Consider the language $\mathbf{T} = \{u^n v^k z^m \mid n, k, m > 0, n > m\}$

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b) Is $G \in \text{LL}(1)$?

c) Have transformations of G , if any, predictive parsers ?

3. Is **LL(1)-inclusion**, decidable for Context Free Languages ?:

(Equally, let $\mathbf{F} \equiv \forall \mathbf{T}, \exists G: (L(G)=\mathbf{T} \text{ and } G \in \text{LL}(1))$).

Is \mathbf{F} a computable decision function ?

Top Down:

Concluding Remarks -2

4. Are LL(K)-Grammars strongly included in LL(1)-Grammars ?

5. Are LL(K)-Languages strongly included in LL(1)-Languages ?

6. What about conditions for LL(k)

let $G = \langle V, \Sigma, s, \Pi \rangle$

$$(\forall A ::= \beta_1 | \beta_2 \in \Pi) \text{ and } ((\forall \gamma): s \xRightarrow{*} \alpha A \gamma) \\ \text{first}_k(\beta_1 \gamma) \cap \text{first}_k(\beta_2 \gamma) = \emptyset$$

$$(\forall A ::= \beta_1 | \beta_2 \in \Pi) \\ \text{first}_k(\beta_1 \text{ follow}_k(A)) \cap \text{first}_k(\beta_2 \text{ follow}_k(A)) = \emptyset$$

Top Down:

Concluding Remarks -3

6. Definition of first_k e follow_k

$\forall G = \langle V, \Sigma, s, P \rangle,$

- $\forall \gamma \in (\Sigma \cup V)^*,$

$$\text{first}_k(\gamma) = \{ \alpha \mid \gamma \xRightarrow{*} \alpha \gamma' \wedge (|\alpha| < k \supset |\gamma'| = 0) \} \\ \cup \{ \epsilon \mid \gamma \xRightarrow{*} \lambda \}$$

- $\forall A \in V,$

$$\text{follow}_k(A) = \{ \alpha \mid \exists \delta A \gamma \in \text{LSF}_G, \alpha \in \text{first}_k(\gamma \$) \}$$

Top Down: Implementations

Parser Predittivo

Recursive Descent

- Stack:** Activation Records P calls
- Recursion:** Tail is Not Applicable
- Error Recovery:** Complicate
- Correctness:** User Competence
- Adaptability:** Low

Adaptive/Generator

- Stack:** Grammar Symbols
- Driver:** Tailored for LL-Analysis
- Error Recovery:** included in Driver
- Correctness:** Grammar
- Adaptability:** Hight

Adaptive is better because:

Tailored for LL (1) the code is written in a suitable language and possibly tested or verified, only once. (2) the code has been designed to interface in the most suitable and efficient way for the used platform.

Recovery (1) It requires the knowledge of specific techniques (2) The implementation may result hard to do when the recovery structures have to traverse the language control stasks (as in the recursive descent parsers).

Correctness: (1) Only limited to grammar correctness; (2) Safe transformations, from the grammar to the analyser, are used

Adaptability: The grammar of a language (not the syntax) is changed during implementation. For example, Javac adopted a LALR grammar for Java, obtained after many changes that affected the Abstract Syntax Tree of programs.